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Formal verification of the ARM6 micro-architecture

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Abstract

This report describes the formal verification of the ARM6 micro-architecture using the HOL theorem prover. The correctness of the microprocessor design compares the micro-architecture with an abstract, target instruction set semantics. Data and temporal abstraction maps are used to formally relate the state spaces and to capture the timing behaviour of the processor. The verification is carried out in HOL and *one-step* theorems are used to provide the framework for the proof of correctness. This report also describes the formal specification of the ARM6's three stage pipelined micro-architecture.

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1 Introduction

This report describes the formal verification of the ARM6 micro-architecture in HOL. This work forms part of a collaborative EPSRC funded project on the formal specification and verification of the ARM6. The project has been carried out with the support of ARM Ltd. Graham Birtwistle's group at Leeds have produced detailed ML specifications of the ARM architecture (Dominic Pajak) and the ARM6 micro-architecture (Daniel Schostak). At Cambridge, formal verification work has been undertaken using the HOL system. The Leeds specifications have been used as the basis for the production of compact and executable HOL models. The ARM instruction set architecture model is presented in [13]. Some simplifications have been made (with respect to the actual ARM6 and Daniel's high-fidelity specification) for the purposes of the initial verification attempt described here. Nevertheless, the verification is substantial and there is scope for carrying out additional more complete verifications in future. The approach used for the formal verification is based on work done at Swansea [17, 16, 14, 11], which has been formalised in HOL at Cambridge [12]. This approach provides a general and structured framework for carrying out processor verifications. However, before now only small scale (toy) case studies have been considered. This project aimed to apply these methods to a commercial processor design and, in doing so, assess the suitability of HOL for this task.

By developing executable models, it has been possible to test the HOL specifications with machine code generated by a GNU assembler. This has allowed sanity checks and extensive debugging to occur before carrying out the formal verification. The HOL specification of the ARM6 micro-architecture is presented in this report. However, it is *not* the intention of this report to give a fully extensive account of the ARM6 instruction set or the ARM6 micro-architecture. Rather, the functionality of the ARM6 is discussed to give a feel for the nature of the design and the correctness issues that arise as a consequence. The HOL specification of the ARM6 is presented in the appendix, primarily to show how the design is modelled in HOL and to illustrate the complexity of the design. Little attempt is made to explain the intricacies of the definitions therein. Two slightly different versions of the design (no-clobber and data forwarding) are presented and these represent two approaches to solving the problem of code invalidating the pipeline state (self-modifying code).

Section 2 provides a brief overview of processor verification work that was undertaken in the 1980s and 1990s. The algebraic approach to processor verification, which was developed at Swansea and used for the ARM6 verification, is presented in Section 3. This section provides an abstract definition of correctness and introduces the one-step theorems, which are used as the basis for the verification. An overview of the ARM instruction set is given in Section 4. The aim of this section is to highlight that ARM is a rich RISC architecture designed for writing compact, general purpose software for embedded systems: it is not a 'toy' architecture. The HOL specification of the architecture is documented in [13]. Modifications have been made to this specification, both in the course of the verification and as subsequent rationalizations; these changes are outlined in Section 5. The ARM6 micro-architecture is presented in Section 6: the data path is discussed in Section 6.1 and the pipeline control is described in Section 6.2. The formal verification is then discussed in Section 7. The HOL specification of the microarchitecture is given in the appendix.

2 Related Work

Several verifications of complete processors were undertaken during the 1980s and early 1990s. Examples include TAMARACK [24], SECD [3, 15], the partial verification of Viper [7, 8, 9], and Hunt's FM8501 and FM9001 [21, 22, 23] and Windley [36, 38]. All these processors were simple uniprocessor fetch-decode-execute engines specifically designed for formal verification. Following this work, Miller and Srivas verified the implementation of some of the instructions of a simple real processor called AAMP5 [27, 28]. A simplified version of the ARM2 processor was verified in [20].

Processors became much more complex from the later 1980s due to the addition of such

features as complex multi-stage pipelines, out-of-order execution and co-processors. Architectures like Alpha, MIPS, Pentium, and PowerPC were considered too complex for complete formal verification and the introduction of parallelism made their specifications that much harder. As a result, the main thrust of hardware verification research work has shifted from one-off proofs of whole processors to focusing on the analysis of fragments (such as buses, caches and pipelines) using a variety of techniques including theorem proving, temporal logic model checking and process algebra.

Various models of correctness have been applied to pipelined designs and a framework for categorizing these has been proposed in [1]. Burch and Dill [6] developed a pipeline flushing abstraction to show the equivalence between an instruction set architecture and a pipelined implementation. The ideas have been further developed by Burch, [5], Windley and Burch, [37], and Skakkebaek *et al.* [33], for pipelined microprocessors. Further developments to an out-of-order processor core have been made by Damm and Pnueli [10] and McMillan [26]. Sawada and Hunt [31] give a formal proof of a pipeline with exceptions which requires invariants between successive pipeline stages. Aagaard and Leeser [2] developed the transaction technique (mirroring how an instruction is decoded and executed down the pipeline stages) method to cater for pipelines with hazards which has been taken up by Launchbury's group at Oregon. The verification of Hennessey and Patterson's widely used pedagogical DLX RISC processor has been studied, using HOL, by Tahar and Kumar [34, 30, 35]. All the above used mechanized proof tools.

3 The Formal Verification of Processor Designs

This section outlines the approach used in the formal verification of the ARM6. A detailed account of this *algebraic framework* can be found in [12].

3.1 Approach

This section formalises, in an abstract setting, a definition of *correctness*. This definition can be applied to the formal verification of pipelined microprocessor designs (such as the ARM6). The approach is based on comparing two models:

- 1. The processor's micro-architecture (MA); and
- 2. The processor's instruction set architecture (ISA).

These two models occupy different levels of data and temporal abstraction, and this is made apparent when one formalises *state* and *time*. Correctness requires there to be a correspondence in behaviour between these two models. The MA and ISA are modelled using *state functions*; these are maps of the form $f: time \rightarrow state \rightarrow state$. The set *time* is required to be countable, and consequently it is simply assumed that $time = \mathbb{N}$. The set of states *state* is called the *state space*, and this is a non-empty set. The function f formally specifies the required behaviour of a design at some level of temporal and data abstraction: the state at time t, from the *pre-initial*¹ state a, is f t a. At the ISA level, the state will contain only entities visible to the programmer (typically, memory and registers) and each state transition marks the execution of a single instruction. At the MA level, the state transition normally from the implementation (for example, the pipeline state) and each state transition normally

¹The initialisation function f 0 maps arbitrary, pre-initialised states to valid initial states.

marks one processor clock cycle. Correctness requires there to be a correspondence between sequences of ISA and MA states.

Correctness is formalised in HOL with the following definition:

```
 \begin{split} \vdash_{\scriptscriptstyle def} \texttt{CORRECT} \ (\texttt{spec:num} \rightarrow \alpha \rightarrow \alpha) \ (\texttt{impl:num} \rightarrow \beta \rightarrow \beta) \ (\texttt{imm:} \beta \rightarrow \texttt{num} \rightarrow \texttt{num}) \ (\texttt{abs:} \beta \rightarrow \alpha) = \\ \texttt{IMMERSION} \ \texttt{imm} \ \land \\ \texttt{DATA\_ABSTRACTION} \ \texttt{abs} \ (\texttt{spec 0}) \ (\texttt{impl 0}) \ \land \\ \forall \texttt{t} \ (\texttt{a:} \beta). \ \texttt{spec t} \ (\texttt{abs a}) = \texttt{abs} \ (\texttt{impl imm a t}) \ \texttt{a}) \end{split}
```

The state function *impl* is the *implementation* (modelling the MA) and *spec* is the *specification* (modelling the ISA). The state spaces are related using a data abstraction **abs**. Temporal abstraction relates the *clocks* of the two systems, and this is the rôle of the *immersion* imm. Note that the temporal abstraction is a function of the pre-initialised state of the implementation. The DATA_ABSTRACTION and IMMERSION conditions are captured using the following definitions:

```
\vdash_{def} DATA\_ABSTRACTION \text{ abs init init'} = \forall a. \exists b. abs (init' b) = init a\vdash_{def} IMMERSION \text{ imm} = (\forall a. imm a 0 = 0) \land \forall a t1 t2. t1 < t2 \Rightarrow imm a t1 < imm a t2
```

The data abstraction criterion ensures that the implementation is complete with respect to the specification i.e. each initial state of the specification is an abstraction of an initial implementation state. An immersion is a monotonic increasing function from time, at the specification level, to time at the implementation level. The immersion is parameterized by the pre-initialised state of the implementation. The state functions *impl* and *spec* are required to be related with the condition:

$$\forall t \ a. \ spec \ t \ (abs \ a) = abs(impl \ (imm \ a \ t) \ a)$$

This condition ensures that after executing t instruction at the specification level, the processor state at time $imm \ a \ t$ is equivalent to the specification state, modulo applications of the data abstraction abs.

