

# Anaphora and Ellipsis in Lambek Calculus with a Relevant Modality: Syntax and Semantics

Lachlan McPheat<sup>1</sup> (he/him), Gijs Wijnholds<sup>2</sup>, Mehrnoosh Sadrzadeh<sup>1</sup>, Adriana Correia<sup>2</sup>, Alexis Toumi<sup>3</sup>

<sup>1</sup>University College London, <sup>2</sup>Utrecht University, <sup>3</sup>Oxford University

# Today's Goal

How to turn the piece of language

*"John sleeps. He snores."*

into a vector?

## My bigger goal

Making distributional-compositional models of discourse

# Anaphora and Ellipsis

# Coreference

When two lexically distinct items have the same meaning.

- ▶ Ontological coreference:
  - *'Stefan Löfven' = 'Prime minister of Sweden'*
  - *'Fock Space' = 'Tensor Algebra'*
- ▶ Contextual coreference: *'He' = 'John' in "John sleeps. He snores."*

Contextual coreference refers mainly to **anaphora** and **ellipsis**

# Anaphora and Ellipsis

**Anaphora** (and cataphora) are words which receive their meaning from previously mentioned words

eg. "**John** sleeps. **He** snores."

**Ellipsis** is a type of coreference where the meaning of a whole phrase is used by a later mentioned word

eg. "John **plays guitar**. Mary **does too**."

See [Coecke et al, 2018] for nice model of discourse and probabilistic anaphora resolution!

# Anaphora and Ellipsis

Combining anaphora and ellipsis can lead to multiple possible meanings, depending on which coreference you resolve first.

"*John likes his code. Bill does too.*"

Resolving anaphora ('*his*') first yields the **strict** meaning

"*John likes John's code. Bill likes John's code.*"

Resolving the ellipsis ('*does too*') first yields the **sloppy** reading:

"*John likes John's code. Bill likes Bill's code.*"

Anaphora and Ellipsis  
via  
Type Logical Grammars

# Anaphora & Ellipsis via TLGs

[Jäger 1998, 2006] proposes method to analyse anaphora and ellipsis in type logical grammars (TLGs)

Given a discourse where  $a$  is being referred to by  $b$ :

(eg.  $a = John$  and  $b = He$  in "**John** sleeps. **He** snores.")

1. Copy the meaning of  $a$
2. Move one of the copies of  $a$  to  $b$
3. Identify  $b$  with  $a$



# Anaphora, Ellipsis and TLGs

1. Copy *a*
2. Move a copy to *b*
3. Identify

*John* sleeps. *He* snores.

# Anaphora, Ellipsis and TLGs

1. Copy *a*

2. Move a copy to *b*

3. Identify

*John*  
*John* sleeps. *He* snores.

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# Anaphora, Ellipsis and TLGs

1. Copy *a*
2. Move a copy to *b*
3. Identify

*John sleeps. **John** snores.*

# !L\* - Definition

First defined in [Kanovich et al, 2016] in a sequent calculus presentation

Fix a fixed set of atoms  $At$ , and define **formulas** of !L\* as:

$$\phi ::= \emptyset \mid \phi \in At \mid \phi, \phi \mid \phi / \phi \mid \phi \setminus \phi \mid !\phi$$

**Sequents** of !L\* written  $\Gamma \longrightarrow A$  meaning " $\Gamma$  reduces to  $A$ "

Sequents are built using **rules** of !L\* (next slide...)

# Rules of $\mathbf{!L}^*$

$$\frac{}{A \rightarrow A}$$

$$\frac{\Gamma \rightarrow A \quad \Delta_1, B, \Delta_2 \rightarrow C}{\Delta_1, B/A, \Gamma, \Delta_2 \rightarrow C} (/L)$$

$$\frac{\Gamma, A \rightarrow B}{\Gamma \rightarrow B/A} (/R)$$

$$\frac{\Gamma \rightarrow A \quad \Delta_1, B, \Delta_2 \rightarrow C}{\Delta_1, \Gamma, A \setminus B, \Delta_2 \rightarrow C} (\setminus L)$$

$$\frac{A, \Gamma \rightarrow B}{\Gamma \rightarrow A \setminus B} (\setminus R)$$

# Rules of $!L^*$

$$\frac{\Delta_1, !A, \Gamma, \Delta_2 \rightarrow C}{\Delta_1, \Gamma, !A, \Delta_2 \rightarrow C} \text{ (perm}_1\text{)}$$

$$\frac{\Delta_1, \Gamma, !A, \Delta_2 \rightarrow C}{\Delta_1, !A, \Gamma, \Delta_2 \rightarrow C} \text{ (perm}_2\text{)}$$

$$\frac{\Delta_1, !A, !A, \Delta_2 \rightarrow C}{\Delta_1, !A, \Delta_2 \rightarrow C} \text{ (contr)}$$

$$\frac{\Gamma_1, A, \Gamma_2 \rightarrow C}{\Gamma_1, !A, \Gamma_2 \rightarrow C} \text{ (!L)}$$

$$\frac{!A_1, \dots, !A_n \rightarrow B}{!A_1, \dots, !A_n \rightarrow !B} \text{ (!R)}$$

