# **Composing Conversational Negation**

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Negation in natural language does not follow Boolean logic and is therefore inherently difficult to model. In particular, it takes into account the broader understanding of what is being negated. In previous work, we proposed a framework for negation of words that accounts for 'worldly context'. In this paper, we extend that proposal now accounting for the compositional structure inherent in language, within the DisCoCirc framework. We compose the negations of single words to capture the negation of sentences. We also describe how to model the negation of words whose meanings evolve in the text.

## 1 Introduction

Negation in language is a complicated operation. Differing views of negation in language are a recurring subject of debate amongst linguists, epistemologists, and psychologists. One view maintains that negation in language conveys denial—rather than assertion—of a proposition (the matching bias account) [11]. Another view on negation in language asserts that it is the collective notion of plausible alternatives (the contrast classes account) [29]; this view traces its origins to as far back as Plato's view of not-X as otherness-than-X [24]. An explanation compatible with both views is that there can be different stages at which the negation is interpreted, for instance initially denying information, and later searching for alternatives [32]. This search for alternatives differentiates negation in conversation from simple logical negation.

Consider the sentences:

- $\mathbf{a})$  This is not a hamster; this is a guinea pig.
- $\boldsymbol{b})$  This is not a hamster; this is a planet.

Both sentences are grammatically and logically correct. Yet, most users of the English language will agree that there is something wrong with sentence b). Unlike sentence a), which seems reasonable without context, sentence b) must undergo a highly unusual 'contextual pressure' [22] to be believable—imagine a sci-fi flick about hamster-sized planets. The plausibility of different alternatives to a negated word naturally has a grading [29, 22]. In our previous work, we modelled operational conversational negation of a word, and experimentally validated that it positively correlates with human judgment of this grading [33].

In this paper, we will show how to perform the conversational negation of sentences using the conversational negation of words. This is analogous to how Coecke et. al. [8] developed the compositional categorical framework DisCoCat to obtain the meaning of a sentence from

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the meaning of its words. To extend from negation of words to negation of a sentence, a new challenge appears: ambiguity arises not only from the meaning of a negated word, but also from which word(s) in the sentence the negation is principally applied to. As an example, take the sentence "Johnny didn't travel to Manchester by train" [30]. Envision that Johnny is given emphasis—the natural conclusion is that someone else, instead of Johnny, went to Manchester by train. Correspondingly, if the emphasized word was Manchester or train, then the respective conclusions would be that Johnny went elsewhere or Johnny took another mode of transportation. Therefore, we note that the conversational negation of this sentence is arrived at from the conversational negation of its constituent words, i.e. constituent negation [14]. We also see that the grammatical structure is unaltered between the non-negated and negated forms of the sentence. This is in line with other attempts in deciphering the meaning of negation in natural language [16, pg. 104].

Another challenge we tackle in this paper is performing conversational negation of words or entities whose meaning is not fixed; instead, the meaning evolves as we obtain more information in the text. For instance, in the text "Waffle is a dog. Waffle is fluffy. Waffle likes to play fetch.", the meaning of the entity "Waffle" evolves with each sentence; i.e. we first learn that "Waffle" refers to a dog, then that it is fluffy, and finally, that it likes to play fetch. We want to perform the conversational negation, i.e. model alternatives, of the entity "Waffle" whose meaning updates with time. The negation of evolving entity has ambiguity similar to the negation of sentences: we do not know which information/property of the evolving entity the negation is actually applied to. Coecke [5] extended the DisCoCat framework to DisCoCirc that models evolving meanings by allowing us to compose sentences in the text. We will show that in the DisCoCirc formalism, the negation of evolving meanings is in fact the same thing as the negation of sentences. Hence, we will be able to use the same framework of conversational negation that we derived for sentences.

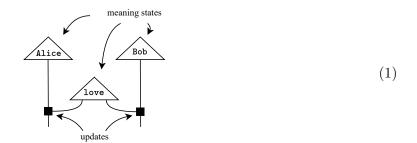
**Structure** In Section 2, we present the compositional DisCoCirc framework and the meaning category of positive operators and completely positive maps. In Section 3, we summarize the framework for conversational negation of words that we originally proposed in [33]. In Section 4, we go from conversational negation of words to conversational negation of sentences. In Section 5, we model the conversational negation of entities whose meaning evolve in the text. Finally, in Section 6, we discuss the implications of the ideas presented in this paper and outline directions for future work.

