

# Information Retrieval

## Lecture 4: Web Search

Computer Science Tripos Part II



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(Lecture Notes after Stephen Clark)

## Challenges of Web Search

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- Distributed data
  - data is stored on millions of machines with varying network characteristics
- Volatile data
  - new computers and data can be added and removed easily
  - dangling links and relocation problems
- Large volume
- Unstructured and redundant data
  - not all HTML pages are well structured
  - much of the Web is repeated (mirrored or copied)

- Quality of data
  - data can be false, invalid (e.g. out of date), SPAM
  - poorly written, can contain grammatical errors
- Heterogeneous data
  - multiple media types, multiple formats, different languages
- Unsophisticated users
  - information need may be unclear
  - may have difficulty formulating a useful query

## Web Challenges – Size of Vocabulary

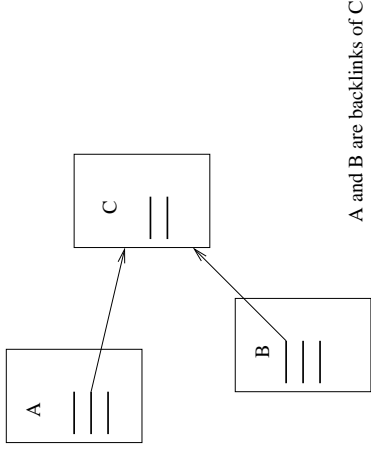
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- Heap's law:  $V = Kn^\beta$ 
  - $\beta$  is typically between 0.4 and 0.6, so vocabulary size  $V$  grows roughly with the square root of the text size  $n$
- 99% of distinct words in the VLC2 collection are not dictionary head-words (Hawking, Very Large Scale Information Retrieval)

- A characteristic of the Web is its hyperlink structure
- Web search engines exploit properties of the structure to try and overcome some of the web-specific challenges
- Basic idea: hyperlink structure can be used to infer the validity / popularity / importance of a page
  - similar to citation analysis in academic publishing
  - number of links to a page correspond with page's importance
  - links coming from an important page are indicators of other important pages
  - Anchor text describes the page
    - \* can be a useful source of text in addition to the text on the page itself, eg *Big Blue* → IBM

## PageRank

- PageRank is *query-independent* and provides a global importance score for every page on the web
  - can be calculated once for all queries
  - but can't be tuned for any one particular query
- PageRank has a simple intuitive interpretation:
  - PageRank score for a page is the probability a random surfer would visit that page
- PageRank is/was used by Google
  - PageRank is combined with other measures such as  $TF \times IDF$



- Pages with many backlinks are typically more important than pages with few backlinks
- But pages with few backlinks can also be important
  - some links, e.g. from Yahoo, are more important than other links

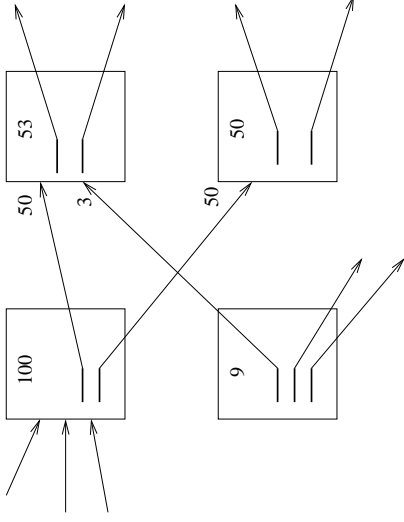
## PageRank Scoring

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- Consider a browser doing a random walk on the Web
  - start at a random page
  - at each step go to another page along one of the out-links, each link having equal probability
- Each page has a long-term visit rate (the “steady state”)
  - use the visit rate as the score

$$R(u) = d \sum_{v:v \rightarrow u} \frac{R(v)}{N_v}$$

$u$  is a web page  
 $N_v$  is the number of links from  $v$



## Teleporting

- Web is full of dead-ends
  - “long-term visit rate” doesn’t make sense
- A page may have no in-links
- *Teleporting*: jump to any page on the Web at random (with equal probability  $1/N$ )
  - when there are no out-links use teleporting
  - otherwise use teleporting with probability  $\alpha$ , or follow a link chosen at random with probability  $(1 - \alpha)$

$$R(u) = (1 - \alpha) \sum_{v:v \rightarrow u} \frac{R(v)}{N_v} + \alpha E(u)$$

- $E(u)$  is a prior distribution over web pages
- Typical value of  $\alpha$  is 0.1
- $R(u)$  can be calculated using an iterative algorithm