# Categorical Presentation of $!L^*$

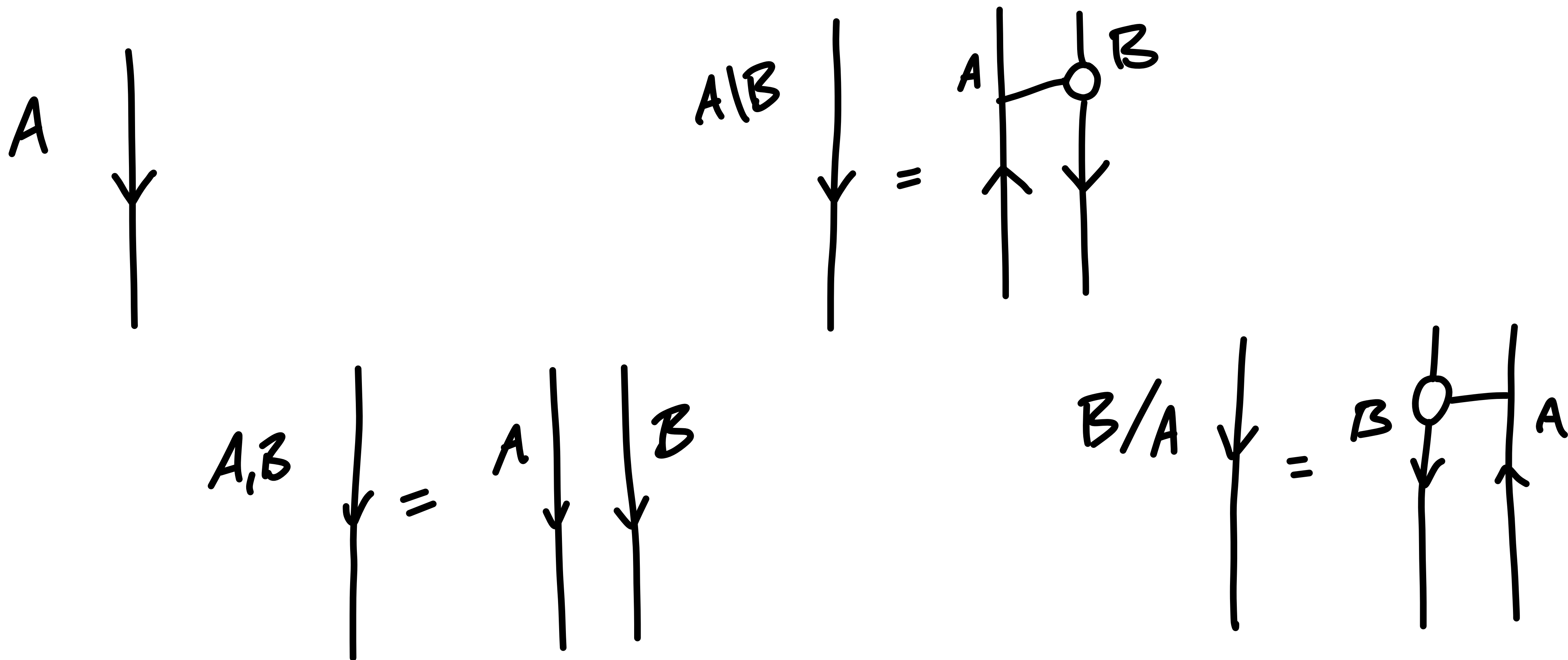
Define a category  $\mathcal{C}(!L^*)$  where  $!L^*$ -formulas are objects, and derivable sequents  $\Gamma \longrightarrow A$  are morphisms