## 2 Compositional language meaning

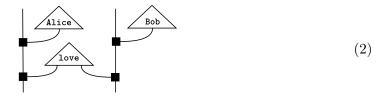
### 2.1 DisCoCirc

The DisCoCat framework [8] combines grammar (cf. categorial grammar [23]) and meanings (cf. vector embeddings in machine learning) within one compositional framework that enables one to compute the meaning of a sentence from the meanings of its words. To achieve this it exploits the common compact closed categorical structure, be it of vectors and linear maps, or of positive operators and completely positive maps [2, 31]. The DisCoCirc framework [5] improved on DisCoCat, (1) by enabling one to compose sentences into larger text, just as gates are composed in circuits; (2) by allowing meanings to evolve as that text evolves; (3) by specifying the sentence type as the tensored spaces of those entities that evolve. For our purposes, a

DisCoCirc diagram has two key ingredients: (1) meaning states; (2) updates [7]:



For example, here we have the noun meanings Alice and Bob, which initially are separate, being updated with the verb meaning love. Alternatively, we can have noun-wires with open input, which we then update to being Alice and Bob respectively, and then love:



### 2.2 The meaning category CPM(FHilb)

While the DisCoCirc framework allows for various encodings of meaning, for this paper, we work with the category CPM(**FHilb**) of positive operators and completely positive maps, as done in [26, 7, 31]. Positive operators are complex matrices, which are equal to their own conjugate transpose (Hermitian) and have non-negative eigenvalues (positive semidefinite). Completely positive maps are linear maps from positive operators to positive operators. The compact closed category CPM(**FHilb**) can be seen as an extension to the category of finite dimensional Hilbert spaces **FHilb**. It can be obtained from **FHilb** via the CPM construction originally introduced by Selinger [35]. In this construction, for any given unit vector  $|v\rangle$  of a finite dimensional Hilbert space, we can obtain a pure state positive operator by taking the outer product  $|v\rangle \langle v|$ . All other positive operators can be obtained as a linear combination of pure states.

In contrast to vectors, which have no inherent ordering structure [1], positive operators can be viewed as an extension of vector spaces that allow for encoding lexical entailment structure such as proposed in [2, 25]. We use these entailment measures to capture hyponomy; a word  $w_1$ is a hyponym of  $w_2$  if  $w_1$  is a type of  $w_2$ ; then,  $w_2$  is a hypernym of  $w_1$ . For example, dog is a hyponym of *animal*, and *animal* is a hypernym of dog. These entailment measures are often graded and take values between 0 (no entailment) and 1 (full entailment).

Additionally, positive operators can be used to encode ambiguity—words having multiple meanings—via mixing [31, 27], i.e. taking weighted sums over the different meanings. This ambiguity can later be disambiguated through additional meaning updates [7, 27]. We will use this property of positive operators to encode the ambiguity of negation in Section 4. For analysis and model performance for encoding and resolving ambiguity in compositional distributional semantics, we refer the reader to the extensive literature [3, 20, 17, 31, 7, 27].

### 3 Conversational negation of words

This section summarizes the operation for conversational negation of words as we proposed in [33]. As pointed out in Section 1 with the example of hamster-sized planets, negation in conversation not only denies information—a planet is indeed not a hamster—but additionally utilizes the listener's understanding of the world to weigh possible alternatives. This builds on the assumption that plausible alternatives to a word should appear in a similar context [30]. To present the framework for conversational negation, we will first present logical negation operations and an encoding of worldly knowledge.

### 3.1 Logical negation

Logical negation (denoted by  $\neg$ ) should fulfill certain properties such as the double negative  $(\neg(\neg p) = p)$  and the contrapositive  $(p \sqsubseteq q \Leftrightarrow \neg q \sqsubseteq \neg p)$ . Lewis [26] proposes the operation  $\neg X := \mathbb{I} - X$ , mapping in the case of projectors to the orthogonal subspace, as Widdows and Peters did for vectors [36]. In [33], we propose another logical negation based on generalizing the matrix inverse, that satisfies the contrapositive condition for the (graded) Löwner order [2].

In some sense, the result of the logical negation of a word is akin to a mixture of everything that is not that word. Despite this aligning with the set-theoretic notion of complement sets, this is unlike how humans perceive negation, as discussed in Section 1. Indeed, in our prior experiments, we found that alternatives elicited by both of the proposed logical negations have a negative correlation with human intuition [33]. We remedied this by amending logical negation with the worldly context of the negated word to achieve a positive correlation.