Correctness is defined with respect to the maps *abs* and *imm*, but it is possible for correctness to hold with respect to different abstractions. A less prescriptive presentation of correctness is:

```
dash_{\scriptscriptstyle def} IS_CORRECT spec impl = \exists imm abs. CORRECT spec impl imm abs
```

The verification of correctness then involves selecting suitable witnesses for the maps imm and abs.

The correctness framework described above is that used in the verification of the ARM6. This framework can be further enriched, for example, to accommodate input and output, and to deal with the temporal characteristics of superscalar processors. For a fuller account the reader is referred to [11, 12].

3.2 One-Step Theorems

This section describes an approach to the verification of correctness. This involves restricting the way in which state functions and immersions are defined. The following *one-step* theorem is used:

This theorem reduces the verification of correctness to a goal in which t has been specialised to the times 0 and 1. This avoids the need to carry out an explicit induction over time when verifying the main correctness goal. The conditions on the specification, implementation and immersion require them to be deterministic. An immersion is *uniform* with respect to a state function if, and only if, each interval imm a (t + 1) - imm a t is a function of the implementation's state at time imm a t. This is expressed with the following definitions:

```
 \begin{array}{l} \vdash_{def} \text{UNIFORM imm } f = \exists \text{dur. UIMMERSION imm } f \text{ dur} \\ \vdash_{def} \text{UIMMERSION imm } f \text{ dur } = \\ (\forall \texttt{a. 0 < dur a}) \land (\forall \texttt{a. imm a 0 = 0}) \land \\ \forall \texttt{a t. imm a (SUC t) = dur (f (imm a t) a) + imm a t} \end{array}
```

The *time-consistency* property is defined by:

 \vdash_{def} TCON f = \forall t1 t2 a. f (t1 + t2) a = f t1 (f t2 a)

Time-consistent state functions have primitive recursive definitions i.e. they can be modelled with *initialisation* and *next state* functions. Furthermore, a state function f is time-consistent if, and only if, the initialisation function $(f \ 0)$ is an identity map on the range of f. This invariance property forms the basis of the one-step theorem. Time-consistency is also defined with respect to an immersion:

```
 \vdash_{def} \text{TCON_IMMERSION f imm} = \\ \forall \text{t1 t2 a.} \\ \text{f (imm (f (imm a t2) a) t1 + imm a t2) a} = \\ \text{f (imm (f (imm a t2) a) t1) (f (imm a t2) a)}
```

Here initialisation is only required to be an identity map at times given by the immersion.

It is often the case that spec 0 a = a by definition, therefore proving TCON spec is normally trivial. Immersions can be constructed so as to be uniform, thus this becomes a relatively simple condition to prove. Nevertheless, ONE_STEP_THM would be of little use if were not possible to verify the TCON_IMMERSION property without resorting to an explicit induction over time. The following theorem is used:

```
_____ TC_IMMERSION_ONE_STEP_THM
```

```
 \label{eq:constraint} \begin{array}{l} \vdash \forall \texttt{f} \ \texttt{imm.} \ \texttt{IS_IMAP} \ \texttt{f} \ \land \ \texttt{UNIFORM} \ \texttt{imm} \ \texttt{f} \Rightarrow \\ (\texttt{TCON_IMMERSION} \ \texttt{f} \ \texttt{imm} = \\ (\forall \texttt{a}. \ \texttt{f} \ \texttt{0} \ (\texttt{f} \ (\texttt{imm} \ \texttt{a} \ \texttt{0}) \ \texttt{a}) = \texttt{f} \ (\texttt{imm} \ \texttt{a} \ \texttt{0}) \ \texttt{a}) \ \land \\ \forall \texttt{a}. \ \texttt{f} \ \texttt{0} \ (\texttt{f} \ (\texttt{imm} \ \texttt{a} \ \texttt{1}) \ \texttt{a}) = \texttt{f} \ (\texttt{imm} \ \texttt{a} \ \texttt{1}) \ \texttt{a}) \end{array}
```

The constraint IS_IMAP requires the state functions to be *iterated maps*, this is defined by:

```
 \vdash_{def} \text{IS_IMAP f} = \exists \text{ init next. IMAP f init next} \\ \vdash_{def} \text{IMAP f init next} = (\forall a. f 0 a = \text{ init a}) \land \forall t a. f (SUC t) a = \text{next (f t a)}
```

r0						
r1						
r2						
r3						
r4						
r5						
r6						
r7						
r8		r8_fiq				
r9		r9_fiq				
r10		r10_fiq				
r11		r11_fiq				
r12		r12_fiq			r13 abt	r13_und
r13		r13_fiq	r13_irq	r13_SVC	r14 abt	r14_und
r14		r14_fiq	r14_irq	r14_svc		
r15 (PC)						
CPSR	SP	SR fig	SPSR_irg	SPSR_svc	SPSR_abt	SPSR_und
L		<u>- [pii-</u>	·			
user mode	fiq mode	irq moc	l sv de mo	rc abo de mo	ort ur de	ndefined mode

Figure 1: ARM's visible registers.

The one-step theorems are, therefore, founded on the use of primitive recursive state functions. Using this approach, the verification of a processor, modelled by an iterated map impl, with respect to an ISA, modelled by an iterated map spec, is dominated by proving that the following set of equations hold for all processor states a:

$$impl \ 0 \ (impl \ (imm \ a \ 0) \ a) = impl \ (imm \ a \ 0) \ a \tag{1}$$

$$impl \ 0 \ (impl \ (imm \ a \ 1) \ a) = impl \ (imm \ a \ 1) \ a \tag{2}$$

$$spec \ 0 \ (abs \ a) = abs(impl \ (imm \ a \ 0) \ a) \tag{3}$$

$$spec \ 1 \ (abs \ a) = abs(impl \ (imm \ a \ 1) \ a). \tag{4}$$

Equations 1 and 3 are likely to be fairly easy to verify. In the case of the ARM6, the functions *impl* and *spec* are complex and the state space is large. This means that verifying equations 2 and 4 is very involved but, nonetheless, conceptually simple.

4 The ARM Architecture

This section gives a brief overview of Version 3 of the ARM 32-bit RISC architecture. The aim here is to introduce the main features of the architecture, rather than going into the full details of the instruction set semantics. A HOL specification of the ARM instruction set architecture is presented in [13]. The official ARM reference manual is [32].

4.1 Modes and Registers

The ARM architecture supports a number of *operating modes*, allowing privileged access to different register banks: see Figure 1. The ARM6 provides six modes: usr (user), fiq (fast interrupt), irq (standard interrupt), svc (supervisor call), abt (abort), and und (undefined instruction). Each mode provides access to sixteen general purpose registers, some of which are



Figure 2: Format of the CPSR.

