

Lecture 6: Evaluation

Information Retrieval

Computer Science Tripos Part II

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¹Adapted from Simone Teufel's original slides

- 1 Recap/Catchup
- 2 Introduction
- 3 Unranked evaluation
- 4 Ranked evaluation
- 5 Benchmarks
- 6 Other types of evaluation

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Summary: Ranked retrieval

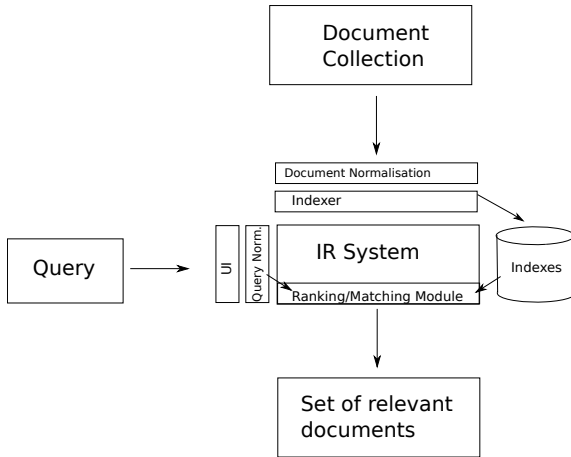
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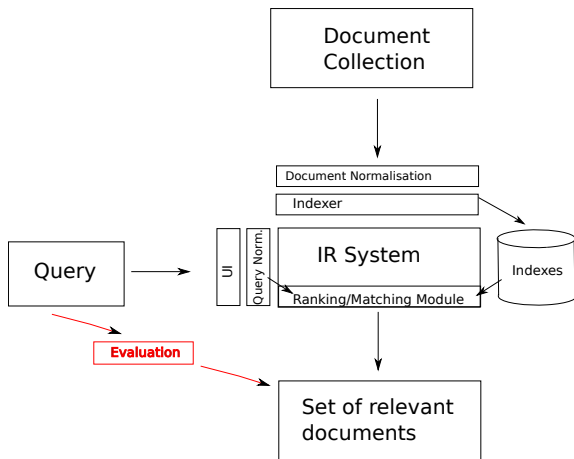
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- Language models rank based on the probability of a document model generating the query





Today: how good are the returned documents?

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 - (actually, maybe even more important: it's free)
- Note that none of these is sufficient: blindingly fast, but useless answers won't make a user happy.

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- But how do you measure relevance?
- Standard methodology in information retrieval consists of three elements.
 - A benchmark document collection
 - A benchmark suite of queries
 - An assessment of the relevance of each query-document pair

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Information need *i*

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- So what about the following document:

Document d'

At the heart of his speech was an attack on the wine industry lobby for downplaying the role of red and white wine in drunk driving.

- d' is an excellent match for query q . . .
- d' is **not** relevant to the information need i .

- User happiness can only be measured by relevance to an information need, not by relevance to queries.

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- Sloppy terminology here and elsewhere in the literature: we talk about query–document relevance judgments even though we mean information–need–document relevance judgments.

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- Recall (R) is the fraction of relevant documents that are retrieved

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Precision and recall

	Relevant	Nonrelevant
Retrieved	true positives (TP)	false positives (FP)
Not retrieved	false negatives (FN)	true negatives (TN)

THE TRUTH

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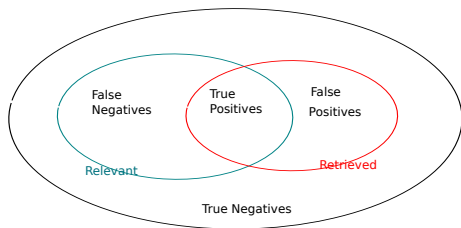
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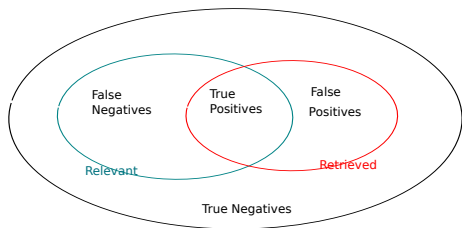
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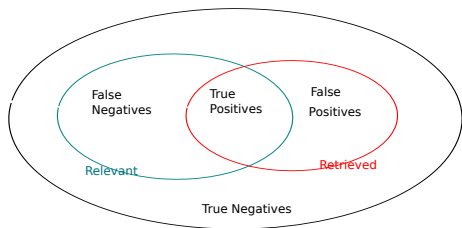


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- Recall is a non-decreasing function of the number of docs retrieved.
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- The converse is also true (usually): It's easy to get high precision for very low recall.

