An Attack on Server Assisted Authentication Protocols

Indexing term: Information theory

The basic server-assisted authentication protocol of Matsumoto, Kato and Imai can be broken in a one-round active attack. The improvements necessary to make it secure may well render it impractical.

Introduction: Matsumoto, Kato and Imai proposed various protocols in [1] to speed up secret computations using insecure auxiliary devices. A typical application would be where a smart card wishes to calculate an RSA signature $m^d \ (mod\ n)$ [2] on a financial transaction and wants computational assistance from a powerful server such as a digital signal processor located in a point of sale device. However, the cardholder would not wish to trust this server with d because of the risk of false terminal attacks.

This problem had been raised by Feigenbaum in [3], and the proposed solution is intended for use in production systems [4]. This would be unwise, as the server can almost trivially determine the card's secret key.

Proposed protocol: In the simplest version of the protocol, the smart card wishes to sign a message m with a secret RSA key d, that is, to calculate $m^d \ (mod\ n)$. To do this, it generates integers d_i and binary weights w_i such that

$$d = \sum_{i=0}^{k} d_i w_i \ mod\ \phi(n) \tag{1}$$

It now sends n, the vector d_i and the message m to the server, which calculates

$$z_i = m^{d_i} \ (mod\ n) \tag{2}$$

and returns the z_i. The card can now calculate m^d by multiplying together those z_i for which $w_i = 1$.

Attacking the protocol: Shimbo and Kawamura devised an active attack on a derived protocol [5], while various multi-round active and passive attacks

are discussed by Burns and Mitchell [6] and Pfitzmann and Waidner [7]. In this letter, we show a simple one-round attack on the basic protocol which reveals the card's secret key.

Instead of returning the z_i as in equation (2) above, the server chooses a random number r and returns $z_i = p_i r$ where the p_i are random primes chosen so that their product is less than n. Now when it receives $\prod_{w_i=1} z_i$ back from the card, the server repeatedly divides this number by r until the result is $\prod_{w_i=1} p_i$, which it can factor, thus obtaining w_i and hence d.

The server can now calculate the correct signature m^d for the message and forward the transaction to the network. The sale will proceed normally and so the customer has no indication that his secret key has in fact been compromised.

Can the protocol be fixed? As suggested in [5], [6] and [7], active attacks may be prevented if the card checks the signature m^d before sending it back to the server. Our attack makes such a check imperative, and this reduces the computational advantage to be gained from a protocol of this type, even when the checking is carried out using a relatively sparse public modulus.

Furthermore, as observed in [6] and [7], if the card returns a signature only when it checks, then this makes active attacks possible in which the server determines the nonzero values of w_i by trial and error. Thus the card would have to disable itself after an error was detected, or choose a new set of d_i as part of the precomputation.

It also seems likely that if the card has the storage to deal with d_i and z_i, then it might just as well be able to speed the calculation of a DSA signature by standard precomputation techniques [8]. In any case, full RSA signatures can now be calculated on smartcards in under half a second for a 512 bit modulus [9].

Server assisted protocols are therefore no longer needed in the point-of-sale environment for which they were invented, and the added complexity needed to make them secure against active attacks will probably ensure that they offer at best a marginal performance benefit, especially when the communication overheads are taken into account. It therefore quite unclear that these protocols are of any practical use.

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