

2005 Paper 7 Question 9

Types

- (a) State the *value-restricted* typing rule for let-expressions in ML. [5 marks]
- (b) Which of the following typing judgements are provable in the ML type system with the value-restricted rule for let-expressions? Justify your answer in each case, stating any other of the ML typing rules that you use. For part (iii) you must decide whether or not there is a type scheme σ that makes the typing provable.
- (i) $\{\} \vdash \text{let } r = \text{ref } \lambda x(x) \text{ in } (!r)(r := \lambda y(\text{true})) : \text{unit}$ [5 marks]
- (ii) $\{\} \vdash \text{let } r = \text{ref } \lambda x(x) \text{ in } (!r)(r := \lambda y(())) : \text{unit}$ [3 marks]
- (iii) $\{\} \vdash \text{let } f = \lambda x(\text{ref } x) \text{ in } f f : \sigma$ [3 marks]
- (iv) $\{x : \alpha\} \vdash \lambda f(f x) : \forall \beta((\alpha \rightarrow \beta) \rightarrow \beta)$ (where α and β are distinct type variables) [2 marks]
- (v) $\{x : \beta\} \vdash \lambda f(f x) : \forall \beta((\beta \rightarrow \beta) \rightarrow \beta)$ [2 marks]