#### 3.2 Worldly context

Worldly context is another primary ingredient of conversational negation. It encodes the intuitive understanding of the world most readers possess. Worldly context captures the context a word tends to appear in. It thus encodes the space of possible alternatives to a word. This worldly context can be utilized to weigh the results of the logical negation.

To build worldly context for a given word, we proposed utilizing entailment hierarchies such as the human-curated WordNet [12] or the unsupervised Hearst patterns [13]. These hierarchies give us entailment relations such as displayed in Figure 1, where the directed edge represents

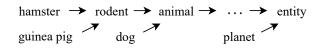


Figure 1: Example of hyponymy structure as can be found in entailment hierarchies

an entailment. We thus get the relations such as every hamster is a rodent, every rodent is an animal and all animals are entities. When negating hamster, we are most likely to talk about other rodents such as guinea pigs. We are less likely to talk about other animals such as dogs and yet less likely to talk about other entities such as planets.

Building on this idea, we proposed to construct the worldly context of a word by considering its hypernym paths and taking a weighted sum over all hypernyms. Hence, for a word w with

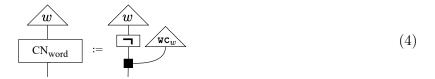
hypernyms  $h_1, \ldots, h_n$  ordered from closest to furthest, we define the worldly context  $wc_w$  as:

$$\llbracket \mathsf{wc}_w \rrbracket \coloneqq \sum_i p_i \llbracket h_i \rrbracket \tag{3}$$

where  $p_i \ge p_{i+1}$  for all *i*. We denote the positive operator encoding meaning of a word with double brackets.

#### **3.3** Framework for conversational negation of words

In [33], conversational negation of words, written as the operation  $CN_{word}$ , is defined as



This framework can be interpreted as the following three steps.

- 1. Calculate the logical negation  $\neg(\llbracket w \rrbracket)$ .
- 2. Compute the worldly context  $\llbracket wc_w \rrbracket$ .
- 3. Update the meaning of  $\neg(\llbracket w \rrbracket)$  by composing with  $\llbracket wc_w \rrbracket$  to obtain  $\neg(\llbracket w \rrbracket) = \llbracket wc_w \rrbracket$ .

This framework is flexible to the choice of logical negation, worldly context generation and composition operation  $\Psi$ . In [33], we studied and compared the performance of various choices of operations. While we only experimentally validated our negation operation on nouns, the same operation is applicable to adjectives and verbs.

### 4 Conversational negation of strings of words

In the distributional approach to natural language processing, the commonly used model is the bag-of-words that disregards any grammar and treats words as a structureless bag. Coecke et. al. [8] proposed the DisCoCat model that combines grammar and distributional word meanings in the categorical framework that allows us to compose the meaning of words to get the meaning of a sentence. In this section, we do the same for conversational negation by introducing the conversational negation of sentences that is calculated using the conversational negation of words.

#### 4.1 Modelling conversational negation

As pointed out by Oaksford and Stenning [30], the negation of more complex structures consisting of multiple words may be interpreted as the negation of a subset of the constituents. For example, a sentence such as "Bob did not drive to Oxford by car" could be interpreted as

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a) Bob did not drive to Oxford by car - Alice did
b) Bob did not drive to Oxford by car - He carpooled
c) Bob did not drive to Oxford by car - He drove to London
d) Bob did not drive to Oxford by car - He drove a van
e) Bob did not drive to Oxford by car - Alice carpooled to Oxford
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where the underline indicates which words are being negated. The last example is one of many possible cases, which negate multiple constituents. While some of these alternatives might immediately seem more plausible to the reader, the correct choice is inherently dependent on the context.

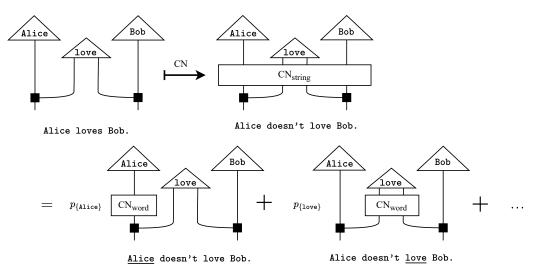
Based on this interpretation that a negation of multiple words is negating a subset of the constituents, we extend our conversational negation framework to a string of words by utilizing conversational negation of individual words (see Section 3). As the correct interpretation of which words to negate may not usually be obvious, we create a mixture of all possible interpretations. Therefore, the negation of a string of n words  $w_1 \otimes w_2 \otimes ... \otimes w_n$  is a weighted mixture of all the interpretations where only one word is negated, all the interpretations where two words are negated, and so on. We have

where in the overall mixture representing the negation, each interpretation has some weight. Formally, for  $S = \{w_1, ..., w_n\}$  and non-empty  $S' \subseteq S$  which we call the **negation set**, we get