Class	Instructions
Branch and Branch with Link	B, BL
Data Processing	ADD, ADC, SUB, SBC, RSB, RSC, CMP, CMN, AND, ORR, EOR, MOV, MVN, BIC, TST, TEQ
Multiply and Multiply Accumulate	MUL, MLA
PSR Transfer	MRS, MSR
Single Data Transfer	LDR, STR
Block Data Transfer	LDM, STM
Single Data Swap	SWP
Software Interrupt and Exceptions	SWI

 Table 1: The ARM Instruction Classes.

shared with other modes. For example, registers r0 through to r7 and the program counter r15 are the same for all modes. The CPSR (Current Processor Status Register) is a special purpose register used to keep track of the operating mode, interrupt status, and four condition code flags NZCV: see Figure 2. The CPSR is accessible in all modes, and the privileged modes (non-user modes) have their own SPSR (Saved Processor Status Register), and these are used to store the CPSR when entering the privileged mode. Register r14 in each mode is used as a *link* register, this stores the program counter address when taking an exception or sub-routine call.

4.2 Memory

In the ARM architecture, memory may be viewed as a linear array of 2^{32} bytes. Data items can be accessed either as bytes or as 32-bit words. When accessing words, address-alignment and byte-ordering are of significance.

4.3 Instruction Classes

The architecture has eight principle instruction classes: see Table 1. Instruction codes that do not correspond with a valid instruction form the *undefined* instruction class. Holes in the instruction space allow the instruction set to be extended for future generations of processors. Undefined instructions are detected at run time and they cause the processor to raise an undefined instruction exception. In the ARM architecture, *all* instructions are conditionally

executed at run time. Instructions that are not executed constitute the dynamic class of *unexecuted* instructions. All of the instructions listed in Table 1 are potentially members of this class.

Data processing instructions are used to perform logical and arithmetic operations, and data transfer instructions are used to transfer data between registers and memory. Both of these instruction classes are very flexible. For example, with single data transfers:

- A single byte or word can be transferred.
- Memory addresses are computed using a base address (stored in a register) and an offset.
- The offset can be added (up) or subtracted (down) from the base address.
- Pre- and post-indexing is possible.
- Base register write-back is allowed, facilitating auto-indexing.
- When loading a word from a mis-aligned memory address, the word is rotated right by 8, 16 or 24 places.

With data processing instruction:

- Eight arithmetic and eight logical operations are available.
- One of the source operands can be
 - an immediate value,
 - a register value,
 - a register value shifted by an immediate value,
 - a register value shifted by a register value, or
 - a register value shifted right one place and extended with the carry bit.

With the exception of shifting by a register value, the offset for a data transfer can be any of the above.

- The condition code flags NZCV can be set.
- A mechanism for retuning from exceptions (changing mode) is available.

Five types of shifting are possible: Logical shift left (LSL), Logical shift right (LSR), Arithmetic shift right (ASR), Rotate right (ROR) and Rotate right extend (RRX).

4.4 Features not Modelled

The following features have not been tackled:

- Thumb instructions.
- Co-processor instructions.
- External interrupts.

The Thumb instruction set can be viewed as a compressed form of a subset of the ARM instruction set. Thumb instructions are 16-bits long (which allows for a higher code density) and compliant ARM processors can switch to and from Thumb mode (flagged with bit five of the CPSR) in order to execute these instructions. This instruction set was introduced with the ARM7 family of processors and so it is not considered here.

Co-processor instructions allow the instruction set to be extended through the addition of co-processors. A strategy for modelling and verifying ARM designs with co-processor instructions has yet to be devised.

The ARM architecture supports two types of external interrupts: standard and fast. These exceptions have not been modelled. Accurately modelling exceptions at the ISA level is not trivial because exceptions tend to expose implementation dependent (pipelined) behaviour. One must consider exception priority and order, with respect to other (possibly simultaneous) exceptions and the instruction sequence. The correctness of systems with input has been studied in an abstract setting, [11], but further work is needed in this area.

5 The ARM Instruction Set Architecture Specification

The HOL specification of the ARM instruction set is described in [13]. This specification was used as the basis for the ISA model used in the ARM6 verification, but a number of modifications have been made. The specification was ported to the latest version of HOL: the Kananaskis release, instead of Taupo. This release adds a number of new features, some of which have been used to refine parts of the ISA specification. Other changes were made in order to reduce the verification effort and these features may be reinstated for later verification attempts. This section outlines the main modifications.

5.1 Unpredictable Behaviour

Some ARM instructions give rise to unpredictable (processor dependent) behaviour. For example, the instruction

EOR r1, r15, r2 ASR r3

is unpredictable because the first operand is the program counter. This was modelled in HOL by using an arbitrary value ARB to represent an unspecified state. However, this approach is not suited to processor verification using the definition of correctness presented in Section 3.1. This is because the ARM6 will always be in some concrete state and it does not make sense to compare these processor states (by equality after data abstraction) with the ISA state ARB. For the purposes of the initial verification attempt the ISA model was changed so as to conform with ARM6 behaviour. Other approaches will be considered in due course.

5.2 Words

In [13] the model of 32-bit words (the principle data type for the ARM architecture) was not wholly satisfactory. Words were defined with the following data type declaration:

```
Hol_datatype 'w32 = W32 of num'
```

This approach is flawed in that term equality does not correspond with word equality. That is to say, the following one-to-one theorem should *not* be true, but it is:

Operation	Function Name	Symbol	Type
One's Complement	word_1comp	NOT	word32→word32
Two's Complement	word_2comp	~	word32→word32
Addition	word_add	+	word32 \rightarrow word32 \rightarrow word32
Subtraction	word_sub	-	word32→word32→word32
Multiplication	word_mul	*	word32→word32→word32
Bitwise Conjunction	word_and	&	word32→word32→word32
Bitwise Disjunction	word_or		word32→word32→word32
Bitwise Exclusive Disjunction	word_eor	#	word32 \rightarrow word32 \rightarrow word32
Logical Shift Left	word_lsl	<<	word32→num→word32
Logical Shift Right	word_lsr	>>>	word32→num→word32
Arithmetic Shift Right	word_asr	>>	word32→num→word32
Rotate Right	word_ror	#>>	word32→num→word32
Rotate Right with Extend	RRX	None	bool→word32→word32

Table 2: Word operations.

 \vdash (W32 a = W32 b) = (a = b)

This precludes a clean presentation of word theorems i.e. some key results (for example, the commutative ring properties of word arithmetic) must be presented as conditional equations or with the inclusion of casting maps. This problem has been addressed with the development of a theory of n-bit words, which has been added to the HOL system. Words are constructed as an equivalence type over the natural numbers and, as such, the following theorem holds for 32-bit words:

⊢ (w32 a = w32 b) = (a MOD (2 EXP 32) = b MOD (2 EXP 32))

where $w32:num \rightarrow word32$ maps numbers to words.² The new word theory supplies numerous (equational) theorems about the word data type, and these have been used in the verification of the ARM6. Operator overloading is also provided: see Table 2. The pretty-printing of word ground terms has also been made possible with the Kananaskis release of HOL, thus the term w32 10 is displayed as 0xA.

The same model of words is used at both the instruction set and micro-architecture levels of abstraction. This reduces the *semantic gap* between the two levels of abstraction, and the sharing of primitive functions between ISA and MA specifications is advantageous. The correctness definition covers both the *data* and *control* aspects of a design, and hence it is important to be able to verify the equivalence of word expressions. Having an executable model of words also provides a means to test specifications through the execution of real code.

5.3 Data Types

Some rationalizations have been made to the specification through making better use of data types. For example, some *nested if* statements have been replaced with *case* statements.

²The function name w32 is actually a pseudonym for n2w in word32Theory.

Of particular significance is the modelling of the general purpose registers. In the original ISA specification, the register bank state space was modelled using six maps, each corresponding with the registers of a given mode. This has been simplified by using one map from register names to 32-bit words. The program status registers have also been modelled using a single map. The following type gives names to each of the registers:

```
Hol_datatype 'register = r0 | r1 | r2 | ... | r13_und | r14_und'
Hol_datatype 'psrs = CPSR | SPSR_fiq | ... | SPSR_abt | SPSR_und'
```

Thus, the register bank is modelled with the type $register \rightarrow word32$ and the program status registers have type $psrs \rightarrow word32$. Kananaskis provides a mechanism for type abbreviations, and this has been used as follows:

```
type_abbrev("mem", ':word30→word32'')
type_abbrev("reg", ':register→word32'')
type_abbrev("psr", ':psrs→word32'')
```

This enables the ARM registers and main memory to be given the type names mem, reg and psr. Note that HOL will still *display* these types in a fully expanded form: see [18].

