

Introduction to MATLAB

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<https://www.cl.cam.ac.uk/teaching/current/TeX+MATLAB/>

Computer Science Tripos – Part II

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What is MATLAB

- ▶ high-level language (garbage collecting, var-len structures)
- ▶ BASIC-like syntax, with elements from C, GUI IDE
- ▶ basic data type: 2- or 3-dimensional floating-point matrix
- ▶ most operators and functions work on entire matrices
⇒ hardly ever necessary to write out loops
- ▶ uses internally highly optimized numerics libraries (BLAS, LAPACK, FFTW)
- ▶ comprehensive toolboxes for easy access to standard algorithms from many fields: statistics, machine learning, image processing, signal processing, neural networks, wavelets, communications systems
- ▶ very simple I/O for many data/multimedia file formats
- ▶ popular for experimental/rapid-prototype number crunching
- ▶ widely used as a visualization and teaching tool

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What MATLAB is not

- ▶ not a computer algebra system
- ▶ not a strong general purpose programming language
 - limited support for other data structures
 - few software-engineering features; typical MATLAB programs are only a few lines long
 - not well-suited for teaching OOP
 - limited GUI features
- ▶ not a high-performance language (but fast matrix operators) got better since introduction of JIT compiler (JVM)
- ▶ not freely available (but local campus licence)

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Open-source MATLAB alternatives

Similar to MATLAB, or largely compatible:

- ▶ *GNU Octave*
- ▶ *SciLab*
- ▶ *FreeMat*

Other high-level languages for technical computing:

- ▶ *R* – focus on statistics and plotting
<https://www.r-project.org/>
- ▶ *Python* – a full-featured programming language. Modules:
 - *numpy* – numerical arrays, fast linear algebra
 - *matplotlib* – MATLAB-like plotting functions
<http://matplotlib.org/>
- ▶ *Julia* – interesting MATLAB-inspired modern language
<http://julialang.org/>
- ▶ *SciLua* – Scientific computing with LuaJIT
<http://scilua.org/>

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Local availability

MATLAB is installed and ready to use on

- ▶ Intel Lab, etc.: MCS Windows
- ▶ Intel Lab, etc.: MCS Linux (`/usr/bin/matlab`)
- ▶ CL MCS Linux server: `ssh -X linux.cl.ds.cam.ac.uk`
- ▶ MCS Linux server: `ssh -X linux.ds.cam.ac.uk`
- ▶ Computer Laboratory managed Linux PCs
`cl-matlab -> /usr/groups/matlab/current/bin/matlab`

Campus license allows installation on staff/student home PCs (Linux, macOS, Windows):

- ▶ <http://www.ucs.cam.ac.uk/compsoft/matlab>
- ▶ Includes toolboxes for Statistics and Machine Learning, Signal Processing, Image Processing, Bioinformatics, Control Systems, Wavelets, ...
- ▶ Installation requires setting up a <http://uk.mathworks.com/> account with your @cam.ac.uk email address.

Computer Laboratory researchers can access additional toolboxes:

- ▶ <https://www.cl.cam.ac.uk/local/sys/resources/matlab/>

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Documentation

- ▶ Full documentation built in: start `matlab` then type
 - `doc` – to browse built-in hypertext manual
 - `doc command` – to jump to a specific manual page (e.g. `plot`)
 - `help command` – to show plain-text summary of a command
- ▶ Read first: `doc` → MATLAB → Getting Started
- ▶ Tutorial videos:
<https://uk.mathworks.com/videos/>
- ▶ Documentation also available online (HTML and PDF):
 - <https://uk.mathworks.com/help/matlab/>
 - <https://uk.mathworks.com/help/> – toolboxes

Locally installed MATLAB may be half a year behind the latest release. If you spot problems with the MCS MATLAB installation, please do let the lecturer know (→ mgk25@c1.cam.ac.uk).

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MATLAB matrices (1)

Generate a “magic square” with equal row/column/diagonal sums and assign the resulting 3×3 matrix to variable `a`:

```
>> a = magic(3)
```

```
a =
```

```
     8     1     6
     3     5     7
     4     9     2
```

Assignments and subroutine calls normally end with a semicolon.