$\mathcal{C}(!L^*)$  is a **monoidal biclosed category** with

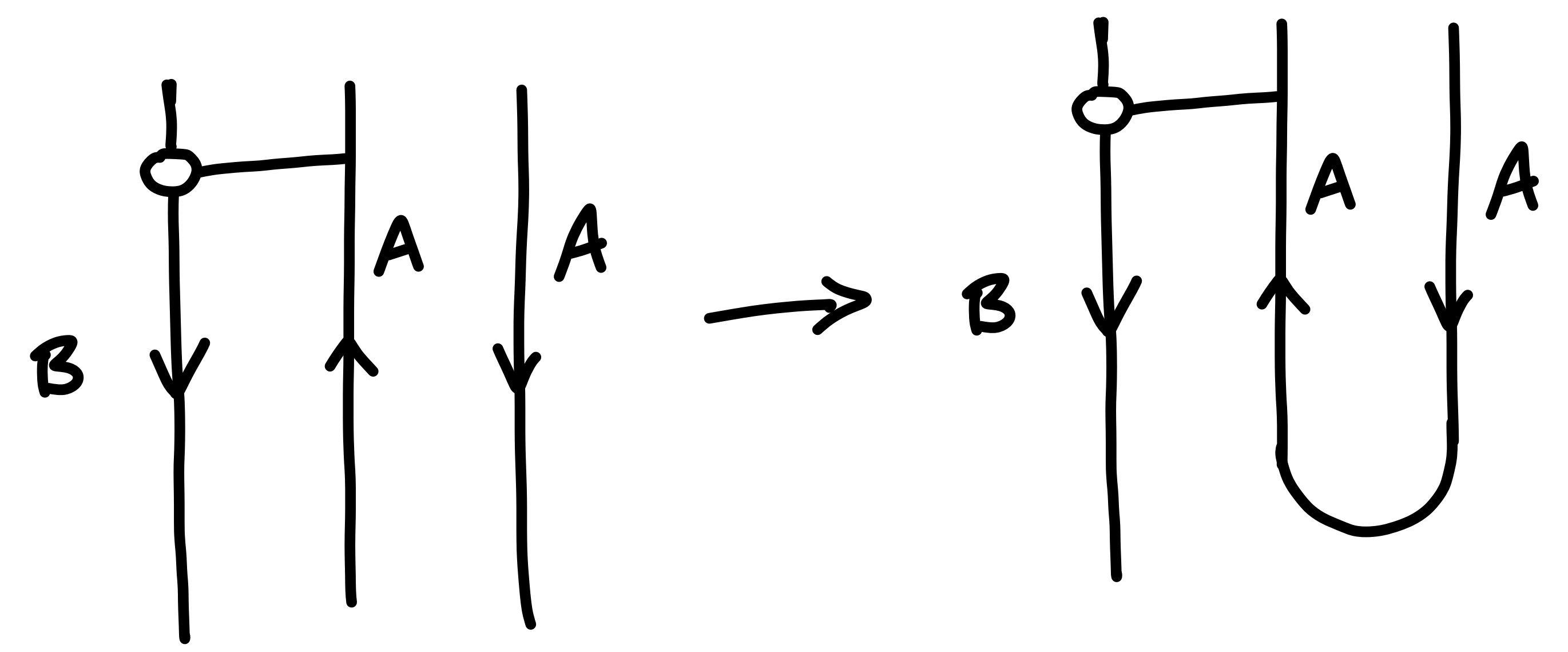
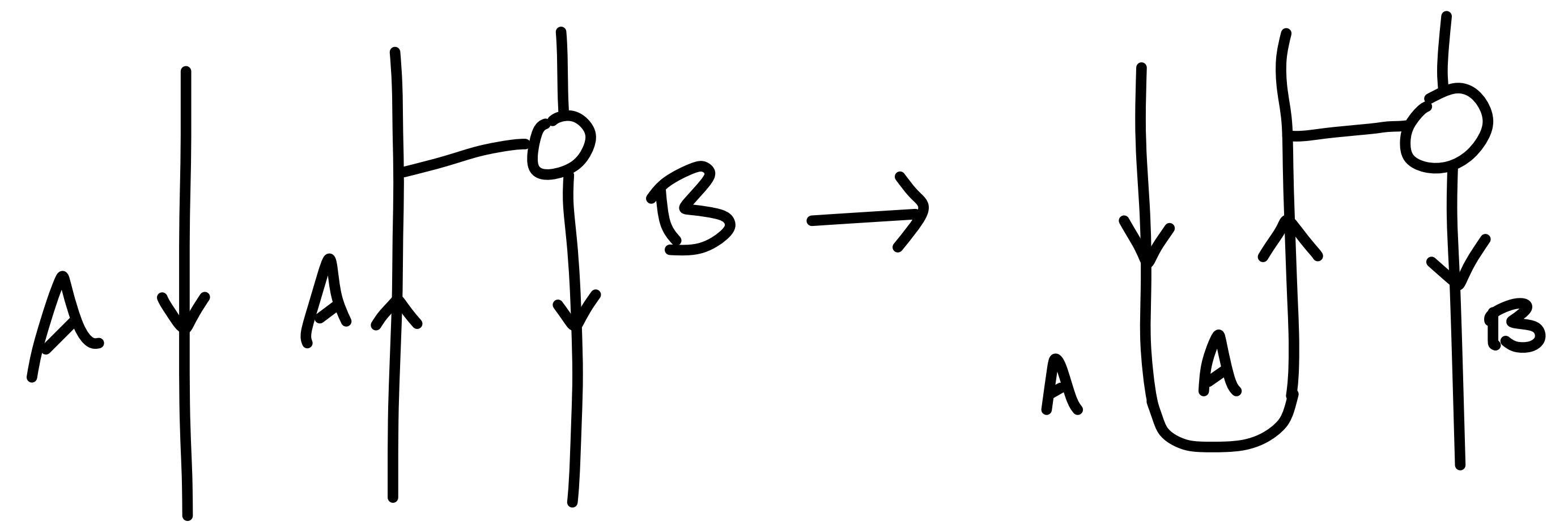
- a monoidal comonad,  $!$
- copying transformation  $\Delta : ! \rightarrow ! \otimes !$
- Permutation isomorphism  $\sigma : ! \otimes 1 \cong 1 \otimes !$