The following data type declaration is made:

```
Hol_datatype 'exception = reset | undefined | software | address |
pabort | dabort | interrupt | fast'
```

This enables exceptions to be named (improving readability) and, with Kananaskis, one can utilize the generated functions num2exception and exception2num. Note that the exception address is redundant with respect to Version 3/4 of the ARM instruction set—it is a legacy of ARM's 26-bit memory addressing. This exception type has been added to the type declaration because it provides a straightforwards means to compute exception vectors, which in turn simplifies the specifications.

Instruction classes are named by the following type declaration:

Hol_datatype 'iclass = swp | mrs_msr | data_proc | reg_shift | ldr | str | br | swi_ex | undef | unexec'

The function DECODE_INST:num→iclass is used to decode instructions (at both levels of abstraction), and the ISA next state function is modified accordingly. The condition codes are also given a data type definition:

Hol_datatype 'condition = EQ | CS | MI | VS | HI | GE | GT | AL'

There are sixteen condition codes in total but the other eight are simply negations of the above. The definition of the ISA function CONDITION_PASSED is changed to be a case expression over the above data type.

5.4 Memory Access Operations

The following memory access operations are defined:

```
 \begin{array}{l} \vdash_{\scriptscriptstyle def} \texttt{MEMREAD} \ \texttt{mem} \ \texttt{addr} = \ \texttt{mem} \ (\texttt{TO}_\texttt{W30} \ \texttt{addr}) \\ \vdash_{\scriptscriptstyle def} \texttt{MEM}_\texttt{READ} \ \texttt{b} = \ \texttt{if} \ \texttt{b} \ \texttt{then} \ \texttt{MEM}_\texttt{READ}_\texttt{BYTE} \ \texttt{else} \ \texttt{MEM}_\texttt{READ}_\texttt{WORD} \\ \vdash_{\scriptscriptstyle def} \texttt{MEM}_\texttt{WRITE} \ \texttt{b} = \ \texttt{if} \ \texttt{b} \ \texttt{then} \ \texttt{MEM}_\texttt{WRITE}_\texttt{BYTE} \ \texttt{else} \ \texttt{MEM}_\texttt{WRITE}_\texttt{WORD} \end{array}
```

These functions help tidy up the presentation of the ISA specification. The function MEMREAD is used for word aligned memory access and is also used in the ARM6 specification, as is the function MEM_WRITE.

5.5 Features Dropped

The original ISA specification had a simplistic memory model, but memory aborts were modelled in the case of address mis-alignment. The modified specification drops all memory abort handling—it is assumed that abort exceptions are never raised. This means that the only exceptions that are handled are software interrupts and undefined instructions. Handling all of the exception types will require a more detailed memory model and a more sophisticated model of correctness.

It is assumed that little-endian word ordering is used throughout. This is a relatively minor change and verifying a version with big-endian ordering should not be difficult.

Finally, two instruction classes have been left out: multiply and multiply accumulate; and block data transfer. The main reason for this is that their verification would not be straight-forward. Both of these instruction classes are implemented (by the ARM6) with an iterated machine cycle i.e. the same cycle is repeated until completion. Multiplication is implemented using a modified Booth's algorithm: the data path is used to carry out additions/subtractions and shifts. In most modern processors the ALU can perform multiplication directly and so the multiplication algorithm does not encroach upon the main processor control logic. Such an implementation would be readily verifiable (at the level of abstraction covered by this report) and, therefore, it is not significant dropping this instruction class. However, verifying the block data transfer instruction class remains a challenge.

6 The ARM6 Implementation

The ARM6 design is split into control and data path components. The data path is presented in Section 6.1 and the control components are introduced in Section 6.2. The pipeline behaviour explained in Section 6.2.2.

6.1 The Data Path

The data path performs various data processing operations throughout the course of an instruction's execution. Figure 3 shows the data path for the ARM6. The main units are the field extractor/extender, the shifter and the ALU. There are two data buses, labelled A and B, supplying the inputs to the ALU; with bus B passing through the shifter. The behaviour of the data path is determined by the control unit. This section gives details of this data path control logic—the pipeline control is covered in Section 6.2. Section 6.1.1 defines the state space of the data path, and the following sections outline the functionality of the data path.

6.1.1 The Data Path State Space

The state space of the data path is modelled in HOL using the following type declaration:

Hol_datatype 'dp = DP of reg=>psr=>word32

The components are named as follows:

DP reg psr areg din alua alub

The components are:



Figure 3: The ARM6 Data Path.

Function	Description
AREG	Selects the value to be written to the AREG latch.
AREGN1	Gives the exception vector to be taken on the next cycle.
DIN	Selects the value to be written to the DIN latch.
DINWRITE	Indicates whether the DIN latch is to be updated.
NBW	Indicates whether the next memory access is for a byte or word.
NRW	Indicates whether the next memory access is a read or write.

Table 3: Functions used in specifying the memory interface.

reg	reg	The register bank
psr	psr	The program status registers
areg	word32	The address register
din	word32	The data-in register
alua	word32	ALU source register A
alub	word32	ALU source register B.

The register bank and program status register types are taken from the ISA model (see [13]). However, the program counter register r15 is treated differently: at the ISA level the program counter stores the address of the instruction being executed, whereas at this level the program counter is the address of the instruction being fetched. A program status register is conceptually a 32-bit word but with version 3/4 of the ARM ISA many of these bits are redundant. This means that the ARM6 does not use 32-bits in storing each status register. This detail is omitted in the implementation described here.

6.1.2 The Memory Interface

The main memory is accessed using the address register **areg**, which is the source/destination address for memory reads/writes. When writing to memory the data source is always bus B. When reading from memory the data is fed to the pipeline (see Section 6.2.2) and to the register din. Multiplexers are used to select the values used in updating the registers din and **areg**. The din register can either: (*i*) remain unchanged, (*ii*) take the value of the current instruction code **ireg**, or (*iii*) be updated with a word from memory. The **areg** register can take one of four values: (*i*) an exception vector, (*ii*) the value of register **r15**, (*iii*) the output of the ALU, or (*iv*) the output of the address increment.

The ARM6 data path actually contains a byte replicator between bus B and the memory, which is used when storing single bytes. This detail has been hidden within the definition of the function MEM_WRITE, which is taken from the modified ISA specification: see Section 5.4.

Table 3 lists the main functions that are responsible for the memory interface behaviour, and each of these functions is defined in Appendix A.1.

6.1.3 The Field Extractor/Extender

The field extractor/extender takes input from the register din and the result is fed to the bus B multiplexer (Section 6.1.6). The unit performs the task of extracting (and if necessary extending) an immediate field from the instruction register (for example, when accessing the branch offset). It is also used to select the appropriate bits from din when executing byte load (or swap) instructions. The field extractor/extender is modelled in HOL using the function FIELD, which is defined in Appendix A.2.

Function	Description
PCWA	Controls whether the incementor bus updates r15.
RAA	Determines which register is written to the RA bus.
RBA	Determines which register is written to the RB bus.
RWA	Controls the (ALU output) update of the Register Bank.

Table 4: Functions used in specifying general purpose register access.

Function	Description
PSRA	Indicates whether the CPSR or an SPSR is written to the PSRRD bus.
PSRDAT	Selects the value to be written to the PSRDAT bus.
PSRFBWRITE	Controls the PSRFB latch update.
PSRWA	Controls the updating of the Program Status Register Bank.

Table 5: Functions used in specifying program status register access.

6.1.4 The General Purpose Registers

Three read ports provide access to the general purpose registers, the outputs are labelled PCBUS, RA and RB. The program counter bus gives direct access to register r15 and is used when setting areg just prior to an instruction fetch. There are two write ports: one is used to update the program counter (after incrementing the address), and the other is connected to the ALU output. Table 4 lists the functions used in accessing the registers, and they are defined in Appendix A.3.

