Floating-Point Computation

(a) A hypothetical (and practically rather useless) floating-point number representation inspired by the IEEE floating-point standards uses 6 bits—one bit for sign, three bits for exponent and two (stored) bits for mantissa (significand). Assuming that 1.0 is represented in this format as 0:011:00 give the values, in decimal notation (fractions are acceptable), of all the other non-negative floating-point values in this representation. You do not need to give details of denormalised numbers or NaNs. [10 marks]

(b) Explain the following terms:

(i) absolute error;

(ii) relative error;

(iii) rounding error;

(iv) truncation error;

(v) ill-conditionedness. [5 marks]

(c) Assuming the floating-point representation for type float has b bits in its mantissa (significand), what can be said about the output of the following program?

```c
float f = 10.0/3.0;
for (i=0; i<100; i++)
{ int v = (int)f; /* get integer part of f */
  printf("%d\n", v); /* print it */
  f = (f - v) * 10;
}
```

Discuss how accurately f represents 10.0/3.0 at the start of each iteration and explain which operation(s) represent the main loss of accuracy in f on each iteration. (You may assume that 10 significant bits of accuracy is approximately 3 decimal digits of accuracy.) [5 marks]