

# CONSTRAINTS IN FEATURE ALGEBRA

Andreas Zelend



**UNA** Universität  
Augsburg  
University

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# THE FEATURE ALGEBRA

## GOALS

- language independent and formal characterisation of important aspects of **feature oriented software development (FOSD)**
- build an algebraic foundation for feature-structure-forests (FSFs), which represent the hierarchical structure of programs (similar to abstract syntax trees)
- provide two operations: superimposition  $+$  to compose features (recursive merging of FSFs), and modification application  $\cdot$  to modify certain parts of a feature

# EXAMPLE FST/FSF

---

```
//feature CONS
```

```
package util;
```

```
class List{
```

```
    ListNode first;
```

```
    void cons(ListNode n){
```

```
        n.next = first;
```

```
        first = n; }
```

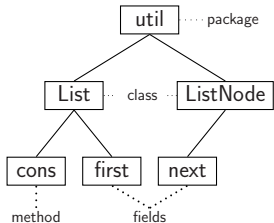
```
}
```

```
class ListNode{
```

```
    ListNode next;
```

```
}
```

---



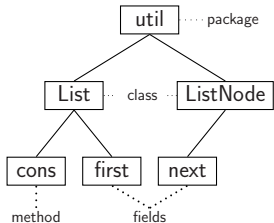
# EXAMPLE FST/FSF

```
//feature CONS
package util;

class List{
  ListNode first;

  void cons(ListNode n){
    n.next = first;
    first = n; }
}

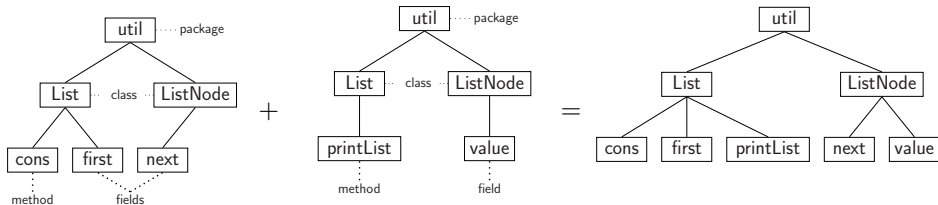
class ListNode{
  ListNode next;
}
```



Or as a prefix-free set:

$\{util.List.cons, util.List.first, util.ListNode.next\}$

# EXAMPLE SUPERIMPOSITION



$\{util.List.cons,$   
 $util.List.first,$   
 $util.ListNode.next \}$  +  $\{util.List.printList,$   
 $util.ListNode.value \} =$

$\{util.List.cons,$   
 $util.List.first,$   
 $util.List.printList,$   
 $util.ListNode.next,$   
 $util.ListNode.value \}$

# FEATURE ALGEBRA

DEFINITION (APEL, LENGAUER, MÖLLER, KÄSTNER 2010)

A **Feature Algebra** is a structure  $(M, I, +, \circ, \cdot, 0, 1)$ , with the following properties:

- $(I, +, 0)$  is a monoid in which **distant idempotence** holds, i.e.,  
 $i + j + i = j + i$ .
- $I$  is a external monoid over the structure  $(M, \circ, 1)$ , i.e.,
  - $\cdot$  is a external binary operation  $\cdot : M \times I \mapsto I$
  - $(m \circ n) \cdot i = m \cdot (n \cdot i)$
  - $1 \cdot i = i$
- $0$  is a right annihilator, i.e.,  $m \cdot 0 = 0$
- $\cdot$  distributes over  $+$ , i.e.,  $m \cdot (i + j) = (m \cdot i) + (m \cdot j)$

Elements of  $I$  are called **introductions**.

# TYPES OF CONSTRAINTS

We distinguish three main classes of constraints:

- **Low-level constraints** stem from code level. An example are **dependences** like “feature  $F$  builds on feature  $G$ ”.
- **High-level constraints** mainly originate from the program model or the problem domain.
  - **Ex:** An optional feature
- An example of a **non-functional constraint** is that “the product must run on a mobile phone and has to have less than 1 Mb of compiled source code”.

## LOW-LEVEL CONSTRAINTS

- **References** describe all code-level constraints where a method, a class, etc. refers to another object. The same type of constraint occurs when program parts are **imported**.