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$$F = \frac{1}{\alpha \frac{1}{P} + (1 - \alpha) \frac{1}{R}} = \frac{(\beta^2 + 1)PR}{\beta^2 P + R} \quad \text{where} \quad \beta^2 = \frac{1 - \alpha}{\alpha}$$

- $\alpha \in [0, 1]$ and thus $\beta^2 \in [0, \infty]$
- Most frequently used: **balanced F** with $\beta = 1$ or $\alpha = 0.5$
 - This is the **harmonic mean** of P and R : $\frac{1}{F} = \frac{1}{2} \left(\frac{1}{P} + \frac{1}{R} \right)$

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retrieved	20	40	60
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- $R = 20 / (20 + 60) = 1/4$
- $F_1 = 2 \frac{1}{\frac{1}{3} + \frac{1}{4}} = 2/7$

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- Accuracy is the fraction of decisions (relevant/nonrelevant) that are correct.
- In terms of the contingency table above,
accuracy = $(TP + TN)/(TP + FP + FN + TN)$.

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- The snoogle search engine below always returns 0 results (“0 matching results found”), regardless of the query.

The logo for snoogle.com, where the word 'snoogle' is in a blue, rounded font with a red shadow, and '.com' is in a smaller, blue, sans-serif font.

Search for:

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- Snoogle demonstrates that accuracy is not a useful measure in IR.

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- You then get 99.99% accuracy on most queries.
- Searchers on the web (and in IR in general) **want to find something** and have a certain tolerance for junk.
- It's better to return some bad hits as long as you return something.
- → We use precision, recall, and F for evaluation, not accuracy.

Recall-criticality and precision-criticality

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- But some tasks particularly need good precision whereas others need good recall:

	Precision-critical task	Recall-critical task
Time	matters	matters less
Tolerance to cases of overlooked information	a lot	none
Information Redundancy	There may be many equally good answers	Information is typically found in only one document
Examples	web search	legal search, patent search

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- For alternatives to using precision/recall and having to produce relevance judgments – see end of this lecture.

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- This is called Precision/Recall at Rank
- Rank statistics give some indication of how quickly user will find relevant documents from ranked list

Rank	Doc
1	d ₁₂
2	d ₁₂₃
3	d ₄
4	d ₅₇
5	d ₁₅₇
6	d ₂₂₂
7	d ₂₄
8	d ₂₆
9	d ₇₇
10	d ₉₀

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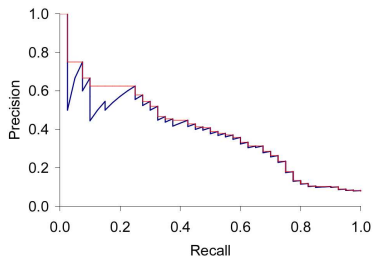
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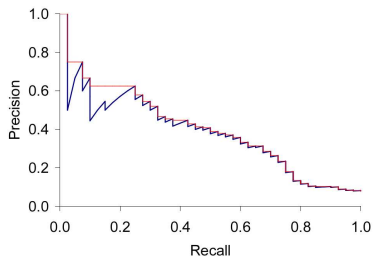
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- $R@n$: $R@3=0.33$, $R@5=0.33$, $R@8=0.66$

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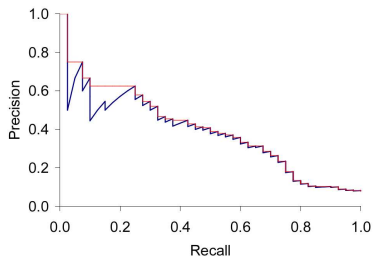


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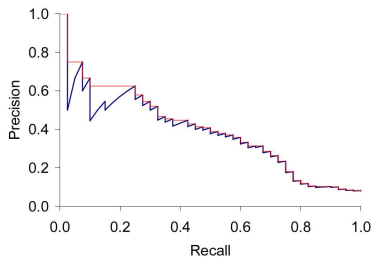
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A precision-recall curve



- Each point corresponds to a result for the top k ranked hits ($k = 1, 2, 3, 4, \dots$)
- **Interpolation (in red): Take maximum of all future points**
- Rationale for interpolation: The user is willing to look at more stuff if both precision and recall get better.