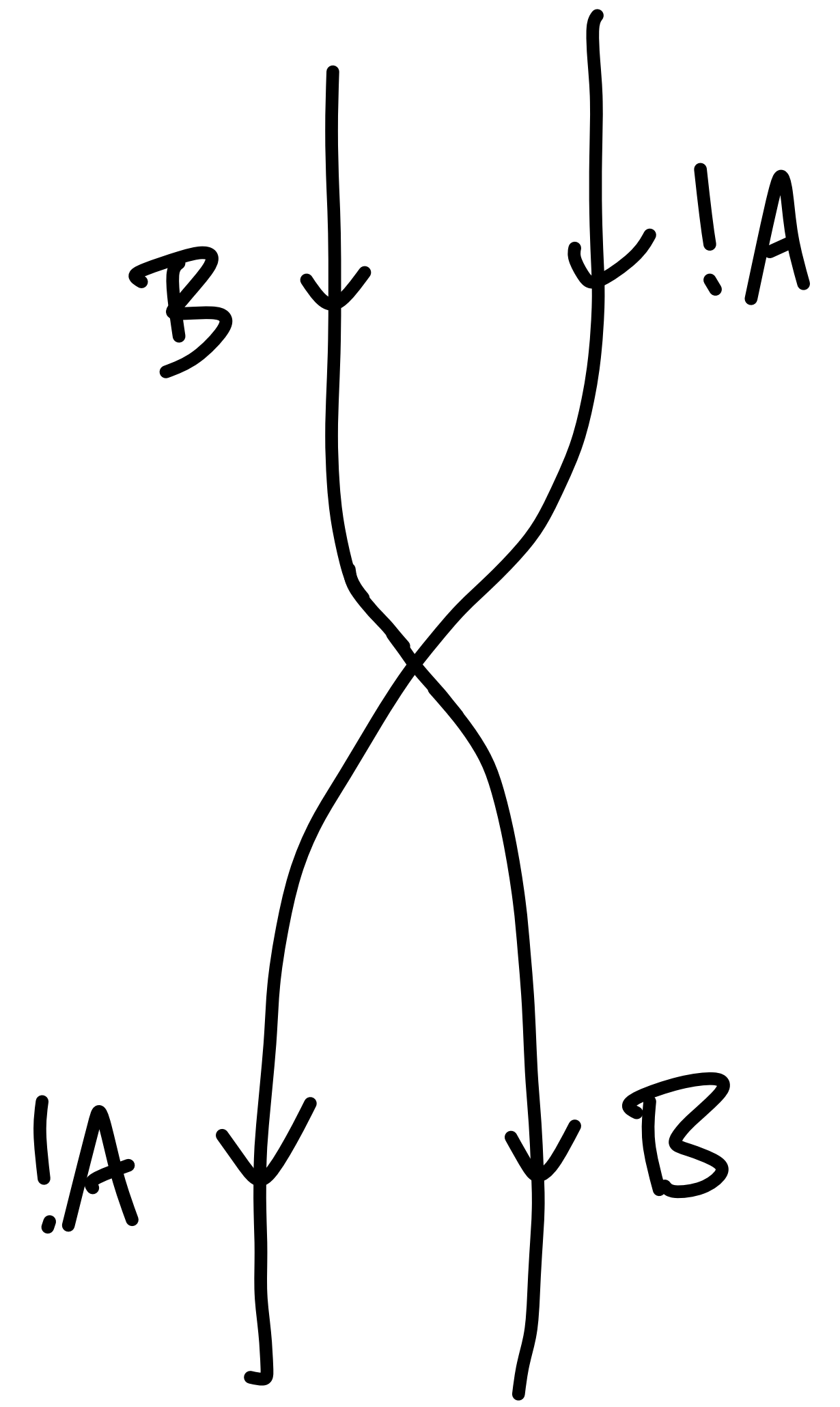
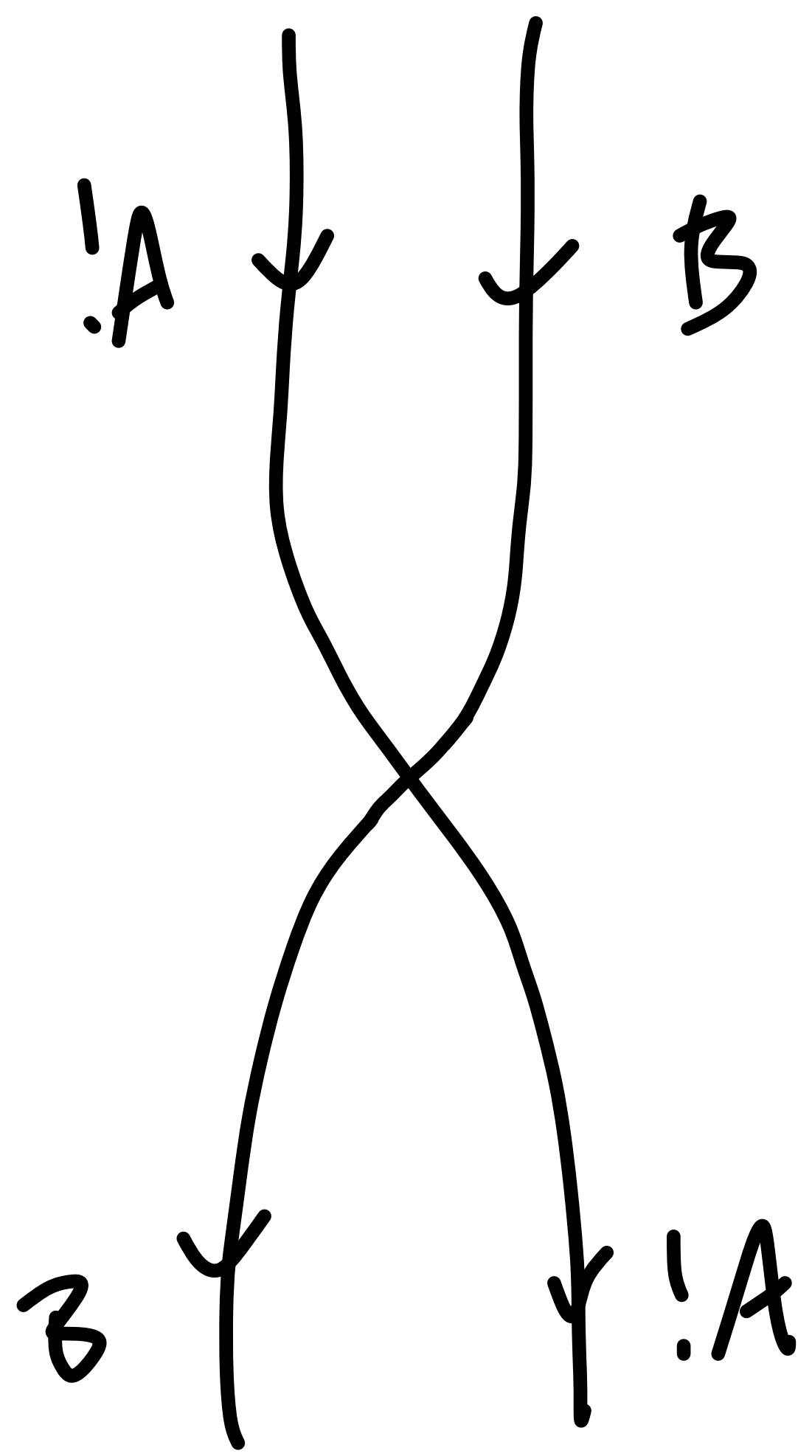
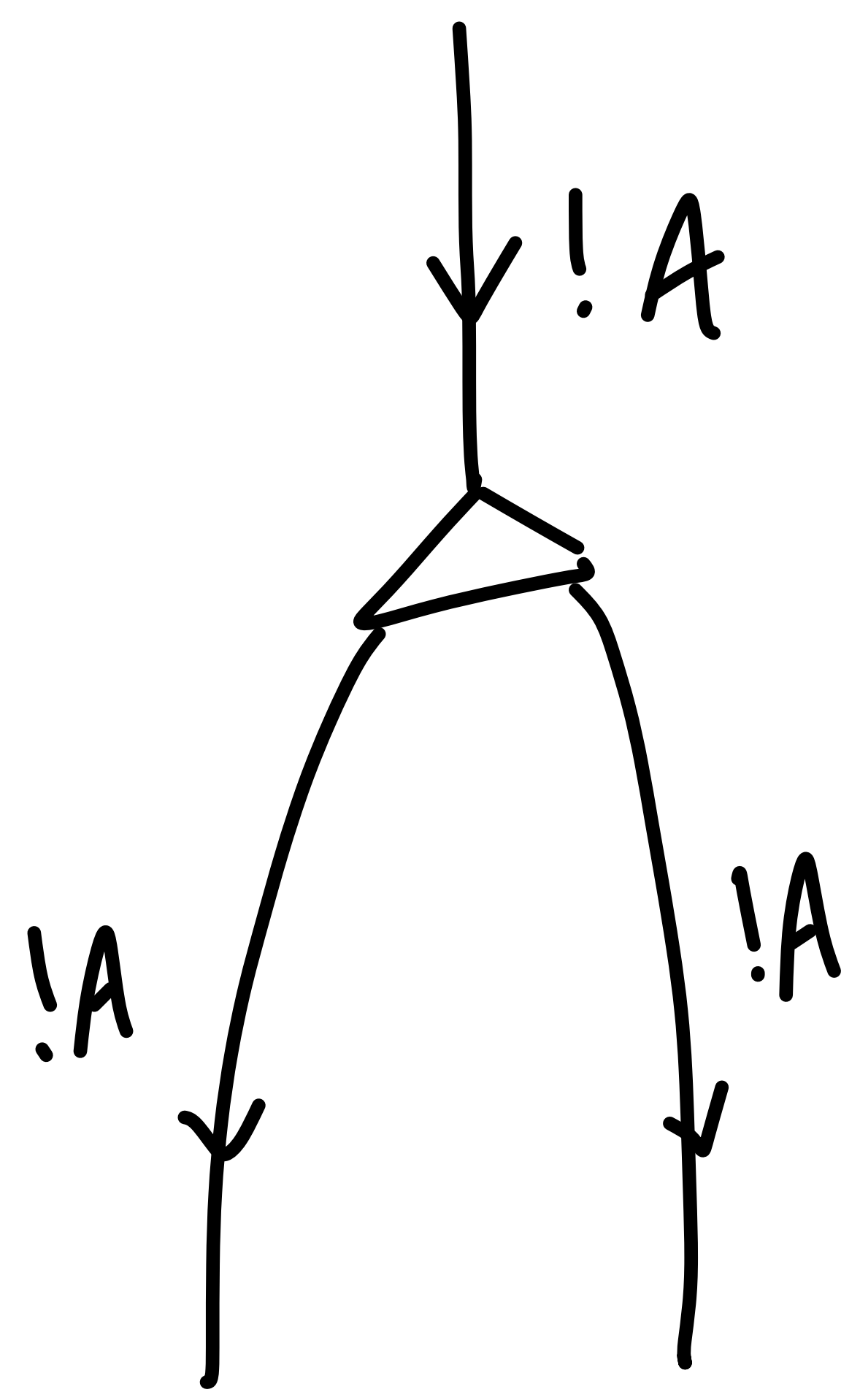
# !L\* Categorically