Without, MATLAB will print each result. Useful for debugging!

Results from functions not called inside an expression are assigned to the default variable `ans`.

Type `help magic` for the manual page of this library function.

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MATLAB matrices (2)

Colon generates number sequence:

```
>> 11:14
```

```
ans =
```

```
    11    12    13    14
```

```
>> -1:1
```

```
ans =
```

```
    -1     0     1
```

```
>> 3:0
```

```
ans =
```

```
Empty matrix: 1-by-0
```

Specify step size with second colon:

```
>> 1:3:12
```

```
ans =
```

```
     1     4     7    10
```

```
>> 4:-1:1
```

```
ans =
```

```
     4     3     2     1
```

```
>> 3:-0.5:2
```

```
ans =
```

```
    3.0000    2.5000    2.0000
```

Single matrix cell: `a(2,3) == 7`. Vectors as indices select several rows and columns. When used inside a matrix index, the variable `end` provides the highest index value: `a(end, end-1) == 9`. Using just “:” is equivalent to “1:end” and can be used to select an entire row or column.

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MATLAB matrices (3)

Select rows, columns and submatrices of a:

```
>> a(1,:)
ans =
     8     1     6

>> a(:,1)
ans =
     8
     3
     4

>> a(2:3,1:2)
ans =
     3     5
     4     9
```

Matrices can also be accessed as a 1-dimensional vector:

```
>> a(1:5)
ans =
     8     3     4     1     5

>> a(6:end)
ans =
     9     6     7     2

>> b = a(1:4:9)
ans =
     8     5     2

>> size(b)
ans =
     1     3
```

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MATLAB matrices (4)

Use [] to build new matrices, where , or space as a delimiter joins submatrices horizontally and ; joins them vertically.

```
>> c = [2 7; 3 1]
c =
     2     7
     3     1

>> d = [a(:,end) a(1,:)']
d =
     6     8
     7     1
     2     6

>> e = [zeros(1,3); a(2,:)]
e =
     0     0     0
     3     5     7
```

Mask matrix elements:

```
>> find(a > 5)
ans =
     1
     6
     7
     8

>> a(find(a > 5)) = 0
a =
     0     1     0
     3     5     0
     4     0     2
```

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Review: matrix multiplication

$$\begin{pmatrix} \bullet & \bullet & \bullet & \bullet \\ \bullet & \bullet & \bullet & \bullet \\ \bullet & \bullet & \bullet & \bullet \\ \bullet & \bullet & \bullet & \bullet \\ \bullet & \bullet & \bullet & \bullet \end{pmatrix} \cdot \begin{pmatrix} \bullet & \bullet & \bullet & \bullet \\ \bullet & \bullet & \bullet & \bullet \\ \bullet & \bullet & \bullet & \bullet \\ \bullet & \bullet & \bullet & \bullet \end{pmatrix}$$

Each element of the matrix product is the scalar product of the corresponding \quad in the \quad and the corresponding \quad in the \quad

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Review: inner and outer product of vectors

Special cases of matrix multiplication

$$(\bullet \quad \bullet \quad \bullet \quad \bullet) \cdot \begin{pmatrix} \bullet \\ \bullet \\ \bullet \\ \bullet \end{pmatrix} =$$

Row vector times column vector:

$$\begin{pmatrix} \bullet \\ \bullet \\ \bullet \\ \bullet \end{pmatrix} \cdot (\bullet \quad \bullet \quad \bullet \quad \bullet)$$

Column vector times row vector:

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MATLAB matrices (5)

Operators on scalars and matrices:

```
>> [1 1; 1 0] * [2 3]'  
ans =  
     5  
     2  
>> [1 2 3] .* [10 10 15]  
ans =  
    10    20    45
```

Inner and outer vector product:

