## 2003 Paper 11 Question 7

## Continuous Mathematics

(a) State the definition of the Fourier Transform, $F(\mu)$, of a function $f(x)$ and give the expression for the inverse Fourier Transform of $f(x)$ in terms of $F(\mu)$.
(b) Consider the function

$$
f(x)=\left\{\begin{array}{cc}
e^{-a x} & x \geq 0 \\
0 & x<0
\end{array}\right.
$$

for $a>0$ and find its Fourier Transform, $F(\mu)$.
(c) Now consider the function

$$
f(x)=e^{-a|x|}
$$

for $a>0$ where $-\infty<x<\infty$ and find its Fourier Transform.
(d) Show that the Fourier Transform of the function

$$
f(x)=\frac{1}{\left(1+x^{2}\right)}
$$

is $F(\mu)=\frac{1}{2} e^{-|\mu|}$.