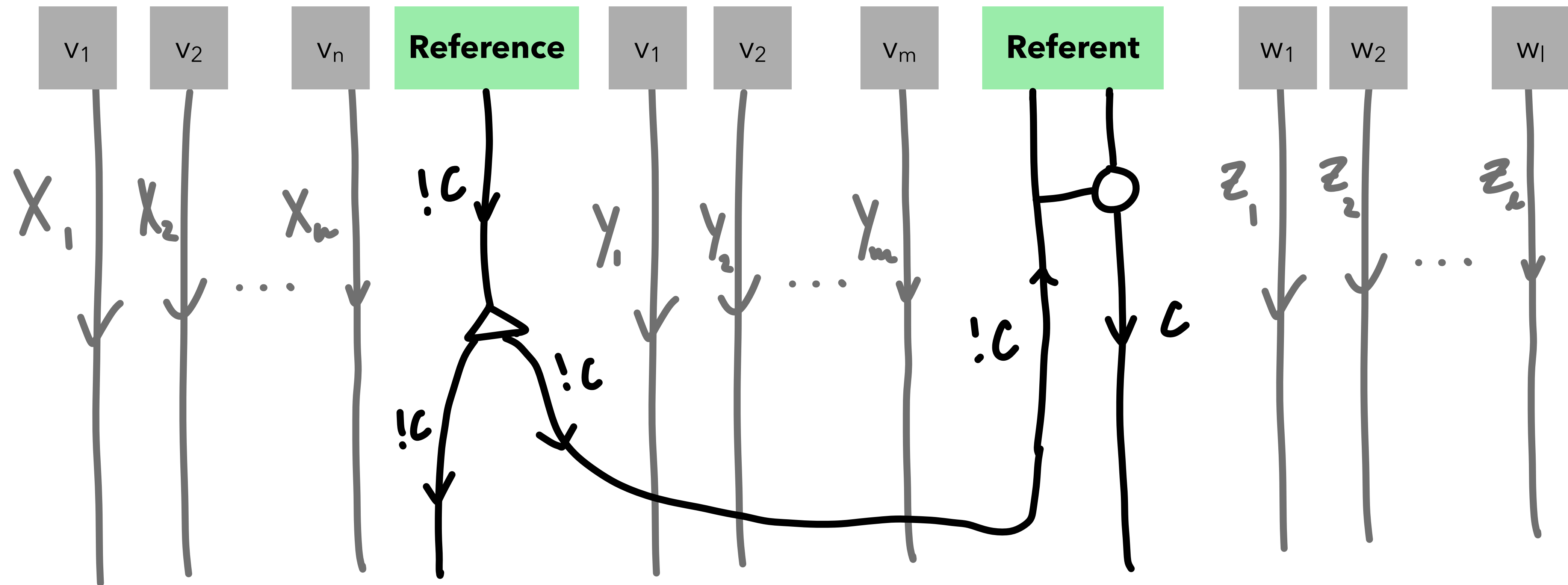
# !L\* Categorically



# !L\* Categorically



# Anaphora/Ellipsis Resolution in $\mathcal{C}(!L^*)$



Vector Space Semantics of

**$\mathbf{!L}^*$**

# Vector Space Semantics of !L\*

Recall vector space semantics (VSS) from ACT2020 [McP. et al, 2020], as strong monoidal biclosed functors