6.1.5 The Program Status Registers

The program status registers are accessed using two read ports and one write port. One of the read ports is dedicated to the CPSR, which is fed to the control unit. The CPSR status flags and mode influence the execution of instructions. The carry flag is also fed to the shifter and the ALU. The write port is used to update either the CPSR or an SPSR. A multiplexer is used to construct a new PSR word using data from the shifter (i.e. the carry out), the ALU and the control unit. Table 5 lists the functions used in accessing the PSRs, and they are defined in Appendix A.4.

6.1.6 The Data Buses and Shifter

There are two buses: bus A takes a value from a general purpose register or from a program status register; bus B passes through the shifter and takes a value from the field extractor/extender (Section 6.1.3) or from the register bank. The 32-bit bus values are stored in registers alua and alub respectively. The shifter also outputs a carry flag, which is fed to the control unit and is used in updating the PSRs (Section 6.1.5). The (barrel) shifter can perform one of five types of shift operation (LSL, LSR, ASR, ROR or RRX). A carry in is input from the PSR unit. The shift amount is either: zero; an immediate value (taken from ireg in the control unit); a register shift amount (taken from sctrlreg in the control unit); or it is an alignment amount (constructed from oareg in the control unit). The last case is used when loading bytes or when reading from a mis-aligned memory address. Table 6 lists the functions used to specify the shifter and bus behaviour, and they are defined in Appendix A.4.

Function	Description
BUSA	Selects the value to be written on bus A.
BUSB	Selects the value to be written on bus B.
SCTRLREGWRITE	Controls the SCTRLREG latch update.
SHIFTER	Gives the output of the barrel shifter, which includes a carry out.

Table 6: Functions used in specifying the shifter and bus behaviour.

Function	Description
ALU6	Gives the output of the ALU, which includes the NZCV flags.
ALUAWRITE	Controls the ALUA latch update.
ALUBWRITE	Controls the ALUB latch update.

 Table 7: Functions used in specifying the ALU behaviour.

6.1.7 The ALU

The ALU performs arithmetic and logical operations on 32-bit words. The operands are read from alua and alub. The ALU also takes the CPSR carry flag, which is needed for executing the ADC and SBC instructions. The unit outputs a 32-bit word together with four status flags NZCV. The ALU is used to: (i) execute the operations from the data processing instruction class; (ii) simply select alua or alub; (iii) implement the auto indexing for data transfers; and (iv) compute branch destination and link register values. Table 7 lists the functions used in specifying the ALU behaviour, and they are defined in Appendix A.6.

6.2 The Control Unit

The behaviour of the pipeline and data path is determined by the control unit. The state space of this unit is given in Section 6.2.1. The ARM6 has a three stage pipeline with fetch, decode and execute stages. The fetch and decode stages always take one machine cycle to complete. Some instructions require more than a single machine cycle to execute, and this means that the fetch and decode stages do not proceed on all cycles. Details of this pipeline behaviour are given in Section 6.2.2.

6.2.1 The Control State Space

The state space of the control unit is modelled in HOL using the following type declaration:

The components are named as follows:

CTRL pipea pipeaval pipeb pipebval ireg iregval apipea apipeb ointstart onewinst opipebll nxtic nxtis aregn nbw nrw sctrlreg psrfb oareg

The first eight components give the state of the pipeline:

pipea	word32	Stores a fetched instruction code
pipeaval	bool	Indicates whether pipea has been invalidated
pipeb	word32	Stores an instruction code prior to decode
pipebval	bool	Indicates whether pipeb has been invalidated
ireg	word32	Stores the instruction code after decode
iregval	bool	Indicates whether ireg has been invalidated
apipea	word32	The source memory location for pipea
apipeb	word32	The source memory location for pipeb.

The components apipea and apipeb are not taken from the actual ARM6 design. They have been added in order to implement correct behaviour (see Section 3.1) when writing to the memory addresses pc and pc-4: see Examples 3 and 4 in Section 6.2.2.

The next five components control the pipeline behaviour:

bool	Indicates whether an exception has been raised
bool	Indicates whether a new instruction has been decoded
bool	Controls whether an instruction will be fetched
iclass	The class of the next instruction to be executed
iseq	The next instruction sequence (for multi-cycle execution).
	bool bool iclass iseq

The remaining components relate to the data path control:

aregn	num	An exception vector
nbw	bool	Controls whether memory access is for a byte or a word
nrw	bool	Controls whether memory access is read or write
sctrlreg	word32	Stores a shift value, which is read from the register bank
psrfb	word32	Stores a word read from the PSRs
oareg	num	The two least-significant bits of the address register.

Note that **aregn** is naturally a 3-bit word³ and **oareg** is a 2-bit word, but for convenience natural numbers are used. The instruction class type **iclass** is defined at the ISA level: see Section 5. The instruction sequence type is declared with:

Hol_datatype 'iseq = t3 | t4 | t5 | t6'

These values could be encoded using 2-bit words.

6.2.2 The Pipeline

The behaviour of the pipeline is explained in this section with the aid of some sample code. This code has been designed to demonstrate some of the intricacies of the design, and is otherwise without purpose. In fact, it is inadvisable to write code of the form found in Examples 3 and 4.⁴ The pipeline has three stages: fetch, decode and execute. A *single-cycle* instruction is in the execute stage for just one cycle, and in the pipeline for three cycles in total. Multi-cycle instructions require more than a single cycle at the execute stage; consequently

 $^{^{3}}$ In fact a single bit would suffice here because only two types of exception are modelled: undefined instructions and software interrupts.

⁴It is good programming practise, when writing assembly code, to ensure that the program and data address spaces are clearly demarcated. Ignoring this guideline leads to the production of obfuscated code and in some cases it will expose (the pipeline) details of a particular processor implementation.

they are in the pipeline for more than three cycles. The distinction between single- and multi-cycle instructions should become clear in the following examples.

Instructions are fetched from the current program counter address pc, which is register r15. Therefore, pc is *not* the address of the instruction being *executed*. In general, the instruction being executed is from address pc-8 and the instruction being decoded is from address pc-4. This is further complicated with multi-cycle instructions because the program counter is incremented on the first execute cycle, which means that the execute and decode instructions then correspond with addresses pc-12 and pc-8 respectively.

Example 1. Consider the following fragment of ARM code:

a:	sub	pc,	pc,	#4			0	0xE24FF004
b:	swp	r0,	r1,	[r2]]		0	0xE1020091
c:	add	r0,	r1,	r2,	ROR	r3	0	0xE0810372
d:	b	a					0	OxEAFFFFB
e:	mvn	r0,	#3				0	0xE3E00003
f:	cmp	r0,	r1				0	0xE1500001

The letters to the left of the colon are instruction labels. The commented hexadecimal numbers to the right (after the @ symbol) are the 32-bit encodings for each of the respective instructions. When executing the code in HOL these values are used to track the flow of instructions through the pipeline. The instructions have the following affect:

- 1. The subtract (sub): This instruction causes a branch to address pc-4. This is the address of the second instruction, and so this is effectively a no-op instruction.
- 2. The swap (swp): This takes four cycles to execute; involving a read from, and write to, main memory.
- 3. The add (add): This takes two cycles to execute. The fist cycle is used to store register r3 in the control unit component sctrlreg.
- 4. The branch (b): The pipeline is returned to the initial state i.e. the pipeline state prior to executing the sub instruction. The mvn and cmp instructions, having been fetched, are not decoded or executed.

Figure 4 shows the pipeline flow for this sequence of instructions. Instruction mnemonics and labels are shown on the *y*-axis and time increases along the *x*-axis. Each block represents the operation (fetch, decode or execute) performed on an instruction. Multi-cycle instructions are emphasised by marking the additional execute stages with a lighter colour. Observe that during the execution of the **swp** and **add** instructions, a fetch occurs on the first execute cycle and a decode occurs on the last execute cycle. This explains the significance of the component **pipeb**, which stores an instruction code prior to decode. (If the fetch and decode were always simultaneous then **pipeb** would be redundant.) A fetch occurs on each execute cycle of the branch. With single-cycle instructions fetch and decode occur simultaneously with the execute. From Figure 4 it is clear that all but the first instruction is multi-cycle. The first instruction (**sub**) is single-cycle, but a further two cycles are needed to re-fill the pipeline after **pc** is modified. Strictly speaking, these extra cycles are deemed not to constitute part of the instruction's execute stage but they are of significance from a correctness standpoint.