Another idea: Precision at Recall r

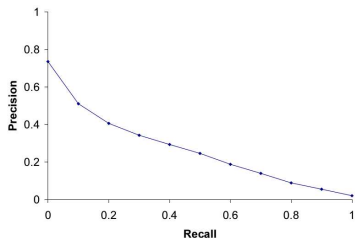
Rank	S1	S2
1	X	
2		X
3	X	
4		
5		X
6	X	X
7		X
8		X
9	X	
10	X	

→

	S1	S2
p @ r 0.2	1.0	0.5
p @ r 0.4	0.67	0.4
p @ r 0.6	0.5	0.5
p @ r 0.8	0.44	0.57
p @ r 1.0	0.5	0.63

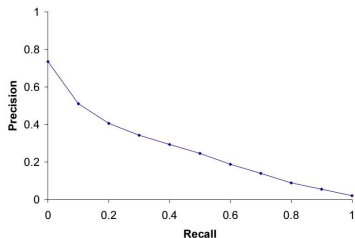
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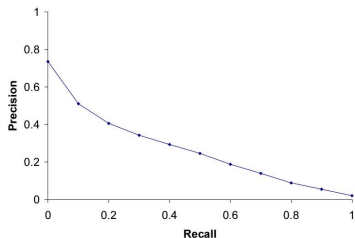
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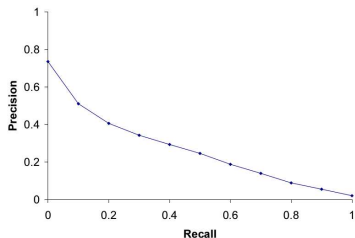
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- The curve is typical of performance levels at TREC (more later).

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with $\tilde{P}_i(r_j)$ the precision at the j th recall point in the i th query (out of N)

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- Worked avg-11-pt prec example for supervisions at end of slides.

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$$MAP = \frac{1}{N} \sum_{j=1}^N \frac{1}{Q_j} \sum_{i=1}^{Q_j} P(doc_i)$$

with:

- Q_j number of relevant documents for query j
- N number of queries
- $P(doc_i)$ precision at i th relevant document

Mean Average Precision: example

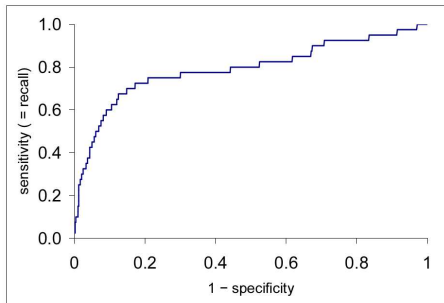
$$(MAP = \frac{0.564+0.623}{2} = 0.594)$$

Query 1		
Rank		$P(doc_i)$
1	X	1.00
2		
3	X	0.67
4		
5		
6	X	0.50
7		
8		
9		
10	X	0.40
11		
12		
13		
14		
15		
16		
17		
18		
19		
20	X	0.25
AVG:		0.564

Query 2		
Rank		$P(doc_i)$
1	X	1.00
2		
3	X	0.67
4		
5		
6		
7		
8		
9		
10		
11		
12		
13		
14		
15	X	0.2
AVG:		0.623

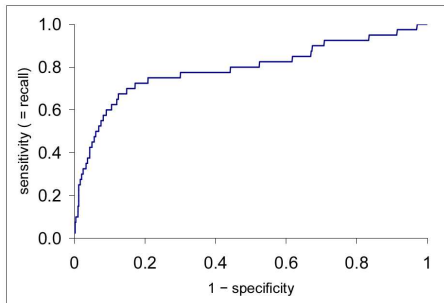
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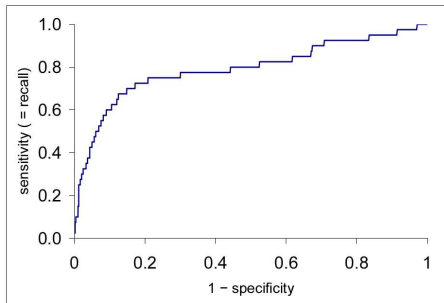
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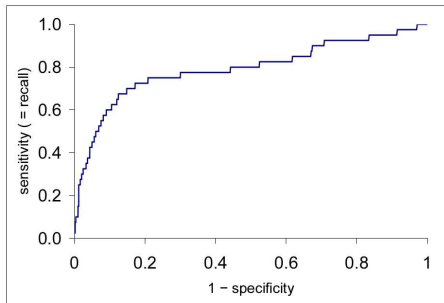
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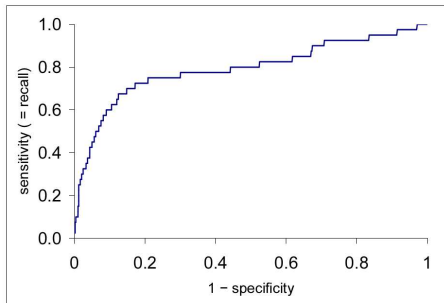
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- x-axis: FPR (false positive rate): $FP / \text{total actual negatives}$;
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- $FPR = \text{fall-out} = 1 - \text{specificity}$ (TNR; true negative rate)