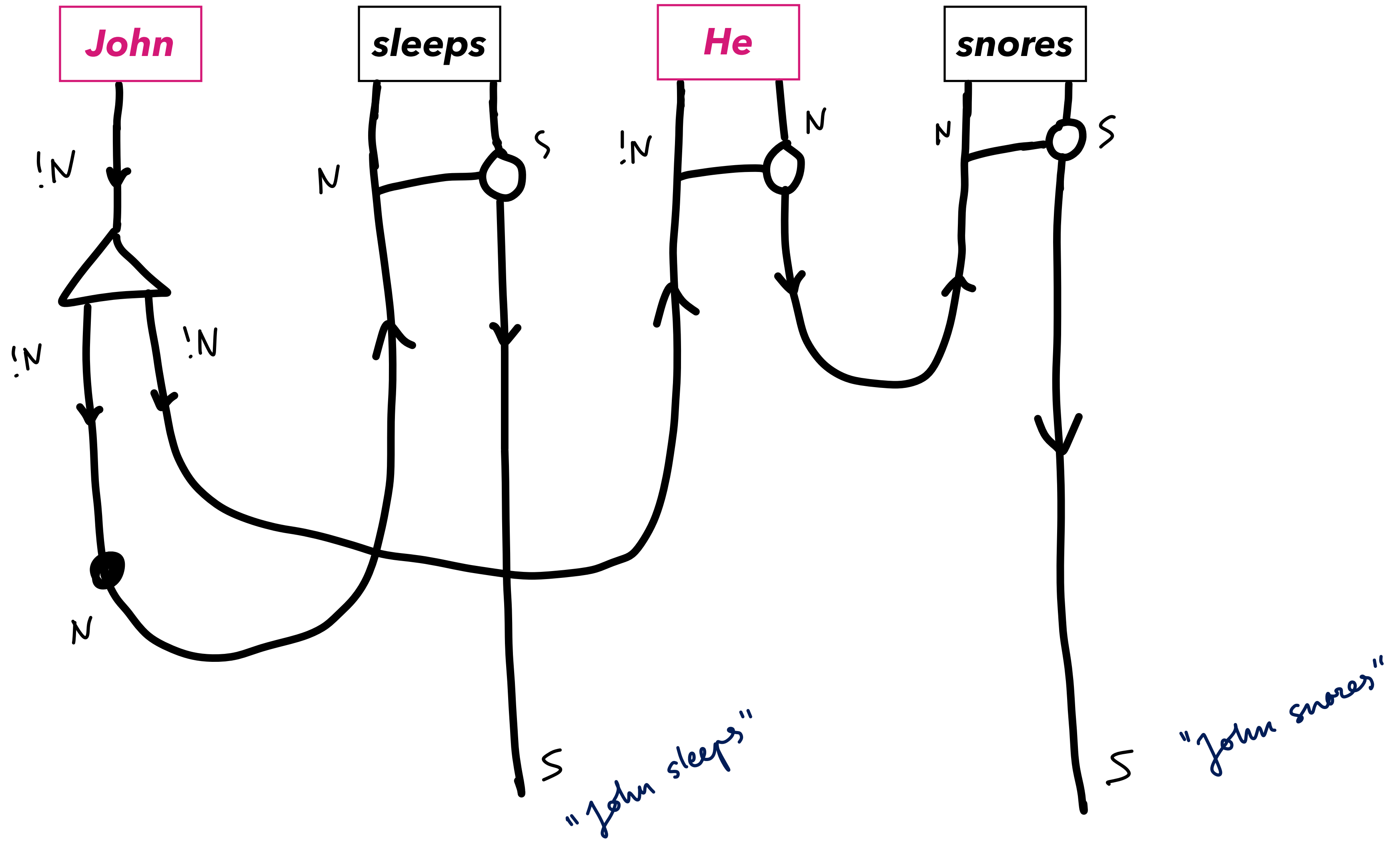
$$F : \mathcal{C}(!L^*) \rightarrow \mathbf{fdVect}$$

Thus, every diagram in  $\mathcal{C}(!L^*)$  allows us to produce vector representations of anaphora and ellipsis.

Mapping ! to fermionic Fock space or identity comonad.