To apply this negation to sentences, we adopt the view that sentences are as processes updating wires as presented in [5]. These processes are built from a combination of meaning states, interacting via updates. We propose negation of a sentence to be viewed as the same set of meaning states, first updated by the conversational negation of the words before updating the wires as if the negation was absent. This is in line with [16, pg. 104], who also grammatically treat sentences with negation as if they were not negated. Hence, we represent the conversational negation as a function called CN that maps the circuit of a sentence to a circuit where the sentence is pre-composed with  $CN_{string}$ .

For example, applying CN to the sentence "Alice loves Bob", we get the circuit for the

sentence "Alice doesn't love Bob":



Here, we sum over all possible non-empty subsets of {Alice, love, Bob}, each of which is weighted by the appropriate scalar.

#### 4.2 Deriving the weights

The main challenge for the conversational negation of a string is deriving the weights for the different interpretations of the negation. The choice of correct interpretation, and therefore the weights, is dependent on context. Context can be derived from many sources, such as the person who is speaking and their intentions. In spoken language, intonation could clarify the intent of the speaker by them emphasizing the words which are meant to be negated.

Another source of context is the grammatical structure of the negated sentence itself. Given the earlier example "Bob did not drive to Oxford by car," which specifically mentions the mode of transport, intuitively the focus of negation is on this detail. If the speaker solely wanted to negate Bob's destination, the sentence "Bob did not drive to Oxford" would be sufficient, not requiring any additional detail. The other example, "Alice doesn't love Bob," is more ambiguous as the grammatical structure does not indicate the target of the negation.

Context from surrounding sentences can further determine the sensibility of interpretations to a negation. Consecutive sentences should have meanings consistent with each other and with the reader's general understanding of the world. The statement Bob did not drive to Oxford by car - He drove to London is reasonable with the knowledge that Oxford and London are cities an hour's drive apart. Likewise, Bob did not drive to Oxford by car - He drove a van makes sense because car and van are similar vehicles.

Overall, no single source of context is sufficient. A combination of all contextual information worldly, textual, physical, grammatical, intonation, etc.—is required to determine the correct interpretation.

While the different weights for the negations sets are context dependent, some general observations can be made. Larger negation sets should tend to have smaller weights. The psychology motivation is that humans are less able to focus on a larger number of details due to "limited information processing capacity" [10, 30]. Considering the previous example, one would require

a lot of context for the interpretation of "Alice doesn't love Bob" to sensibly imply "Claire likes Dave". Secondly, one can observe that the weight of a negation set should depend on the likelihood of its individual elements to be the target of the negation. If Alice being the target of the negation is unlikely, for instance if the entire text is about Alice, then the negation set of both Alice and love is also unlikely.

#### 4.2.1 Determining weights using entailment

As mentioned earlier, one possible source of context can be the surrounding text. In a text which solely talks about Alice and Bob, the sentence "Alice doesn't love Bob" probably intends to negate the word love, therefore asserting that Alice feels emotions other than love for Bob. Building on this intuition, we propose to use entailment measures to derive the weights for the different interpretations of a negation. If the given interpretation of the negation entails the surrounding sentences to a high degree, then the interpretation is consistent with the surrounding text and hence, it is likely to be the intended meaning of the sentence.

We compare each possible interpretation of the negation with the surrounding sentences, where sentences closer in the text have more influence towards the final weighting than sentences that are further away. Let us consider the following, simplified scenario of a negation, followed immediately by the clarification with both sentences of the same grammatical structure:

> This is not red wine This is white wine

Here, we colour code the sentences for visual clarity, where the negated sentence is red. We want to determine the respective weights  $p_{\{\text{red}\}}$ ,  $p_{\{\text{wine}\}}$  and  $p_{\{\text{red}, \text{wine}\}}$  of the negation sets  $\{\text{red}\}$ ,  $\{\text{wine}\}$  and  $\{\text{red}, \text{wine}\}^1$ . As a human reader, the sentence following the negation clarifies that wine is not negated. Thus, the intended negation set is  $\{\text{red}\}$ .