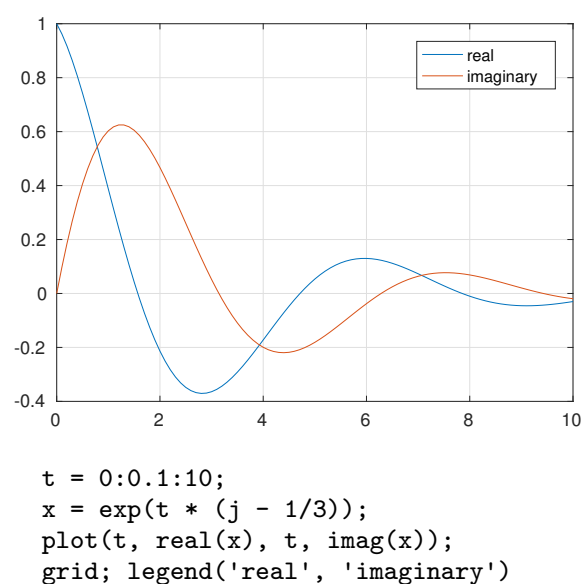
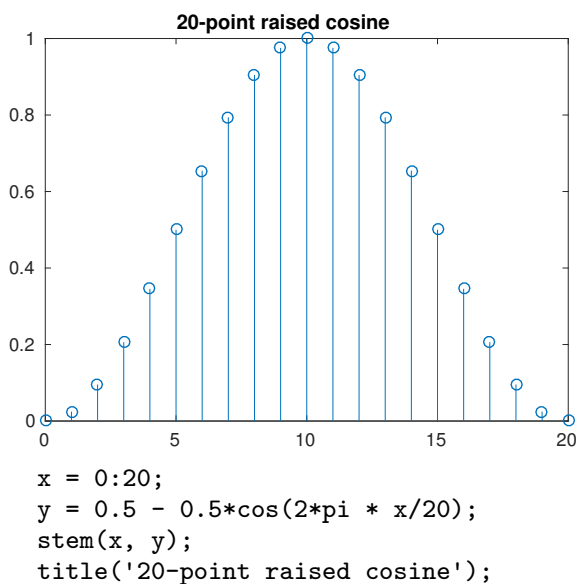
```
>> [2 3 5] * [1 7 11]'  
ans =  
     78  
>> [2 3 5]' * [1 7 11]  
ans =  
     2    14    22  
     3    21    33  
     5    35    55
```

The imaginary unit vector $\sqrt{-1}$ is available as both `i` and `j`, and matrices can be complex.

Related functions: `real`, `imag`, `conj`, `exp`, `abs`, `angle`

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Plotting

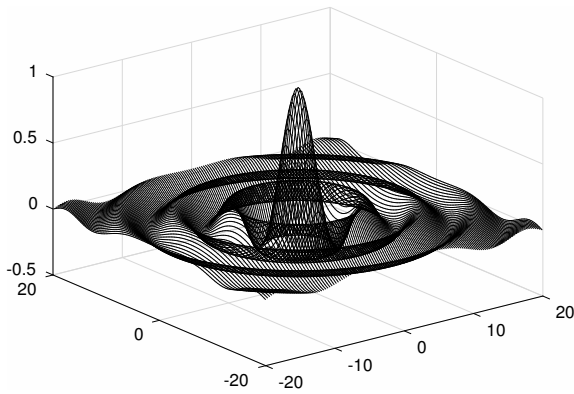


Plotting functions `plot`, `semilogx`, `semilogy`, `loglog` all expect a pair of vectors for each curve, with x and y coordinates, respectively.

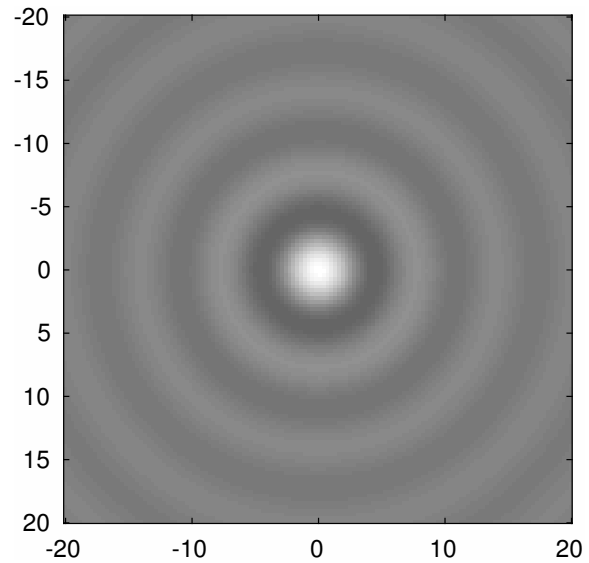
Use `saveas(gcf, 'plot2.eps')` to save current figure as graphics file.