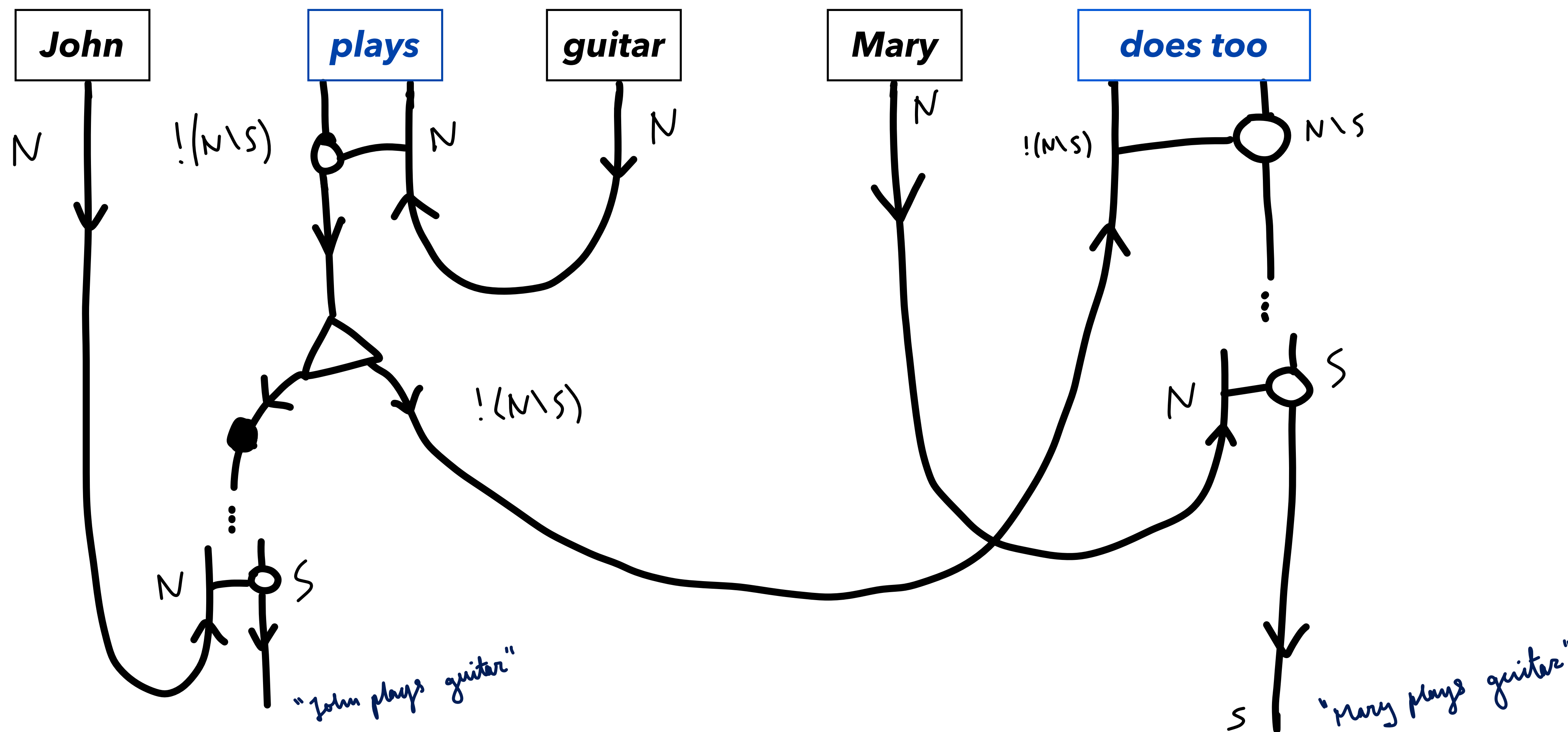
Examples

# Example: Anaphora

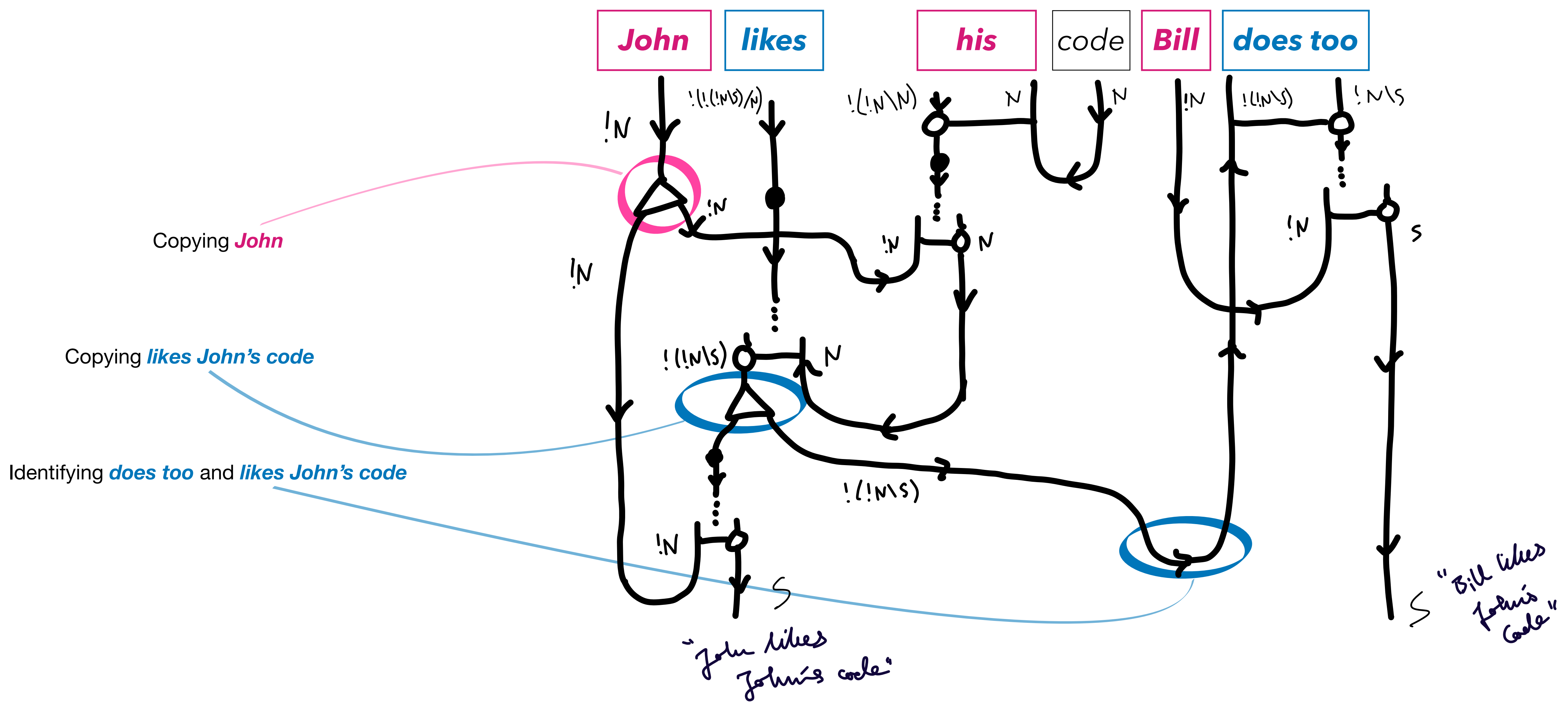




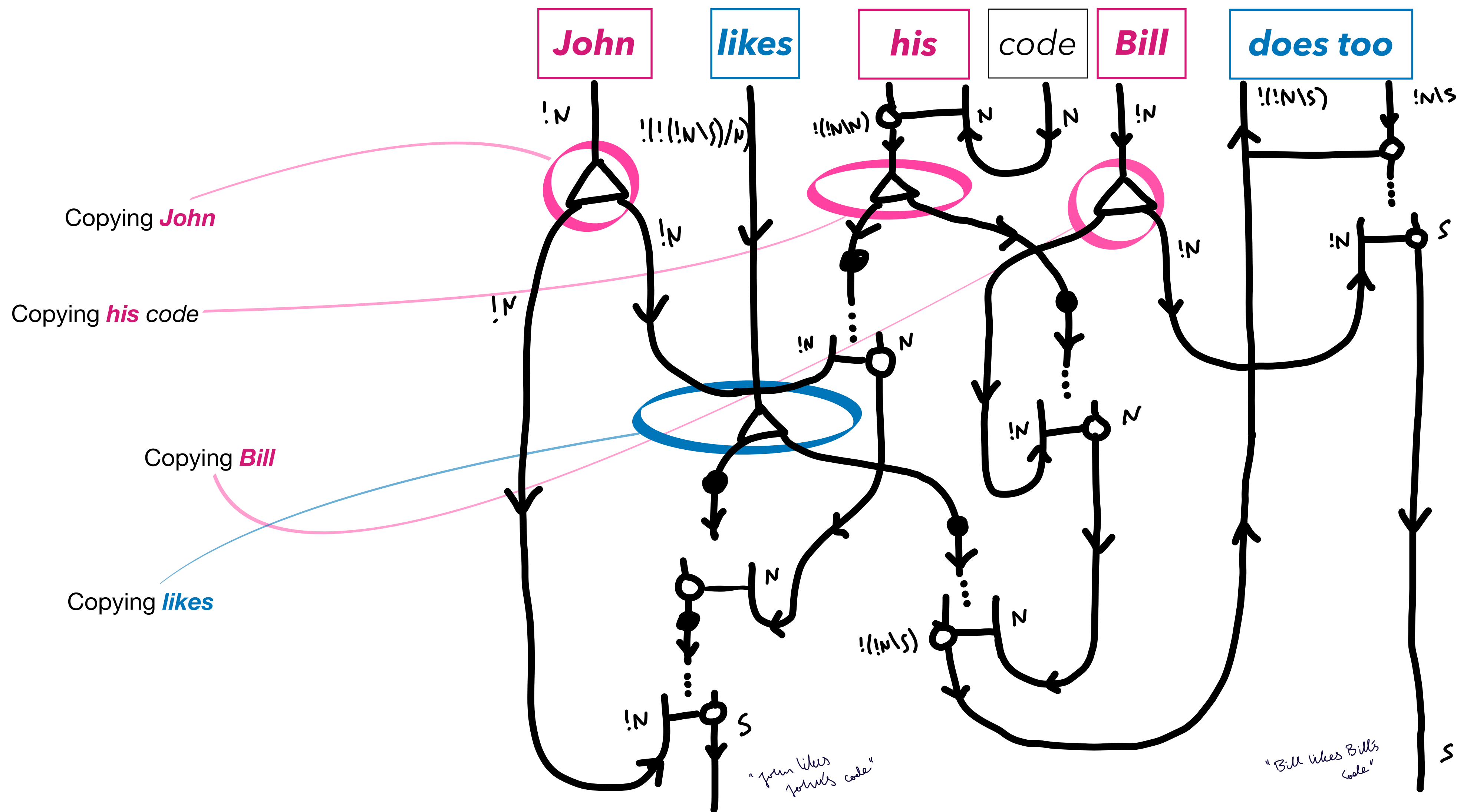
# Example: Ellipsis



# Example: Strict and Sloppy



# Example: Strict and Sloppy



# Empirical Validation

# The Task

Applied VSS to disambiguation task from [Wijnholds & Sadrzadeh 2019]

The goal is disambiguating elliptical sentences of the form

*"Man draws sword and artist does too"*

Where the ambiguous verb (*draw*) has two meanings: '*depict*' and '*pull*'

(General sentence format: "*S V's O and S\* does too*")

# The Results

Tested over 400 such sentences, and correlated with human annotations.

	$v \mapsto$	$v \otimes v$	$\mathbf{1} \otimes v$	$v \otimes \mathbf{1}$	$v \otimes \mathbf{k} + \mathbf{k} \otimes v$
		full	basis copy(a)	basis copy(b)	k-extension
<b>word2vec</b>		0.44	0.34	0.42	0.44
<b>fasttext</b>		0.43	0.36	0.41	0.43
baselines					
<b>verb only</b>		0.24			
<b>additive</b>		0.31			
<b>BERT phrase</b>		0.36			
inter-annotator agreement		0.58			

Spearman's  $\rho$  correlations, upper bound is inter-annotator agreement

# Outlook

VSS for decidable calculus with similar properties to **!L\***

Find complete models of **!L\***

Apply plausibility model to solve **Winograd Schema Challenge**

Study compatibility of our model of anaphora and ellipsis with **DisCoCirc**

# Many thanks!

# Any questions?

## References

- [Kanovich et al, 2016] Max Kanovich, Stepan Kuznetsov, and Andre Scedrov. *Undecidability of the Lambek calculus with a relevant modality*
- [Coecke et al, 2018] Bob Coecke, Giovanni de Felice, Dan Marsden, and Alexis Toumi. *Towards compositional distributional discourse analysis*
- [Jäger, 1998] Gerhard Jäger. *A multi-modal analysis of anaphora and ellipsis*
- [Jäger, 2006] Gerhard Jäger. *Anaphora and type logical grammar*
- [Baez & Stay, 2009] John Baez and Michael Stay. *Physics, topology, logic, and computation: A rosetta stone*
- [McP. et al, 2020] McPheat, Lachlan, Mehrnoosh Sadrzadeh, Hadi Wazni, and Gijs Wijnholds. *Categorical vector space semantics for lambek calculus with a relevant modality*