---

```
//feature F2
class C1{
  void foo(){
    o.something();
    ... }
}
```

---

---

```
//feature F1
class C1{
  Object o;
}
```

---

FIGURE : Low-level Constraint: Reference



## LOW-LEVEL CONSTRAINTS

- **Refinements** are similar to references. In jak, the keyword **refines** indicates that a feature builds on another. The Java keyword **extends** has the same effect.

---

```
//feature F3  
class C3{  
  ...  
}
```

---

---

```
//feature F4  
refines class C3{  
  ...  
}
```

---

FIGURE : Low-level Constraint: Refinement

We call references and refinements, which behave similarly, **structural dependences**.

## LOW-LEVEL CONSTRAINTS

- **Abstract Class Constraints** and **Interface Constraints**.  
A concrete subclass **class** C of an **abstract class** or **interface** A must implement all inherited abstract methods. Features may introduce new classes inheriting from A or may introduce new abstract methods into A.

---

```
//feature F5  
abstract class C5{  
  abstract void foo();  
}
```

---

---

```
//feature F6  
class C6 extends C5{  
  void foo(){};  
}
```

---

FIGURE : Abstract Class Constraint

# HIGH-LEVEL CONSTRAINTS

## Mandatority

- A certain feature has to be present in a product.
- **Ex:** A user requires a `toString()`-method for each class.

## Optionality

- A feature is optional in an product line.
- **Ex:** The optional feature  $F$  may be part of product  $P$ , whereas another product  $Q$  does not have  $F$ .

## Alternative

- provides a choice from a given set of features. It can be seen as “exactly one of  $m$  different features”.

# HIGH-LEVEL CONSTRAINTS

## Exclusion

- Two features are not allowed to be within the same product.
- **Ex:** If a product  $P$  has a 64-bit implementation of `foo()`,  $P$  is not allowed to have a 32-bit implementation of the same method.

## Implication

- A second feature is required.
- **Ex:** If  $P$  provides a method (feature) to allocate memory, another feature for deallocation has to be provided.

## Requirements

- The dependences between features are given by the feature model or the user.
- **Ex:** A customer demands the implementation of a printer driver whenever a function `print ()` is implemented.

# CONSTRAINTS IN FEATURE ALGEBRA

The main idea is to use triples  $(i, d, c)$  consisting of

- an introduction  $i$
- a collection  $d$  of structural dependences, again represented by an introduction
- a condition  $c$

# CONSTRAINTS IN FEATURE ALGEBRA

## EXAMPLE

---

```
//feature PRINT_LIST
package util;

class List{

    public void printList(){
        ListNode iter = first;
        while (iter != null){
            System.out.print(iter.toString()+",");
            iter = iter.next; }
        }
}

class ListNode{
    Object value;
}
```

---

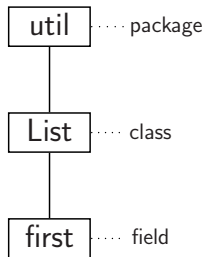


FIGURE : Structural  
Dependence of PRINT

FIGURE : Implementation of PRINT

# CONSTRAINTS IN FEATURE ALGEBRA

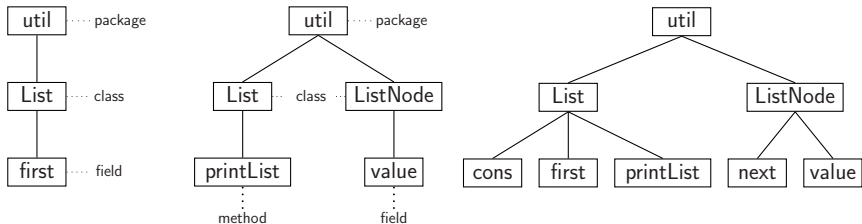
## EXAMPLE

- The introduction of PRINT (*impl*) is just its FSF
- Its structural dependence (*sdpl*) is the FSF given before
- PRINT does not impose any condition, i.e., its condition is the constant predicate **true**

The design  $D_p$  can now be defined as (*impl*, *sdpl*, **true**).