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- x-axis: FPR (false positive rate): $FP / \text{total actual negatives}$;
- y-axis: TPR (true positive rate): $TP / \text{total actual positives}$, (also called sensitivity) \equiv recall
- $FPR = \text{fall-out} = 1 - \text{specificity}$ (TNR; true negative rate)
- But we are only interested in the small area in the lower left corner (blown up by prec-recall graph)

Variance of measures like precision/recall

- For a test collection, it is usual that a system does badly on some information needs (e.g., $P = 0.2$ at $R = 0.1$) and really well on others (e.g., $P = 0.95$ at $R = 0.1$).

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- Indeed, it is usually the case that the **variance of the same system across queries** is much **greater than the variance of different systems on the same query**.
- That is, there are easy information needs and hard ones.

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- 2 Introduction
- 3 Unranked evaluation
- 4 Ranked evaluation
- 5 Benchmarks**
- 6 Other types of evaluation

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- 1398 abstracts of aerodynamics journal articles, a set of 225 queries, exhaustive relevance judgments of all query-document-pairs
- Too small, too untypical for serious IR evaluation today

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- Rather, NIST assessors' relevance judgments are available only for the documents that were among the top k returned for some system which was entered in the TREC evaluation for which the information need was developed.

<num> Number: 508

<title> hair loss is a symptom of what diseases

<desc> Description:

Find diseases for which hair loss is a symptom.

<narr> Narrative:

A document is relevant if it positively connects the loss of head hair in humans with a specific disease. In this context, “thinning hair” and “hair loss” are synonymous. Loss of body and/or facial hair is irrelevant, as is hair loss caused by drug therapy.

TREC Relevance Judgements



Humans decide which document–query pairs are relevant.

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information need	number of docs judged	disagreements
51	211	6
62	400	157
67	400	68
95	400	110
127	400	106

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- Probably the evaluation methodology that large search engines trust most

Take-away today

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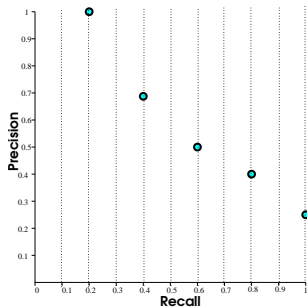
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 - slowly becoming more common
 - underlying population distributions unknown, so apply non-parametric tests such as the sign test

- MRS, Chapter 8

Worked Example avg-11-pt prec: Query 1, measured data points



- Blue for Query 1
- Bold Circles measured

Query 1			
Rank		R	P
1	X	0.2	1.00
2			
3	X	0.4	0.67
4			
5			
6	X	0.6	0.50
7			
8			
9			
10	X	0.8	0.40
11			
12			
13			
14			
15			
16			
17			
18			
19			
20	X	1.0	0.25

$$\tilde{P}_1(r_2) = 1.00$$

$$\tilde{P}_1(r_4) = 0.67$$

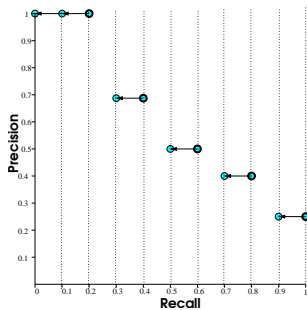
$$\tilde{P}_1(r_6) = 0.50$$

$$\tilde{P}_1(r_8) = 0.40$$

$$\tilde{P}_1(r_{10}) = 0.25$$

- Five r_j s ($r_2, r_4, r_6, r_8, r_{10}$) coincide directly with datapoint

Worked Example avg-11-pt prec: Query 1, interpolation



- Bold circles measured
- thin circles interpolated

Query 1			
Rank		R	P
1	X	.20	1.00
2			
3	X	.40	.67
4			
5			
6	X	.60	.50
7			
8			
9			
10	X	.80	.40
11			
12			
13			
14			
15			
16			
17			
18			
19			
20	X	1.00	.25