Table 8 shows the pipeline behaviour with respect to the first thirteen components of the control unit. The instruction labels have been used, in place of the instruction codes, to indicate the state of the components pipea, pipeb and ireg. Observe that the components



Figure 4: Pipeline flow for Example 1.

State \setminus Cycle	<u>0</u>	1	2	<u>3</u>	4	5	6	<u>7</u>	8	9	10	11	<u>12</u>
pipea,pipeaval	b,T	c,F	b,T	c,T	d,T	d,T	d,T	d,T	e,T	e,T	f,T	a,T	b,T
pipeb,pipebval	b,T	c,F	b,T	c,T	c,T	c,T	c,T	d,T	d,T	e,T	f,T	a,T	b,T
ireg,iregval	a,T	b,F	c,F	b,T	b,T	b,T	b,T	c,T	c,T	d,T	d,T	d,T	a,T
ointstart	F	F	F	F	F	F	F	F	F	F	F	F	F
onewinst	Т	Т	Т	Т	F	F	F	Т	F	Т	F	F	Т
opipebll	Т	Т	Т	Т	F	F	F	Т	F	Т	Т	Т	Т
nxtic	data_proc	swp	reg_shift	swp	swp	swp	swp	reg_shift	reg_shift	br	br	br	data_proc
nxtis	t3	t3	t3	t3	t4	t5	t6	t3	t4	t3	t4	t5	t3

Table 8: The pipeline behaviour for Example 1.

pipeaval, pipebval and iregval are used to implement the re-filling of the pipeline (tagging invalidated instruction codes) after the sub instruction writes to register pc. This differs from the branch instruction, which takes three cycles to *execute*, re-filling the pipeline in the process.

The states are grouped together into blocks, with the cycle at the start of each block underlined. This grouping corresponds with the temporal abstraction used in verifying the design. The underlined cycles are specified by an immersion, which gives the times at which data abstraction yields ISA states. These states are characterised by the fact that the pipeline is ready for the first execute cycle of the instruction in **ireg**.

Example 2. This example considers the pipeline flow for the unexecuted and undefined instruction classes. When an undefined instruction code is encountered an exception is raised, causing a branch to memory address 0x4. The following code fragment forms part of a stub exception handler:

0x0: movsr15,#32© 0xE3B0F020 - Reset0x4: movsr15,r14© 0xE1B0F00E - Undefined Instruction0x8: movsr15,r14© 0xE1B0F00E - Software Interrupt0xC: subsr15,r14,#4© 0xE25EF004 - Prefetch Abort

This simplistic exception handler ignores each exception and returns to the link address, which is stored in register r14.

The code containing the unexecuted and undefined instructions is given below:

a:	andnv	r0,	r0,	r0			0	0xF000000
b:	${\tt undef}$						0	0xE6000010
c:	mvn	r0,	#3				0	0xE3E00003
d:	\mathtt{cmp}	r0,	r1				Q	0xE1500001
e:	str	r12	, [r:	1,r5,	ASR	#6]!	0	0xE7A1C345

The first instruction is never⁵ executed and the second instruction has an undefined instruction code. Figure 5 shows the pipeline flow and Table 9 shows the state component trace for this example. The unexecuted instruction andnv is initially decoded and identified as a data processing instruction. When the instruction comes to being executed the actual instruction class (ic) is determined to be unexec. The value ic is computed by examining the condition code (bits 31-28 of the instruction register) and, as appropriate, performing tests on the program status flags. If the class is determined to be unexec then the execute stage does not proceed. The undefined instruction gives rise to an exception, which is handled by the swi_ex instruction class; the execution of which is shown in Figure 5 using different coloured boxes (labelled with an I). Exceptions have a similar behaviour to branch (with link) instructions and they take three cycles to execute. The control component aregn has value 1 at cycle two and the exception causes a branch to address aregn*4.

Example 3. This example has been devised to illustrate the execution of self-modifying code. The ARM6 has a von Neumann style architecture—program and data memories are not separated. This means that it is possible for a program to modify the memory at locations coincident with the code being executed. Therefore, one must consider what happens when instructions in the pipeline are overwritten in memory. The following code fragment contains store and swap instructions, both of which try to modify the code itself:

⁵Note that using the never (nv) condition code is strongly discouraged by ARM because it utilizes an area of the instruction space reserved for future use.



Figure 5: Pipeline flow for Example 2.

State \setminus Cycle	<u>0</u>	<u>1</u>	2	3	4	5
pipea,pipeaval pipeb,pipebval ireg,iregval ointstart onewinst opipebll nxtic	b,T b,T a,T F T T data_proc	 c,T c,T b,T F T T undef	d,T d,T c,T T T swi_ex	e,T e,T c,T F F T swi_ex	0×4,T 0×4,T c,T F F T swi_ex	2 0×8,T 0×8,T 0×4,T F T T data_proc
nxtis	t3	t3	t3	t4	t5	t3

Table 9: The pipeline behaviour for Example 2.

a:	ldr	r0,	f		0	0xE59F000C
b:	adr	r1,	е		0	0xE28F1004
c:	swp	r2,	r0,	[r1]	0	0xE1012090
d:	str	r2,	f		0	0xE58F2000
e:	\mathtt{cmp}	r3,	#1		0	0xE3530001
f:	mvn	r4,	#2		0	0xE3E04002
g:	mov	r5,	#3		0	0xE3A05003

The instruction labelled \mathbf{f} is first read into register $\mathbf{r0}$. The *pseudo-instruction*⁶ adr causes $\mathbf{r1}$ to take the address of the instruction with label \mathbf{e} . The swap instruction stores the instruction code of \mathbf{f} (which is in $\mathbf{r0}$) at address \mathbf{e} . The old instruction code at \mathbf{e} is stored in $\mathbf{r2}$. The store instruction then stores this instruction code at address \mathbf{f} . At this point the instructions labelled \mathbf{e} and \mathbf{f} have been swapped in memory. The remaining instruction perform simple data-processing operations.

When this sequence of instructions is executed on an ARM6, the cmp and mvn instructions are executed in the original program order, even though the instructions are swapped in memory. This is because in both cases the instructions are fetched prior to updating the memory. The HOL model of the ARM instruction set architecture does not take account of this. In the abstract ISA model the mvn instruction is executed before the cmp instruction. Consequently there is an inconsistency in behaviour between the two levels of abstraction, preventing a formal verification of the design. This needs to be addressed, and a number of options have been considered:

- 1. Leave the ARM6 model unchanged and investigate one of the following:
 - (a) Modify the ISA specification so as to implement (highly abstract) pipeline behaviour.
 - (b) Modify the ISA specification—abstracting out details of instruction sequencing. This would require a small modification to the ISA model, but necessitate a more elaborate definition of correctness.
 - (c) Deem such self-modifying code to be unpredictable. It would then be necessary to modify the correctness definition, so as to accommodate unpredictable behaviour.
- 2. Change the data behaviour of the ISA and ARM6 models. If the swp and str instructions do not write over (clobber) the following two instructions, then correctness holds. This involves minor changes to both specifications and preserves the ARM6 pipeline behaviour.
- 3. Change the pipeline behaviour of the ARM6, so as to correctly implement the abstract ISA behaviour. This has been implemented using data forwarding, and consequently it only affects the timing of str instructions when writing over the following instruction (one extra cycle is needed).

Options 2 and 3 are implemented with the no-clobber and data forwarding versions of the ARM6 respectively. These versions are very similar and the small differences in the control logic may be seen in Appendix C. Unless otherwise stated, this report will focus on the no-clobber implementation. Option 1(a) is not ideal because it would involve changing the state space of the ISA. Options 1(b) and 1(c) are promising and will be investigated in due course.

 $^{^{6}}$ Pseudo-instructions are converted by the assembler into a real ARM instructions. In this example the **adr** becomes an **add** instruction.

