## 1993 Paper 4 Question 10

## Numerical Analysis I

What is meant by the term *loss of significance*? What is the essential difference between the terms *condition* and *stability* in numerical analysis? Define the term *machine epsilon* and explain why it is an important parameter. [6 marks]

Use the recurrence formula

$$\cos[(k+1)\theta] = 2\cos\theta\cos[k\theta] - \cos[(k-1)\theta]$$

with starting values  $\cos 0 = 1$ ,  $\cos \theta = \frac{1}{\sqrt{2}} + \varepsilon$  to evaluate  $\cos 2\theta$  and show that loss of significance occurs. [4 marks]

Evaluate  $\cos 3\theta$  and  $\cos 4\theta$ , ignoring terms  $O(\varepsilon^3)$ . On this evidence, comment on the stability of the formula. [8 marks]

Is the computed value of  $\cos 2\theta$  acceptable? Explain your answer. [2 marks]