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2D plotting



```
x1 = -20:0.3:20;
y1 = -20:0.3:20;
[x,y] = meshgrid(x1, y1);
r = sqrt(x.^2 + y.^2);
s = sin(r) ./ r; s(find(r==0)) = 1;
plot3(x, y, s);
grid on;
```



```
imagesc(x1, y1, s, [-1 1]);
colormap(gray);
set(gca, 'DataAspectRatio', [1 1 1]);
```

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Some common functions and operators

```
*, ^
matrix multiplication, exponentiation
/, \, inv
A/B = AB-1, A\B = A-1B, A-1
+, -, .*, ./, .^
element-wise add/sub/mul/div/exp
==, ~=, <, >, <=, >=
relations result in element-wise 0/1
length, size
size of vectors and matrices
zeros, ones, eye, diag
all-0, all-1, identity, diag. matrices
xlim, ylim, zlim
set plot axes ranges
xlabel, ylabel, zlabel
label plot axes
audioread, audiowrite, sound
audio I/O
csvread, csvwrite
comma-separated-value I/O
```

```
imread, imwrite, image,
imagesc, colormap
bitmap image I/O
plot, semilog{x,y}, loglog
2D curve plotting
conv, conv2, xcorr
1D/2D convolution,
cross/auto-correlation sequence
fft, ifft, fft2
discrete Fourier transform
sum, prod, min, max
sum up rows or columns
cumsum, cumprod, diff
cumulative sum or product,
differentiate row/column
find
list non-zero indices
figure, saveas
open new figure, save figure
```

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Functions and m-files

To define a new function, for example $\text{decibel}(x) = 10^{x/20}$, write into a file `decibel.m` the lines

```
function f = decibel(x)
% DECIBEL(X) converts a decibel figure X into a factor
f = 10 .^ (x ./ 20);
```

Only the function that has the same name as the m-file in which it is defined can be called from outside the file; all other functions are only visible inside the file. The `function` keyword sets the variable whose value will be returned and lists the parameter variables.

The m-file must be in the current directory (`cd`) or MATLAB's search path (`path`) to become accessible.

Use `edit db` to edit the m-file, `help db` to show the first comment lines and `type db` to show its source text.

M-files can also contain just sequences of statements instead of a function definition. These are called simply by typing their name.

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Example: generating an audio illusion

Generate an audio file with 12 sine tones of apparently continuously exponentially increasing frequency, which never leave the frequency range 300–3400 Hz. Do this by letting them wrap around the frequency interval and reduce their volume near the interval boundaries based on a raised-cosine curve applied to the logarithm of the frequency.