State \setminus Cycle	<u>0</u>	1	2	<u>3</u>	4	5	6	7	8	9	<u>10</u>	<u>11</u>
pipea,pipeaval pipeb,pipebval	b,T b,T	c,T b,T	c,T b,T	c,T c,T	d,T d,T	e,T d,T	e,T d,T	e,T d,T	e,T e,T	f,T e,T	f,T f,T	g,T g,T
ointstart	a,i F	a, i F	a, i F	D,I F	F	C,I F	C,I F	F	G,I F	G,I F	F	F
onewinst	Т	F	F	Т	Т	F	F	F	Т	F	Т	Т
opipebll	Т	F	F	Т	Т	F	F	F	Т	F	Т	Т
nxtic	ldr	ldr	ldr	data_proc	swp	swp	swp	swp	str	str	data_proc	data_proc
nxtis	t3	t4	t5	t3	t3	t4	t5	t6	t3	t4	t3	t3

State \setminus Cycle	<u>0</u>	1	2	<u>3</u>	<u>4</u>	5	6	7	8	9	<u>10</u>	<u>11</u>
pipea,pipeaval	b,T	c,T	c,T	c,T	d,T	e,T	e,T	[f],T	[f],T	f,T	[e],T	g,T
pipeb,pipebval	b,T	b,T	b,T	c,T	d,T	d,T	d,T	d,T	[f],T	[f],T	[e],T	g,T
ireg,iregval	a,T	a,T	a,T	b,T	c,T	c,T	c,T	c,T	d,T	d,T	f,T	[e],T
ointstart	F	F	F	F	F	F	F	F	F	F	F	F
onewinst	Т	F	F	Т	Т	F	F	F	Т	F	Т	Т
opipebll	Т	F	F	Т	Т	F	F	F	Т	F	Т	Т
nxtic	ldr	ldr	ldr	data_proc	swp	swp	swp	swp	str	str	data_proc	data_proc
nxtis	±3	±4	t5	±3	+3	+4	±5	±6	±3	±4	+3	±3

(a) Actual ARM6 behaviour.

(b) With data forwarding.

Table 10: The pipeline behaviour for Example 3.

Figure 6 shows the pipeline flow for this example. In Figure 6(a) the instruction sequence corresponds with the actual ARM6 behaviour. This is also the pipeline flow for Option 2 above. In Figure 6(b) data forwarding is introduced, which implements the abstract ISA behaviour. Data forwarding is a technique used to resolve dependencies in pipelines—completed computations are used to update the pipeline state, thus avoiding the need to re-load (modified) data from its original source. In Figure 6(b) the boxes labelled W-a mark instances where the word being stored in memory is also forwarded to pipea. This is triggered when there is a match between the current address register (see Section 6.1.2) and apipea. This could be implemented in hardware without great difficulty.

The pipeline states for this example are shown in Table 10. The true ARM6 behaviour is shown in Table 10(a) and this can be contrasted with Table 10(b) which shows the data forwarding behaviour.

Example 4. In the previous example the instruction fetched from address pc (stored in pipea) is compromised by a memory store to the pc address. The following code fragment is used to illustrate a memory store to address pc-4.

a:	ldr	r0,	е	0	0xE59F0008
b:	str	r0,	с	0	0xE50F0004
c:	\mathtt{cmp}	r3,	#1	0	0xE3530001
d:	mvn	r4,	#2	0	0xE3E04002
e:	mov	r5,	#3	0	0xE3A05003

In this example data forwarding does not provide a simple fix. This is because the cmp instruction (labelled c) is decoded simultaneously with the memory store; however it then becomes necessary to decode the mov instruction, as this is forwarded to pipeb replacing the cmp. The original ARM6 pipeline behaviour is modified with the introduction of an extra cycle.



(a) Actual ARM6 behaviour.



(b) With data forwarding.

Figure 6: Pipeline flow for Example 3.

pipea,pipeaval b,T pipeb,pipebval b,T ireg,iregval a,T ointstart F	c,T b,T a,T	c,T b,T a,T	c,T c,T b,T	d,T c,T b,T	d,T d,T c,T	e,T e,T d,T
onewinst T opipebll T	F F F	F F F	F T T	F F F	F T T	F T T
nxtic 1dr	ldr	ldr	str	str	data_proc	data_proc
nxtic 1dr	F ldr	F ldr	T str	F str	T data proc	T data proc

(a) Actual ARM6 behaviour.

State \setminus Cycle	<u>0</u>	1	2	<u>3</u>	4	5	<u>6</u>	<u>7</u>
pipea,pipeaval pipeb,pipebval ireg,iregval ointstart onewinst opipebl	b,T b,T a,T F T T	c,T b,T a,T F F	c,T b,T a,T F F F	c,T c,T b,T F T T	d,T c,T b,T F F F	d,T e,T c,F F T T	d,T d,T e,T F T T	2 e,T e,T d,T F T T
nxtic nxtis	ldr t3	ldr t4	ldr t5	str t3	str t4	data_proc t3	data_proc t3	data_proc t3

(b) With data forwarding.

 Table 11: The pipeline behaviour for Example 4.

In this cycle the mov decode is carried out and the mvn instruction is also re-fetched. The fetch may seem unnecessary (because the required instruction code is already in the pipeline) but it keeps the control logic fairly simple.

The pipeline flow for this example, with and without data forwarding, is shown in Figure 7. The box labelled W-b shows data forwarding to pipeb. Table 11 gives the state changes for this example.

6.2.3 Formal Specification

The functions used to specify the ARM6 pipeline control are listed in Table 12. The formal specification of these functions is given in Appendix B. Most of these functions are inherently simple in definition and some have been further simplified by the absence of (most) exceptions, and by omitting the multiply and block data transfer instruction classes. Daniel Schostak's phase level specification is far less abstract but one of the objectives of his work was to provide formal, high fidelity models.

6.3 The ARM6 State Function

The ARM6 state space is modelled in HOL with the following type declaration:

Hol_datatype 'state_ARM6 = ARM6 of mem=>dp=>ctrl'

where mem is a type abbreviation for word30 \rightarrow word32. The ARM6 is modelled with the function STATE_ARM6, which is defined by:

 \vdash_{def} STATE_ARM6 O a = INIT_ARM6 a \land STATE_ARM6 (SUC t) a = NEXT_ARM6 (STATE_ARM6 t a)



(a) Actual ARM6 behaviour.



(b) With data forwarding.

Figure 7: Pipeline flow for Example 4.

Function	Description
ABORTINST	Indicates whether the instruction in execute has failed its condition code or has been invalidated.
IC	Gives the instruction class for the current instruction cycle.
INTSEQ	Indicates whether an exception vector is to be taken on the next instruction cycle.
IREGVAL	Indicates whether the next execute stage has been invalidated by a direct change to r15.
IS	Gives the instruction sequence for the current instruction cycle.
NEWINST	Indicates whether a new instruction is to be executed.
NXTIC	Gives the instruction class for the next instruction cycle. (Provided the condition is passed.)
NXTIS	Gives the instruction sequence for the next instruction cycle.
PCCHANGE	Indicates whether r15 is changed (other than by a branch or exception vector) in the current instruction cycle.
PIPEALL	Indicates whether the result of instruction fetch is to be latched to PIPEA.
PIPEAVAL	Indicates whether instruction fetch has been invalidated by a direct change to r15.
PIPEAWRITE	Controls the PIPEA latch update.
PIPEBLL	Indicates whether the instruction in predecode is to be preseved in the current instruction cycle.
PIPEBWRITE	Controls the PIPEB latch update.
PIPECWRITE	Controls the PIPEC latch update.
PIPESTATAWRITE	Controls the PIPEAVAL latch update.
PIPESTATBWRITE	Controls the PIPEBVAL latch update.
PIPESTATIREGWRITE	Controls the IREGVAL latch update.

 Table 12: Functions used to specify the pipeline control.

The functions INIT_ARM6 and NEXT_ARM6 are specified in Appendix C, and they are discussed in the following sections.

