# COMPUTER SCIENCE TRIPOS Part II (General) DIPLOMA IN COMPUTER SCIENCE 

Thursday 3 June 19931.30 to 4.30

Paper 13 (Paper 4 of Diploma in Computer Science)

Answer five questions.
Submit the answers in five separate bundles each with its own cover sheet.
Write on one side of the paper only.

## 1 Digital Electronics and Computer Design

What is a stack?

Discuss the merits of providing small hardware stacks in a CPU for holding (a) subroutine return addresses and (b) anonymous results that occur during expression evaluation.

Sketch the design of a very fast stack, implemented in hardware, which can be used in a CPU.

## 2 Computer Structures

Write short notes on the following methods of improving the performance of a computer system:
(a) cache memory
(b) pipelining
(c) Reduced Instruction Set Computer (RISC)

## 3 Digital Communication I

Describe the properties of a physical channel which need to be considered when the channel is used for communications.

Describe how the properties of a digital synchronous channel are related to the properties of the underlying physical channel.

Describe three ways in which a protocol entity can provide higher layer channels from lower layer channels.
[6 marks]

## 4 Graphics II

Compare object-space and image-space visibility tests in synthesising an image for display.
[12 marks]
Describe one visibility test in detail.

## 5 Programming in C

Two identical packs of ordinary playing cards ( 52 different cards in a pack) are shuffled and placed face downwards on a table. Two players then play a game of Snap. Each player is allocated one pack and at each turn in the game one card in each pack is turned up and the two upturned cards are compared. If the cards are the same (i.e. match in every respect) a snap-turn is declared. A game ends when all 52 pairs have been compared.

Write a C program which will simulate the game for the purposes of determining the probability of there being at least one snap-turn in a game.
[20 marks]
Note: you may assume the existence of a random number generator but must state its properties.

## 6 Programming Language Compilation

Write notes on each of the following topics:
(a) the implementation of labels and jumps in a recursive, block structured programming language
(b) the implementation of arrays with non-constant bounds
(c) problems in the specification and implementation of Algol own variables

## 7 Artificial Intelligence II

Discuss any two methods for computing information about the three-dimensional layout of surfaces in a scene, given one or more images of the scene. Illustrate your answer with appropriate mathematical relationships and fragments of computer programs.
[20 marks]

## 8 Databases

Describe the ANSI-SPARC architecture for managing data, explaining how it enables data independence to be achieved.
[6 marks]
Outline the CODASYL/DBTG proposals for network database management, showing how they relate to the ANSI-SPARC architecture.

In what ways do the DBTG proposals compromise data independence? [3 marks]
What provision is made for data security in them?
[3 marks]

## 9 Introduction to Functional Programming

Consider the ML definition

```
datatype 'a tree = Lf | Br of 'a * 'a tree * 'a tree;
```

Say that a tree is balanced if, for each of its nodes of the form $\operatorname{Br}\left(v, t_{1}, t_{2}\right)$, the number of Br nodes in $t_{1}$ differs from the number of Br nodes in $t_{2}$ by at most one. Express this definition succinctly as an ML function of type 'a tree->bool.

Show how to implement functional arrays using binary trees, such that the root holds the value of subscript 1 , the left subtree holds the values of even subscripts, and the right subtree holds the values of odd subscripts. Explain how the update operation works, taking subscript 6 as an example.

Give an informal proof that every functional array must be represented by a balanced tree. You may assume that the array contains no gaps, i.e. the defined subscripts are $1, \ldots, n$ for some $n>0$.

Let the depth of a tree be defined by

$$
\operatorname{depth}(\operatorname{Lf})=0 \quad \text { and } \quad \operatorname{depth}\left(\operatorname{Br}\left(v, t_{1}, t_{2}\right)\right)=1+\max \left\{\operatorname{depth}\left(t_{1}\right), \operatorname{depth}\left(t_{2}\right)\right\} .
$$

State and justify precise lower and upper bounds for the number of Br nodes contained in a balanced tree of depth $d$, for arbitrary $d \geqslant 0$.

## 10 Computation Theory

Explain what is meant by the following:
' $F$ is a recursively enumerable set each of whose elements is a total recursive function $f: \mathbb{N} \rightarrow \mathbb{N}$.'

In each of the following cases state with reasons whether the set is recursively enumerable:
(a) the set $A$ of all total recursive functions $a: \mathbb{N} \rightarrow \mathbb{N}$ such that $a(n+1) \geqslant a(n)$ for all $n \in \mathbb{N}$
(b) the set $D$ of all total recursive functions $d: \mathbb{N} \rightarrow \mathbb{N}$ such that $d(n+1) \leqslant d(n)$ for all $n \in \mathbb{N}$
[10 marks]

## 11 Complexity Theory

Explain the relationship between integer and polynomial multiplication. [2 marks]
Show how the latter can be reduced to an interpolation problem which can be solved by matrix multiplication.

Starting from this idea, outline an efficient algorithm for forming the product of two $n$-bit unsigned integers.

What is the cost of the algorithm that you have described?

## 12 Formal Languages and Automata

For each of the following languages over the alphabet $\{a, b\}$, say whether or not it is regular. Justify your answers stating clearly any results that you use.
(a) The set of all strings which are not palindromes (i.e. which are not equal to their own reverse)
(b) The union of countably many regular languages $L_{1}, L_{2}, L_{3}, \ldots$
(c) The set of all strings in which the number of occurrences of the letter $a$ and the number of occurrences of the letter $b$ are both divisible by 3 [4 marks]
(d) The set of all strings which are of the form $w w$ for some string $w$ [4 marks]
(e) The set of all strings such that in each initial substring the number of occurrences of the letter $a$ and the number of occurrences of the letter $b$ differ by no more than 2
[4 marks]

