

## 2004 Paper 13 Question 12

### Complexity Theory

- (a) Define a one-way function. [4 marks]
- (b) Explain why the existence of one-way functions would imply that  $P \neq NP$ . [7 marks]
- (c) Recall that **Reach** is the problem of deciding, given a graph  $G$  a source vertex  $s$  and a target vertex  $t$ , whether  $G$  contains a path from  $s$  to  $t$ ; and **Sat** is the problem of deciding whether a given Boolean formula is satisfiable.

For each of the following statements, state whether it is true or false and justify your answer.

- (i) If **Reach** is NP-complete then  $P=NP$ . [3 marks]
- (ii) If **Reach** is NP-complete then  $NP \neq PSPACE$ . [3 marks]
- (iii) If **Sat** is PSPACE-complete then  $NP=PSPACE$ . [3 marks]