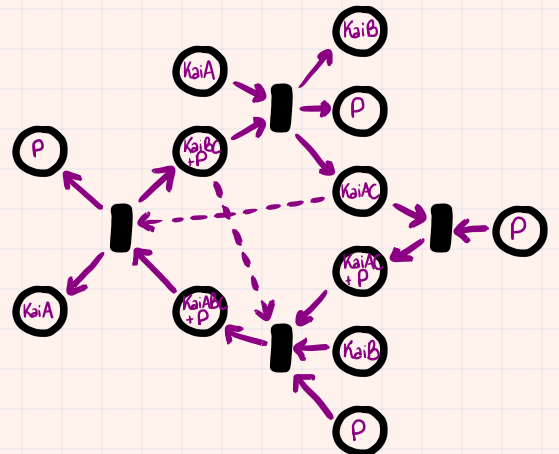


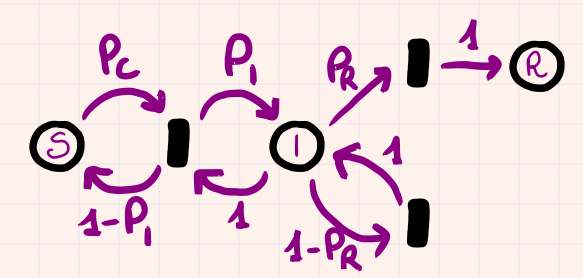
GOAL
 Composing Petri nets and closing them under linear logic connectives

KLEENE DIALECTICA
 $L = \{-1, 0, 1\}$



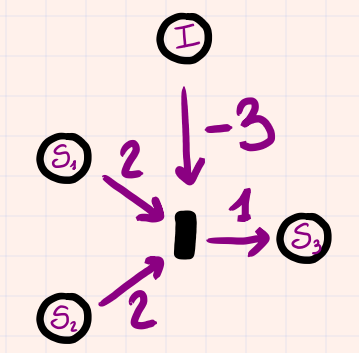
Chemical reaction network regulating the circadian clock of *Synechococcus Elongatus*

PROBABILISTIC DIALECTICA
 $L = [0, 1]$



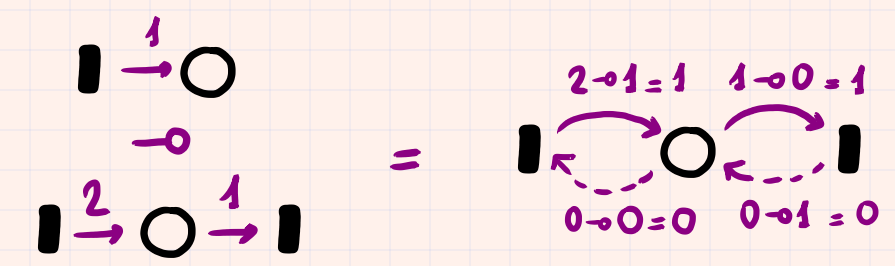
Petri net representing the SIR model for infectious diseases