## Probabilistic Interpretation of PageRank

- PageRank models the behaviour of a "random surfer"
- Surfer randomly clicks on links, sometimes jumping to any page at random based on  $E$
- Probability of a random jump is  $\alpha$
- PageRank for a page is the probability that the random surfer finds himself on that page

- A Markov chain consists of  $n$  states plus an  $n \times n$  transition probability matrix  $\mathbf{P}$
- At each step, we are in exactly one of the states
- For  $1 \leq i, j \leq n$ , the matrix entry  $P_{ij}$  tells us the probability of  $j$  being the next state given the current state is  $i$
- For all  $i$ ,  $\sum_{j=1}^n P_{ij} = 1$
- Markov chains are abstractions of random walks
  - crucial property is that the distribution over next states only depends on the current state, and not how the state was arrived at

## Random Surfer as a Markov Chain

- Each state represents a web page; each transition probability represents the probability of moving from one page to another
  - transition probabilities include teleportation
- Let  $\bar{x}^t$  be the probability vector for time  $t$ 
  - $x_i^t$  is the probability of being in state  $i$  at time  $t$
- we can compute the surfer's distribution over the web pages at any time given only the initial distribution and the transition probability matrix  $\mathbf{P}$

$$x_i^t = \bar{x}^0 P^t$$

- A Markov chain is *ergodic* if the following two conditions hold:
  - For any two states  $i, j$ , there is an integer  $k \geq 2$  such that there is a sequence of  $k$  states  $s_1 = i, s_2, \dots, s_k = j$  such that  $\forall l, 1 \leq l \leq k - 1$ , the transition probability  $P_{s_l, s_{l+1}} > 0$
  - There exists a time  $T_0$  such that for all states  $j$ , and for all choices of start state  $i$  in the Markov chain, and for all  $t > T_0$ , the probability of being in state  $j$  at time  $t$  is  $> 0$

## Ergodic Markov Chains

- **Theorem:** For any ergodic Markov chain, there is a unique steady-state probability distribution over the states,  $\pi$ , such that if  $N(i, t)$  is the number of visits to state  $i$  in  $t$  steps, then

$$\lim_{t \rightarrow \infty} \frac{N(i, t)}{t} = \pi(i),$$

where  $\pi(i) > 0$  is the steady-state probability for state  $i$ .

(Introduction to IR, ch.21)

- $\pi(i)$  is the PageRank for state/web page  $i$



- The *left eigenvectors* of the transition probability matrix  $P$  are  $N$ -vectors  $\bar{\pi}$  such that

$$\bar{\pi} P = \lambda \bar{\pi}$$

- We want the eigenvector with eigenvalue 1 (this is known as the *principal*/ left eigenvector of the matrix  $P$ , and it has the largest eigenvalue)
- This makes  $\pi$  the steady-state distribution we're looking for

## PageRank Computation

- There are many ways to calculate the principal left eigenvector of the transition matrix
- One simple way:
  - Start with any distribution, eg  $\bar{x} = (1, 0, \dots, 0)$
  - After one step, distribution is  $x P$
  - After two steps, distribution is  $x P^2$
  - For large  $k$ ,  $x P^k = a$ , where  $a$  is the steady state
  - Algorithm: keep multiplying  $x$  by  $P$  until the product looks stable

- Putting all the probability mass from  $E$  onto a single page produces a personalised importance ranking relative to that page
- $E$  gives the probabilities of jumping to pages via a random jump
- Putting all the mass on one page emphasises pages "close to" that page