To mathematically come to the same conclusion, we calculate the entailment between each interpretation of the negation and the follow-up sentence, i.e. how much each negation set of **not** red wine entails white wine. We compare the two sentences word by word (or more precisely, treating adjectives and nouns individually) and then take the product of the results. We consider

- not <u>red</u> wine ⊆ white wine We first calculate the entailment of CN<sub>word</sub>(red) with white which is medium as something that is not red could have many other colors, including white. The entailment of wine with wine is maximal as a wine is indeed a wine. Therefore the overall score of this interpretation is high. Overall entailment: high
- not red wine ⊆ white wine This interpretation has medium entailment between CN<sub>word</sub>(wine) and wine due to the fact that in distributional semantics, a word and its conversational negation appear in similar contexts [28, 30]. Yet the entailment between red and white is low since something being red does not entail that it is white. Overall entailment: low
- not red wine  $\sqsubseteq$  white wine This interpretation has a medium entailment between  $CN_{word}(red)$  and white and a medium entailment between  $CN_{word}(wine)$  and wine. Overall entailment: medium

 $<sup>^{1}</sup>$ For the sake of simplicity, we ignore the fact that "This" could also be the target of the negation, as in "This is not red wine. That is!".

Comparing the three interpretations, the first option has the highest score, matching our intuition of being the correct choice.

While this entailment method, presented here, relies on the sentences having an identical grammatical structure to compare the sentences word by word, we can also directly compare entailment between two sentences. This requires composition operations and entailment measures which interact well to preserve word level entailment on the sentence level. This is still a field of active research, with some promising results presented in [19, 18, 34, 9].

#### 5 Conversational negation of evolving meanings

Coecke [5] enhanced the DisCoCat framework to create DisCoCirc, which allows the meaning of sentences to be composed to obtain the meaning of text. In this section, we show that our conversational negation framework can be easily extended from sentences to conversational negation of text and evolving meanings.

#### 5.1Negating evolving meanings

One of the key features of DisCoCirc is that it allows the meaning of entities to evolve as text evolves. The meanings are updated when the wires of the entities are composed with some meaning states. In DisCoCirc, texts that have the same meaning result in the same updates on the wires, even if they contain different sentences. For example, a text containing the following two sentences

> Bob is a scientist. Bob is an alcoholic.

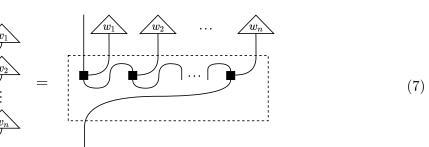
results in the same circuit as the text containing the single sentence:

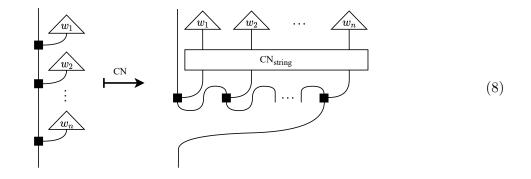
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Bob who is a scientist is an alcoholic.
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This motivates us to think of all the meaning updates to a wire as a single large sentence. If we have a sequence of updates to a wire, we can morph the wire using the snake equation. We thereby derive a single meaning update process that updates the wire with a sequence of word meanings. Hence, for a wire whose meaning evolves through updates by words  $w_1, \dots, w_n$ , we have

(7)

Now, to perform conversational negation, we can simply apply the CN function (see Section 4) that maps the circuit of a sentence to a circuit where the sentence is pre-composed with  $CN_{string}$ .





Thus, the conversational negation of a dynamic evolving entity becomes:

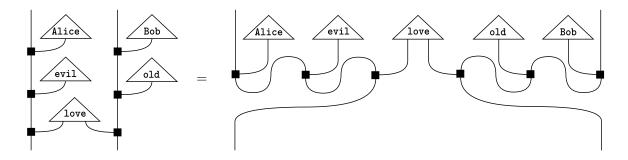
This idea can also be applied to text with multiple, interacting actors. Consider the text:

### Alice is evil. Bob is old. Alice loves Bob.

Alternatively, we can write this as a single sentence:

Alice who is evil loves Bob who is old.

The circuit for the text looks like the following.