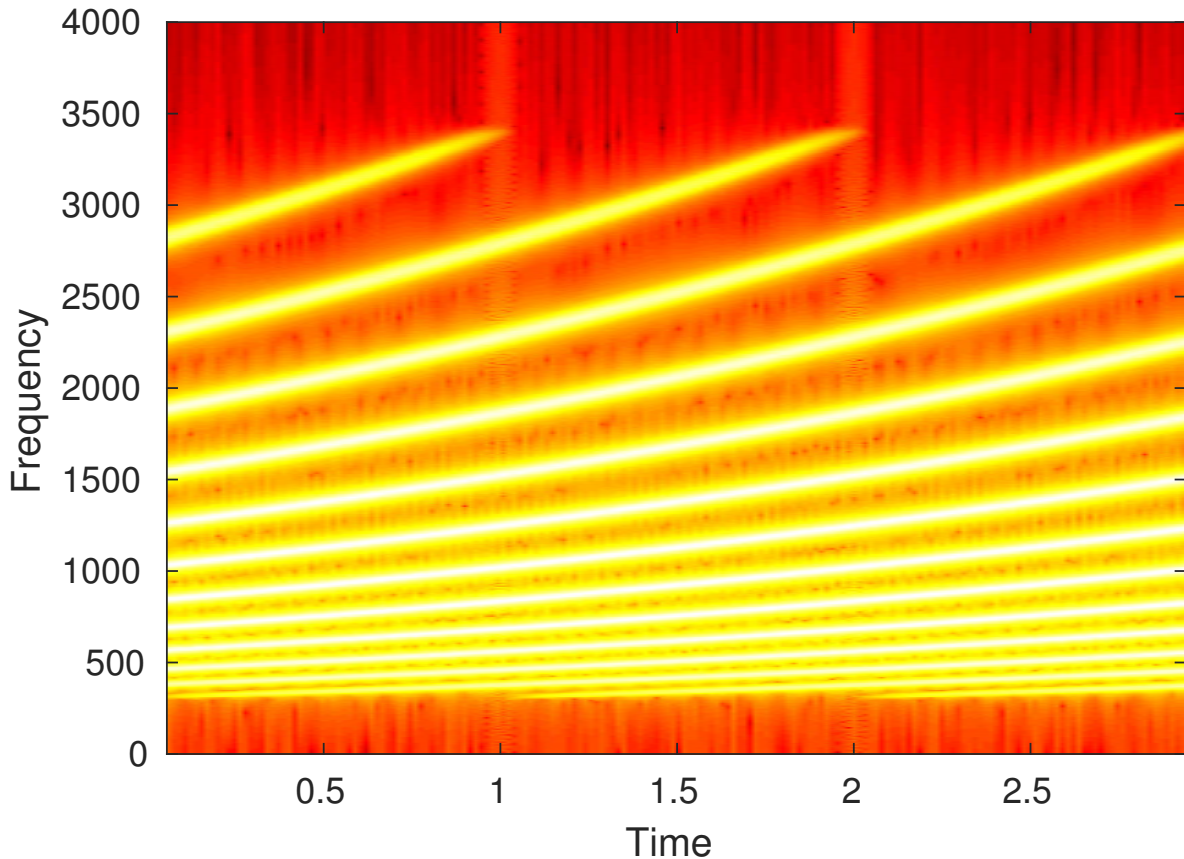
First produce a 1 s long waveform in which each tone raises 1/12 of the frequency range, then concatenate that to a 60 s long 16-bit WAV file, mono, with 16 kHz sampling rate. Avoid phase jumps.

Parameters:

```
fs = 16000; % sampling frequency [Hz]
d = 1; % time after which waveform repeats [s]
fmin = 300; % lowest frequency
fmax = 3400; % highest frequency
n = 12; % number of tones
```

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Spectrogram of the first 3 s:



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Example solution:

```

t = 0:1/fs:d-1/fs;    % timestamps for each sample point
% normalized logarithm of frequency of each tone (row)
% for each sample point (column), all rising linearly
% from 0 to 1, then wrap around back to 0
l = mod(([0:n-1]/n)' * ones(1, fs*d) + ones(n,1) * (t/(d*n)), 1);
f = fmin * (fmax/fmin) .^ l;    % freq. for each tone and sample
p = 2*pi * cumsum(f, 2) / fs;    % phase for each tone and sample
% make last column a multiple of 2*pi for phase continuity
p = diag((2*pi*floor(p(:,end))/(2*pi))) ./ p(:,end)) * p;
s = sin(p);    % sine value for each tone and sample
% mixing amplitudes from raised-cosine curve over frequency
a = 0.5 - 0.5 * cos(2*pi * l);
w = sum(s .* a)/n; % mix tones together, normalize to [-1, +1]

w = repmat(w, 1, 3);    % repeat waveform 3x
specgram(w, 2048, fs, 2048, 1800); ylim([0 4000]) % plot
w = repmat(w, 1, 20); % repeat waveform 20x
audiowrite('ladder.wav', w, fs, 'BitsPerSample', 16); % make audio file

```

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