# CONSTRAINTS IN FEATURE ALGEBRA

## EXAMPLE



- $D_p$  does not satisfy its dependence ( $sdpl \not\subseteq impl$ ).
- In contrast CONS + PRINT does, since it includes  $sdpl$  as a subtree. ( $sdpl \subseteq \text{CONS} + \text{PRINT}$ )



# CONSTRAINTS IN FEATURE ALGEBRA

We model the classes of constraints using a predicate  $has(F)(i)$  that checks whether a feature  $F$  is included in a given Feature Algebra element  $i \in I$ . If  $F$  can be represented as an introduction  $f$ , this can be expressed as the condition  $has(f)(i) \iff_{df} f \leq i$ .

- Feature exclusion:  $has(F)(i) \implies \neg has(G)(i)$
- Feature implication:  $has(F)(i) \implies has(G)(i)$ .
- Abstract class constraints (and interface constraints):  
 $extends_D(i) \implies has(foo())(i)$

# CONSTRAINTS IN FEATURE ALGEBRA

## DEFINITION

Let  $A = (M, I, +, \circ, \cdot, 0, 1)$  be a Feature Algebra and  $\mathcal{P}_I$  be the set of all predicates over the introductions  $I$  of  $A$ .

- A **design** over  $A$  is an element of  $I \times I \times \mathcal{P}_I$
- A design  $(i, d, c)$  **satisfies** its **dependence**  $d$  iff  $d \leq i$
- A design  $(i, d, c)$  **satisfies** its **condition**  $c$  iff  $c(i) = \text{true}$
- A design that satisfies its dependence and its condition is called a **product**

## DEFINITION

The **conjunction** of predicates  $p, q \in \mathcal{P}_I$  is defined by  $(p \wedge q)(i) =_{df} p(i) \wedge q(i)$  for all  $i \in I$ . The predicate that maps every element of  $I$  to true is denoted by **true**.

# CONSTRAINTS IN FEATURE ALGEBRA

## DEFINITION

Assume an arbitrary set  $I$ , the set of predicates  $\mathcal{P}_I$  over  $I$  and predicates  $p, q \in \mathcal{P}_I$ .

- By  $\mathcal{PT}_I$  we denote the set of all **predicate transformers**
- A predicate transformer  $t$  is **conjunctive** if  $t(p \wedge q) = t(p) \wedge t(q)$  holds for all  $p, q \in \mathcal{P}_I$  (e.g.  $id(p) = p$  is conjunctive)
- The set of all conjunctive predicate transformers over  $A$  is denoted by  $\mathcal{CT}_I$ .
- A predicate  $p$  is called **stable** iff  $p(i) \implies p(i + j)$  for all  $j$ .

# CONSTRAINTS IN FEATURE ALGEBRA

## LEMMA

*For a set  $I$  of introductions the structure  $(\mathcal{CT}_I, \mathcal{P}_I, \wedge, \circ, \cdot, \mathbf{true}, id)$  forms a Feature Algebra.*

Now the following result is immediate by universal algebra.

## THEOREM

*For a Feature Algebra  $A = (M, I, +, \circ, \cdot, 0, 1)$  the structure  $DES_A =_{df} (M \times M \times \mathcal{CT}_I, I \times I \times \mathcal{P}_I, +, \circ, \cdot, \mathbf{0}, \mathbf{1})$  forms a Feature Algebra of designs if  $\mathbf{0} =_{df} (0, 0, \mathbf{true})$ ,  $\mathbf{1} =_{df} (1, 1, id)$  and the operations as well as modifications are lifted pointwise.*

# CONSTRAINTS IN FEATURE ALGEBRA

## LEMMA

*If the designs  $f = (i, d, b)$  and  $g = (j, e, c)$  are products and  $b$  and  $c$  are stable then the composition  $f + g$  is also a product. Furthermore if  $f$  is a product and  $(t \cdot b)(m \cdot i) = b(i)$  then  $(m, m, t) \cdot f$  is a product.*

- A design with a stable condition can be composed with another design while the condition does not change its value
- For example all  $has(f)(i)$  conditions are stable

## CONCLUSION AND OUTLOOK

- We have shown how constraints can be embedded into the abstract structure of Feature Algebra
- Future work will be directed towards representative case studies to gain a better insight into Feature Algebra and constraints