2003 Paper 11 Question 7

Continuous Mathematics

- (a) State the definition of the Fourier Transform, $F(\mu)$, of a function f(x) and give the expression for the inverse Fourier Transform of f(x) in terms of $F(\mu)$. [4 marks]
- (b) Consider the function

$$f(x) = \begin{cases} e^{-ax} & x \ge 0\\ 0 & x < 0 \end{cases}$$

for a > 0 and find its Fourier Transform, $F(\mu)$. [4 marks]

(c) Now consider the function

$$f(x) = e^{-a|x|}$$

for a > 0 where $-\infty < x < \infty$ and find its Fourier Transform. [4 marks]

(d) Show that the Fourier Transform of the function

$$f(x) = \frac{1}{(1+x^2)}$$

is $F(\mu) = \frac{1}{2}e^{-|\mu|}$. [8 marks]

1