## HITS

- Hypertext Induced Topic Search (Kleinberg)
  - Hyperlinks encode a considerable amount of latent human judgement"
  - "The creator of page  $p$ , by including a link to page  $q$ , has in some measure *conferred authority* on  $q$ "
- Example: consider the query "Harvard"
  - `www.harvard.edu` may not use *Harvard* most often
  - but many pages containing the term *Harvard* will point at `www.harvard.edu`
- But some links are created for reasons other than conferral of authority, e.g. navigational purposes, advertisements
- Need also to balance criteria of *relevance* and *popularity*
  - e.g. lots of pages point at `www.google.com`

- An **authority** is a page which has many relevant pages pointing at it
  - authorities are likely to be relevant (precision)
  - there should be overlap between the sets of pages which point at authorities
- A **hub** is a page which links to many authorities
  - hubs help find relevant pages (recall)
  - hubs "pull-together" authorities on a common topic
  - hubs allow us to ignore non-relevant pages with a high *in-degree*
- Relationship between hubs and authorities is mutually reinforcing:
  - a good hub points to many good authorities
  - a good authority is pointed at by many good hubs

## Finding Hubs and Authorities

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- Suppose we are given some query  $\sigma$
- We wish to find authoritative pages with respect to  $\sigma$ , restricting computation to a relatively small set of pages:
  - recover top- $n$  pages using some search engine: the *root set*
  - add pages which link to the root set and pages which the root set link: the *base set*
- Base set might contain a few thousand documents, with many authorities
  - how do we find the authorities?

- Each page  $p$  has a hub weight  $h_p$  and authority weight  $a_p$
- Initially set all weights to 1
- Update weights iteratively:

$$h_p \leftarrow \sum_{q:p \rightarrow q} a_q$$

$$a_p \leftarrow \sum_{q:q \rightarrow p} h_q$$

- $p \rightarrow q$  means  $p$  points at  $q$
  - weights are normalised after each iteration
  - can prove this algorithm converges
- Pages for a given query can then be weighted by their hub and authority weights

## Calculating Hub and Authority Weights

Loop( $G, k$ ):

$G$ : a collection of  $n$  linked pages

$K$ : a natural number

Let  $z$  denote the vector  $(1, 1, 1, \dots, 1) \in \mathcal{R}^n$

Set  $\bar{a}_0 := z$

Set  $\bar{h}_0 := z$

For  $i = 1, 2, \dots, k$

Update  $\bar{a}_{i-1}$  obtaining new weights  $\bar{a}'_i$

Update  $\bar{h}_{i-1}$  obtaining new weights  $\bar{h}'_i$

Normalise  $\bar{a}'_i$  obtaining  $\bar{a}_i$

Normalise  $\bar{h}'_i$  obtaining  $\bar{h}_i$

Return  $(\bar{a}_k, \bar{h}_k)$

Query	Top Authorities
censorship	.378 <a href="http://www.eff.org/">http://www.eff.org/</a> .344 <a href="http://www.eff.org/blueribbon.html">http://www.eff.org/blueribbon.html</a> .238 <a href="http://www.cdt.org/">http://www.cdt.org/</a> .235 <a href="http://www.vtw.org/">http://www.vtw.org/</a>
"search engines"	.346 <a href="http://www.yahoo.com/">http://www.yahoo.com/</a> .291 <a href="http://www.excite.com/">http://www.excite.com/</a> .239 <a href="http://www.mckinley.com/">http://www.mckinley.com/</a> .231 <a href="http://www.lycos.com/">http://www.lycos.com/</a> .231 <a href="http://www.altavista.digital.com">http://www.altavista.digital.com</a>
Gates	.643 <a href="http://www.roadahead.com/">http://www.roadahead.com/</a> .458 <a href="http://www.microsoft.com/">http://www.microsoft.com/</a> .440 <a href="http://www.microsoft.com/corpinfo">http://www.microsoft.com/corpinfo</a>

The Electronic Frontier Foundation  
 Campaign for online free speech  
 Center for democracy & technology  
 Voters telecommunications watch  
 Yahoo  
 Excite  
 Welcome to Magellan  
 Lycos home page  
 AltaVista  
 Bill Gates: The Road Ahead  
 Welcome to Microsoft

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available online