14: Clique Finding

Machine Learning and Real-world Data (MLRD)

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Last session: betweenness centrality

- You implemented betweenness centrality.
- This let you find "gatekeeper" nodes in the Facebook network.
- We will now turn to the task of finding clusters in networks.
- You will test this on a small network derived from one Facebook user.

Clustering in networks

- clustering: automatically grouping data according to some notion of closeness or similarity.
- agglomerative clustering works bottom-up.
- divisive clustering works top-down, by splitting.
- Newman-Girvan method a form of divisive clustering.
- Criterion for breaking links is edge betweenness centrality.
- When to stop?
 - Prespecified (today's tick): use prior knowledge to decide when to stop, based on number of clusters.
 - Inherent 'goodness of clustering' metric: today's starred tick uses **modularity** (Newman 2004).

Step 1: Code for determining connected components

- Today's graph is disconnected: there are five **connected components**.
- Finding connected components: depth-first search, start at an arbitrary node and mark the other nodes you reach.
- Repeat with unvisited nodes, until all are visited.
- Implementation hint: depth-first, so use recursion (the program stack stores the search state).

Step 2: Edge betweenness centrality

- Previously: $\sigma(s, t|v)$ the number of shortest paths between s and t going through node v.
- Now: $\sigma(s, t|e)$ the number of shortest paths between s and t going through edge e.
- Algorithm only changes in the bottom-up (accumulation) phase: $\delta(v)$ much as before, but $c_B[(v,w)]$

Brandes (2008) pseudocode

Edge betweenness

```
output: betweenness c_B[q] for q \in V \cup E (initialized to 0)
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 \begin{tabular}{|c|c|c|c|} \hline \textbf{v} & \textbf{accumulation} \\ \hline & \textbf{for } v \in V \ \textbf{do} \ \delta[v] \leftarrow 0 \\ \hline & \textbf{while } S \ not \ empty \ \textbf{do} \\ \hline & pop \ w \leftarrow S \\ \hline & \textbf{for } v \in Pred[w] \ \textbf{do} \\ \hline & c \leftarrow \frac{\sigma[v]}{\sigma[w]} \cdot (1 + \delta[w]) \\ \hline & c_B[(v,w)] \leftarrow c_B[(v,w)] + c \\ \hline & \delta[v] \leftarrow \delta[v] + c \\ \hline & \textbf{if } w \neq s \ \textbf{then} \ c_B[w] \leftarrow c_B[w] + \delta[w] \\ \hline \end{tabular}
```

Step 3: Newman-Girvan method

while number of connected subgraphs < specified number of clusters (and there are still edges):

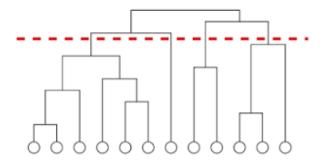
- 1 calculate edge betweenness for every edge in the graph
- 2 remove edge(s) with highest betweenness
- 3 recalculate number of connected components

Note:

Treatment of tied edges: either remove all (today) or choose one randomly.

Visualization as dendrogram

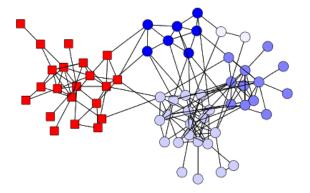
- Either: stop at prespecified level (tick).
- Or: complete process and choose best level by 'modularity' (starred tick).



Newman and Girvan (2004)

Dolphin data: different clustering layers

- squares vs circles: first split
- different colours: further splits

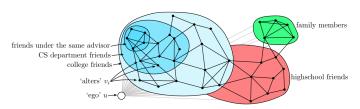


Facebook circles dataset: McAuley and Leskovec (2012)

- Designed to allow experimentation with automatic discovery of circles: Facebook friends in a particular social group.
- Profile and network data from 10 Facebook ego-networks (networks emanating from one person: referred to as an ego).
- Gold-standard circles, manually identified by the egos themselves.
- Average: 19 circles per ego, each circle with average of 22 alters.
- Complete network consists of 4,039 nodes in 193 circles.

Facebook circles

Requires more sophisticated methods than Newman-Girvan: a) nodes may be in multiple circles, b) not just network data.



25% of circles are contained completely within another circle 50% overlap with another circle 25% have no members in common with any other circle

Evaluating simple clustering

- Assume data sets with gold standard or ground truth clusters.
- But: unlike classification, we don't have labels for clusters, number of clusters found may not equal true classes.
- purity: assign label corresponding to majority class found in each cluster, then count correct assignments, divide by total elements (cf accuracy).
 - http://nlp.stanford.edu/IR-book/html/
 htmledition/evaluation-of-clustering-1.html
- But best evaluation (if possible) is **extrinsic**: use the system to do a task and evaluate that.

Clustering and classification

- Classification (e.g., sentiment classification): assigning data items to predefined classes.
- Clustering: groupings can emerge from data, unsupervised.
- Clustering for documents, images etc: anything where there's a notion of similarity between items.
- Most famous technique for hard clustering is **k-means**: very general (also variant for graphs).
- Also soft clustering: clusters have graded membership

Schedule

Task 12:

- Implement the Newman-Girvan method.
- Discover clusters in the network provided.