INTEGERS DIALECTICA
 $L = \mathbb{Z}$

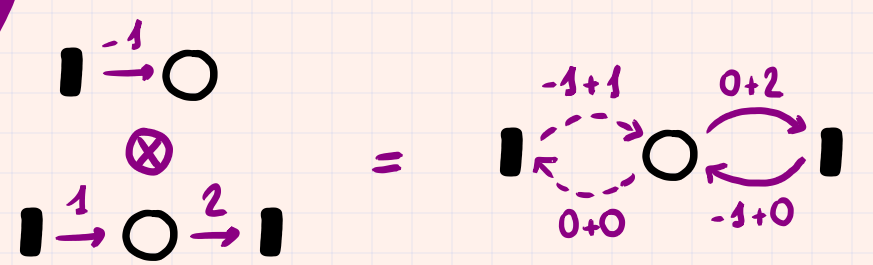


Chemical reaction network with inhibitor arc

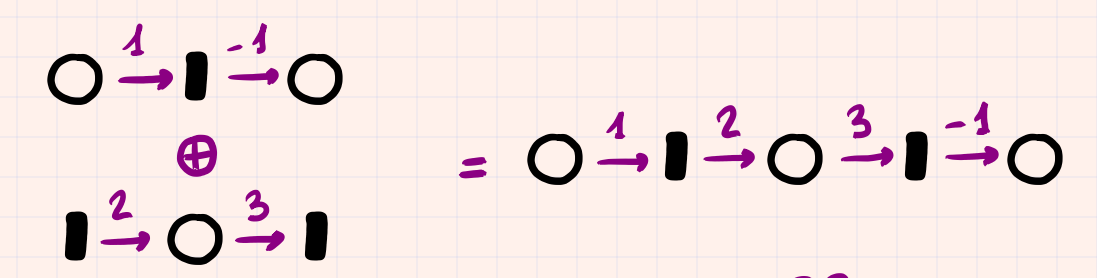
INTERNAL HOM



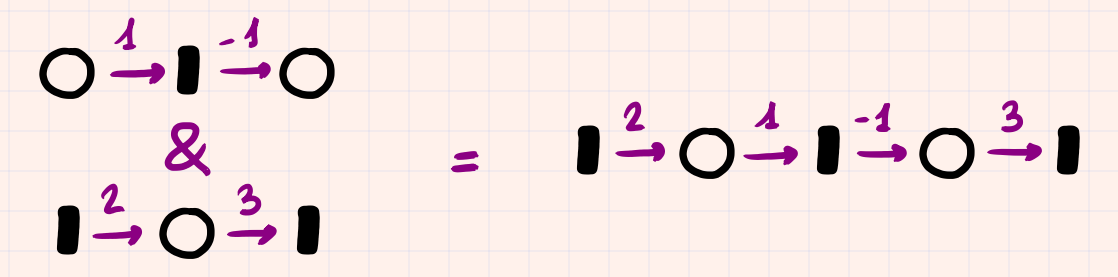
TENSOR



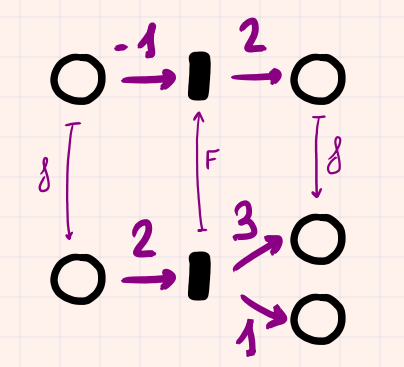
COPRODUCT



PRODUCT



MORPHISMS



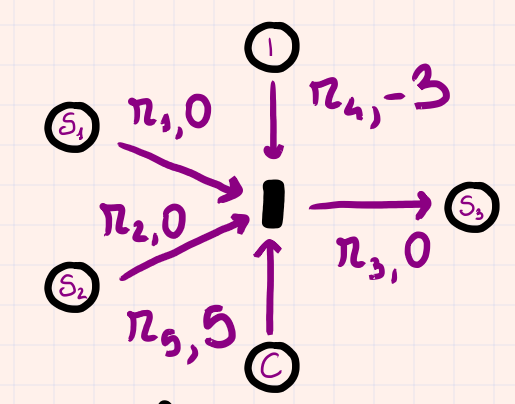
DIALECTICA PETRI NETS

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Valeria de Paiva
 Copos Institute

PRODUCT OF LINEALES
 $(L = \mathbb{R}^+ \times \mathbb{Z})$



Chemical reaction network specifying the rates, with inhibitor and catalyst

FUTURE WORK

- Notions of behaviour of Petri nets
- Differential linear logic Petri nets
- Implementations

MAIN REFERENCES

- E. Di Lavore, W. Leal, V. de Paiva
 Dialectica Petri nets
 arXiv preprint arXiv:2105.12801
- L. Brown, D. Gurr
 A categorical linear framework for Petri Nets
 LICS 1990
- V. de Paiva
 Categorical multirelations, linear logic and Petri nets
 Technical report 1991