$$\tilde{P}_1(r_0) = 1.00$$

$$\tilde{P}_1(r_1) = 1.00$$

$$\tilde{P}_1(r_2) = 1.00$$

$$\tilde{P}_1(r_3) = .67$$

$$\tilde{P}_1(r_4) = .67$$

$$\tilde{P}_1(r_5) = .50$$

$$\tilde{P}_1(r_6) = .50$$

$$\tilde{P}_1(r_7) = .40$$

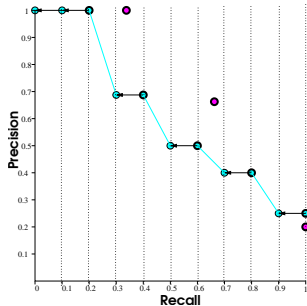
$$\tilde{P}_1(r_8) = .40$$

$$\tilde{P}_1(r_9) = .25$$

$$\tilde{P}_1(r_{10}) = .25$$

- The six other r_j s (r_0 , r_1 , r_3 , r_5 , r_7 , r_9) are interpolated.

Worked Example avg-11-pt prec: Query 2, measured data points



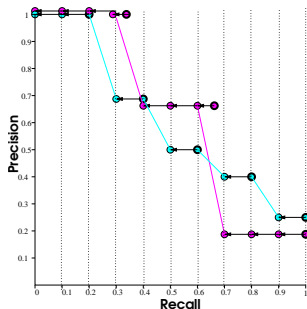
- Blue: Query 1; Red: Query 2
- Bold circles measured; thin circles interpol.

Query 2			
Rank	Relev.	R	P
1	X	.33	1.00
2			
3	X	.67	.67
4			
5			
6			
7			
8			
9			
10			
11			
12			
13			
14			
15	X	1.0	.2

$$\tilde{P}_2(r_{10}) = .20$$

- Only r_{10} coincides with a measured data point

Worked Example avg-11-pt prec: Query 2, interpolation



- Blue: Query 1; Red: Query 2
- Bold circles measured; thin circles interpol.

Query 2			
Rank	Relev.	R	P
1	X	.33	1.00
2			
3	X	.67	.67
4			
5			
6			
7			
8			
9			
10			
11			
12			
13			
14			
15	X	1.0	.2

$$\tilde{P}_2(r_0) = 1.00$$

$$\tilde{P}_2(r_1) = 1.00$$

$$\tilde{P}_2(r_2) = 1.00$$

$$\tilde{P}_2(r_3) = 1.00$$

$$\tilde{P}_2(r_4) = .67$$

$$\tilde{P}_2(r_5) = .67$$

$$\tilde{P}_2(r_6) = .67$$

$$\tilde{P}_2(r_7) = .20$$

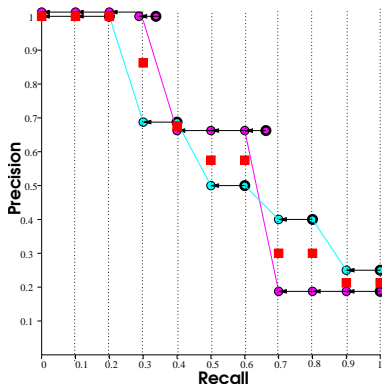
$$\tilde{P}_2(r_8) = .20$$

$$\tilde{P}_2(r_9) = .20$$

$$\tilde{P}_2(r_{10}) = .20$$

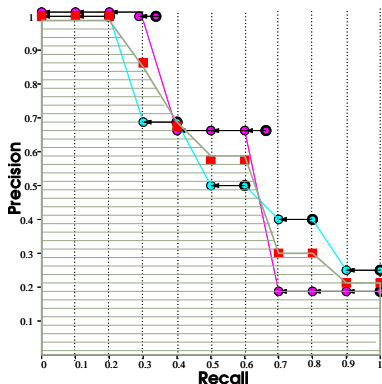
- 10 of the r_j s are interpolated

Worked Example avg-11-pt prec: averaging



- Now average at each p_j
- over N (number of queries)
- \rightarrow 11 averages

Worked Example avg-11-pt prec: area/result



- End result:
- 11 point average precision
- Approximation of area under prec. recall curve