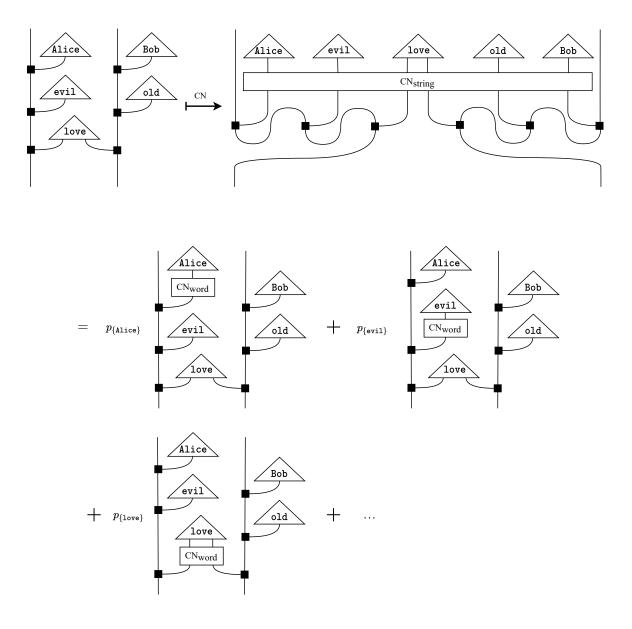


Suppose we want to find the conversational negation of the actor named Alice in the above text, i.e. we want to know that if someone is not Alice, who else could they be. Similar to the case of conversational negation of sentences, we have various possibilities based on the meaning updates that have been performed on the wire corresponding to Alice. Any subset of the words that have contributed to the meaning update of Alice – either directly or via meaning updates to entangled actors – could be negated. For example, "not Alice" could be

- a) <u>Claire</u> who is evil and loves old Bob
- b) Alice (different person but same name) who is <u>virtuous</u> and <u>hates</u> old Bob
- $c) \ \underline{\texttt{Dave}}$  who is evil and loves young Bob
- $d) \ \underline{\texttt{Claire}}$  who is  $\underline{\texttt{virtuous}}$  and  $\underline{\texttt{hates}}$  old Daisy

If we again think of the text as a single large sentence, we can simply apply the CN function

from Section 4.



If we want to perform the conversational negation of the actor Bob instead of Alice, we will again get the same resulting circuit after applying the CN function. The difference to the conversational negation of Alice is that we will have different weights for the negation sets. For example, the weight of the negation set {Bob, old} is likely low for the negation of Alice – someone who is not Alice is intuitively unlikely to be someone who is called Alice and is evil but loves a person with different attributes than Bob. In contrast, the weight of the same negation set could be reasonably high for the negation of Bob – someone who is not Bob could have a different name and age but still be the lover of Alice. Therefore, while having the same diagrammatic representation, the negation of the actor Alice can give a fundamentally different result than the negation of Bob through the weights which were chosen for the negation sets.

#### 5.2 Example: finding alternatives

Consider the following text where the meaning of the words evolves as the text evolves:

Alice is a human.	Alice is an archaeologist.
Bob is a human.	Bob is a biologist.
Claire is a human.	Claire is a pianist.
Daisy is a dog.	Daisy is a pet.

Suppose we want to perform the conversational negation of the actor Alice and evaluate how much it entails the other actors: Bob, Claire and Daisy. Based on the given text, it is reasonable to expect that someone who is not Alice (a human archaeologist) is more likely to be Bob (a human biologist) than Claire (a human pianist). In fact, someone who is not Alice is still more likely to be Claire (a human pianist) than Daisy (a pet dog). Now we will analyze if the conversational negation presented in Section 5.1 reflects this intuition.

When we apply the conversational negation to the actor Alice, we get a mixture containing all possible negation sets along with their weights. These negation sets are nonempty subsets of {Alice, human, archaeologist}. The weights of the negation sets must be determined using all context as discussed in Section 4.2. However, to explore the maximum entailment that can be achieved from the negation of the actor Alice to each of the remaining actors, we only consider the most appropriate negation sets of "not Alice" for each actor.

• Bob - Since Bob is a human biologist, the best negation set of "not Alice" for Bob is {Alice, archaeologist}. The table below shows the entailment between this negation set of "not Alice" and the actor Bob. From the table, it is clear that "not Alice" highly entails Bob.

"not Alice"	Bob	Entailment
$CN_{word}(\texttt{Alice})$	Bob	medium
human	human	1 (max)
$\mathrm{CN}_{\mathrm{word}}(\texttt{archaeologist})$	biologist	high

• Claire - Similar to Bob, the best negation set for Claire is {Alice, archaeologist}. As shown in table below, "not Alice" moderately entails Claire.

