In this question you should ensure that your predicates behave appropriately with backtracking and avoid over-use of cut. You should provide an implementation of any library predicates used. You may not make use of extra-logical built-in predicates such as `findAll`. Minor syntactic errors will not be penalised.

(a) Explain the operation of cut (!) in a Prolog program. [2 marks]

(b) Rewrite `choose` without using cut. [2 marks]

```prolog
choose(0,_,[]) :- !.
choose(N,[H|T],[H|R]) :- M is N-1, choose(M,T,R).
choose(N,[_|T],R) :- choose(N,T,R).
```

(c) Explain the operation of `not` (also written as \(+\)) in a Prolog program. [1 mark]

(d) Rewrite `chooseAll` without using `not` and cut (!). [10 marks]

```prolog
chooseAll(N,L,Res) :- chooseAll(N,L,[],Res).
chooseAll(N,L,Seen,Res) :- choose(N,L,R),
    not(member(R,Seen)), !,
    chooseAll(N,L,[R|Seen],Res).
chooseAll(_,_,Res,Res).
```

(e) What is Last Call Optimisation and why is it beneficial? [3 marks]

(f) Rewrite `pos` to enable Last Call Optimisation. [2 marks]

```prolog
pos([],[]).
pos([H|T],[H|R]) :- H >= 0, pos(T,R).
pos([_|T],R) :- H < 0, pos(T,R).
```