1. Sequences
Define a function that takes a sequence (a lazy list) of integers, and produces a sequence containing the sums of adjacent pairs. So, the list \([x_1, x_2, x_3, x_4, \ldots]\) would be mapped to \([x_1 + x_2, x_3 + x_4, \ldots]\).

2. Lazier Lists
The following datatype provides an alternative implementation of lazy lists to the one given in the lectures. It avoids the unnecessary computation of the first element, when it is not required.

\[
\text{datatype 'a seq = Nil} \\
\quad | \text{Cons of unit -> 'a * 'a seq;}
\]

Modify the functions \text{hdq, tlq, from} and \text{take} to work with this datatype.

Repeat Question 1 for this datatype.

3. Structural Induction
Prove the following identities by induction on lists.

\[
(\text{map } f) \circ \text{reverse} = \text{reverse} \circ (\text{map } f)
\]

\[
\text{foldr}(\text{op ::})l_1l_2 = l_2@l_1
\]

Write a function \text{mirror} that produces the mirror image of a binary tree, i.e. the tree obtained by interchanging (recursively) the left and right child of every node.

Prove, by induction on trees, that \text{reflect(reflectt)} = t.