"not Alice"	Claire	Entailment
$\mathrm{CN}_{\mathrm{word}}(\texttt{Alice})$	Claire	medium
human	human	1 (max)
$\mathrm{CN}_{\mathrm{word}}(\texttt{archaeologist})$	pianist	medium

• Daisy - For Daisy the pet dog, the best negation set of "not Alice" is {Alice, human, archaeologist}. From the table below, "not Alice" only slightly entails Daisy.

"not Alice"	Daisy	Entailment
$\mathrm{CN}_{\mathrm{word}}(\texttt{Alice})$	Daisy	medium
$\mathrm{CN}_{\mathrm{word}}(\mathtt{human})$	dog	medium
$\mathrm{CN}_{\mathrm{word}}(\texttt{archaeologist})$	pet	low

Therefore, in our proposed framework, someone who is not Alice has the highest chance to be (from most to least likely): Bob, Claire and Daisy, which indeed lines up with the human intuition. Yet the final result of the negation depends on the weights of the negation sets, which are determined by the context. Hence, if for some reason, the negation set {Alice, human, archaeologist} has been determined to be the correct interpretation, then "not Alice" might be more closely related to Daisy than Claire after all.

### 6 Discussion and future work

The framework to model conversational negation, proposed in this paper, utilises a new mechanism not currently present in DisCoCirc: the external derivation of the weights required for the mixture of different interpretations of a negation. This is motivated by the observation that disambiguation in language relies on an understanding of the world not necessarily present in the text. In the case of the conversational negation of words, this understanding is captured in a single meaning state derived from existing lexical entailment hierarchies, which we called the worldly context (Section 3.2). In the case of conversational negation of sentences and evolving meanings, the weights allow for this understanding to be integrated into the circuit. While Section 4.2.1 provides an intuition of how the surrounding text can partially inform the correct choice of weights, they should also take into consideration other contexts such as worldly knowledge, intonation, or the environment of the speaker. One goal for future work is to explore these sources of context and find methods to incorporate that information into the weights. Apart from using the weights to inject context, we would like to explore embedding the sources of context directly within the representation of word meanings; for instance, by building upon the work on conceptual space models of cognition in compositional semantics [4].

The ideas presented in this paper are built on the intuitions gathered from psychology papers and the experiments performed for the conversational negation of words in [33]. To empirically validate the framework for conversational negation of sentences and of evolving meaning, experiments should be devised. With the basic intuition for deriving the weights from surrounding sentences being solely presented for grammatically identical sentences, further work needs to be done to generalize this process.

In this paper, we modelled the conversational negation of a sentence as the conversational negation of its constituent words. We focused on single word constituents, 1) for the purpose of clarity, and 2) because in our prior work we proposed and experimentally validated a framework for conversationally negating a single word [33]. However, our model does not forbid constituents made of multiple words. For instance, in the following example the negated constituent is "the key to the garage":

#### This is not the key to the garage. - This is a toy.

If we were to broaden the scope of our conversational negation to generate plausible alternatives

to a sentence with a different grammatical structure, we would require a mechanism for parsing and negating constituents made of multiple words. In this view, it could then be possible to model the negation of non-conjunctive composition of concepts such as the compositional explanation of the "pet fish" phenomenon by Coecke and Lewis [6].

Although we have devised a treatment for modelling the conversational negation of a sentence as the conversational negations of its constituent words then composed together grammatically, there are other forms of negation in natural language. Since Klima [21] and Jackendoff [15], most linguists have treated the form of negation we model—constituent negation—as distinct from sentential negation [14]. Consider the sentence I did not walk my dog. Constituent negation invokes the collective mixture of possible alternative interpretations: that someone else walked the dog, I cuddled the dog, it was my friend's dog, etc. Instead, it may be that we simply want to negate the sentence as a whole—it is untrue that I walked my dog. Without experiment, it is unclear to us whether logical negation of the sentence meaning alone suffices to model sentential negation.

Another related challenge is to formalize a mathematical model of the logic underlying conversational NOT, AND, and OR. This requires investigating the extent to which boolean logic holds in a setting known to not follow boolean logic. A long-term goal would be to extend the conversational negation process to a *conversational logic* process, compatible with compositional distributional semantics, particularly its properties with regards to entailment.

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