6.3.1 The Initialisation Function

The initialisation function is critical to the verification of a design when using the one-step theorems of Section 3.2. If the initialisation function is suitably defined then time-consistency (with respect to an immersion) will hold. The process of defining the initialisation function can be likened to developing an invariant for an inductive proof. Not all implementation states are valid and the primary job of the initialisation function is to ensure that the implementation states in a suitable state. There must be at least one initial state for each state at the ISA level (this is the DATA_ABSTRACTION condition). Non-initial states will either be completely erroneous (the processor should never exhibit such states) or states that the machine passes through in the course of instruction execution. Examples of these two cases are:

- Erroneous: any state with nxtic = data_proc, iregval = T, onewinst = F and nxtis = t5.
- Intermediate: a state with nxtic = reg_shift, iregval = T, onewinst = F and nxtis = t4 and the rest of the state corresponding with one cycle through the execution of a reg_shift instruction.

The first case is erroneous because it is inconsistent with control logic i.e. the next instruction sequence is never t5 for a data processing instruction. The second case *could* be considered initial (with the immersion defined accordingly) but to do so would add unnecessary complexity i.e. the initialisation function would not have a simple definition and more cases would have to be considered in the verification. The initialisation function forces the processor to be in a state

for which nxtis = t3 and the pipeline is set so as to be consistent with the program counter value. In this way, the initial states are those at the beginning of the blocks in Tables 8-11. It is the job of the duration map to define how many cycles there are between two initial states. This corresponds with the number of cycles taken at the execute stage, which is a function of the instruction register.

The function INIT_ARM6 is the same for the no-clobber and data forwarding implementations. After initialisation, the instruction about to executed is in the **ireg** register and this is from memory address pc-0x8. The rest of the state is consistent with having fetched and decoded this instruction. The instruction at address pc-0x4 is fetched and the next instruction to be fetched is from address pc.

6.3.2 The Next State Function

The next state function NEXT_ARM6 is specified in Appendix C. Two versions are presented and these correspond with Options 2 and 3 from page 25. The next state function is decomposed into two functions: PHASE1 and PHASE2. By the end of the first phase the ALU registers (alua and alub) have the right values. The field extractor/extender and shifter have both been utilized by this point. In the second phase the ALU becomes active and results are stored as appropriate. Instruction decode also occurs in the second phase.

The next state function brings together all of the control logic and data path operations defined in Sections 6.1 and 6.2.

7 The ARM6 Verification

In Section 7.1 the correctness of the ARM6 is formally stated in terms of a data abstraction (Section 7.1.1) and temporal abstraction (Section 7.1.2). The formal verification of this correctness statement is discussed in Section 7.2.

7.1 Correctness Statement

The following correctness statement has been verified:

```
CORRECT STATE_ARM STATE_ARM6 IMM_ARM6 ABS_ARM6
```

The immersion IMM_ARM6 and data abstraction ABS_ARM6 are defined in Appendix D. The ISA state function STATE_ARM was originally defined in [13] but modifications have been made since, as outlined in Section 5. This correctness statement has been verified for two pairs of state functions i.e. for the no-clobber and data forwarding implementations. The no-clobber version requires the ISA specification to be modified so as to avoid writing over the pipeline state; see Section 6.2.2.

7.1.1 Data Abstraction

The data abstraction ABS_ARM6 is specified in Appendix D. The map is essentially a projection, extracting out the memory mem, the general purpose registers reg and program status registers psr. The later two are taken from the data path unit. However, the program counter is decremented by eight, and this adjusts for the pipeline. That is to say, the ARM6 is about to execute the instruction from address pc-0x8 and not that from address pc. The ISA model

executes the instruction from address pc and adds eight to this value (as appropriate) when executing an instruction. This (offset by eight) relationship between the two program counters must be preserved in order for correctness to hold.

An alternative approach would have been to mimic the MA program counter behaviour at the ISA level. This is illustrated in the following table:

	ISA model	MA model
Execute instruction	рс	pc-0x8
Reading during execution	pc+0x8	pc
	pc+0x12	pc+0x4
Writing during execution	рс	pc+0x8
Data abstraction	pc⊢→pc-0x8	pc⇔pc

The data abstraction is a pure projection if one adopts the MA behaviour at the ISA level. However, very little is gained by this approach (at the ISA level one must modify pc write instead of pc read) and it runs contrary to the spirit of the ARM architectural reference.

The data abstraction is surjective (and the initialisation function never modifies mem, reg or psr) and therefore it is possible to verify the DATA_ABSTRACTION condition: see Section 7.2.2. This mean that the ARM6 implements all of the ISA behaviour.

7.1.2 Temporal Abstraction

The immersion IMM_ARM6 is specified in Appendix D. This function is defined so as to be uniform with respect to STATE_ARM6 using a duration map DUR_ARM6. The duration map gives a value from one to six cycles. The data forwarding version has a slightly more complicated duration map—an extra cycle is needed for str instructions that write to pipeb. In order to detect such cases the ISA functions DECODE_LDR_STR and ADDR_MODE2 are used to determine the destination address for the store.

7.2 Formal Verification

The formal verification is structured around proving the following results:

- 1. The immersion IMM_ARM6 is uniform with respect to STATE_ARM6.
- 2. The data abstraction $\texttt{ABS_ARM6}$ meets the $\texttt{DATA_ABSTRACTION}$ condition.
- 3. The state function STATE_ARM is time-consistent, and the state function STATE_ARM6 is time-consistent with respect to IMM_ARM6.
- 4. The state function STATE_ARM6 is correct with respect to STATE_ARM, IMM_ARM6 and ABS_ARM6.

These goals are discussed in the following sections.

7.2.1 Uniformity

The duration map DUR_ARM6 is used as the witness in proving

⊢ UNIFORM IMM_ARM6 STATE_ARM6

It is necessary to prove

 \vdash \forall a. 0 < DUR_ARM6 a

and this can be verified in HOL using the simplification tactic RW_TAC.

7.2.2 Completeness

For each ISA state ARM mem reg psr the processor state

ARM mem (DP (ADD8_PC reg) psr areg din alua alub) ctrl

is a suitable witness for the DATA_ABSTRACTION property. Free variables are used for components other than mem, reg and psr. The function ADD8_PC is defined by:

⊢_{def} ADD8_PC reg = SUBST reg (r15,reg r15 + 0x8)

This function is the inverse of SUB8_PC:

 $\vdash \forall r. SUB8_PC (ADD8_PC r) = r$

This theorem was not verifiable when using the old 32-bit type definition; see Section 5.2. This meant that it was impossible to prove the data abstraction condition (because it was false) without resorting to modifying the definitions of SUB8_PC and ADD8_PC. The development of word32Theory has been of great use in this regard.

7.2.3 Time-Consistency

The state function STATE_ARM does not have an initialisation function and therefore the following theorem can be used to derive time-consistency:

 $\vdash \forall \texttt{f} \texttt{ next. IMAP f I next} \Rightarrow \texttt{TCON f}$

where I is the identity map. This theorem states that any iterated map whose initialisation function is the identity map is time-consistent.

Establishing the time-consistency of STATE_ARM6 with respect to IMM_ARM6 is more involved. The theorem TC_IMMERSION_ONE_STEP_THEOREM is used to derive the following equivalence:

```
\label{eq:constant} \begin{split} \vdash \mbox{TCON_IMMERSION STATE_ARM6 IMM_ARM6} = & (\forall a. \mbox{STATE_ARM6 0 (STATE_ARM6 (IMM_ARM6 a 0) a)} = \mbox{STATE_ARM6 (IMM_ARM6 a 0) a)} \land \\ \forall a. \mbox{STATE_ARM6 0 (STATE_ARM6 (IMM_ARM6 a 1) a)} = \mbox{STATE_ARM6 (IMM_ARM6 a 1) a} \end{split}
```

Thus, time-consistency can be verified by term rewriting (with appropriate case splitting) using the definitions of STATE_ARM6 and IMM_ARM6, which are in turn defined using NEXT_ARM6, INIT_ARM6 and DUR_ARM6. The cycle zero case can be discharged quite simply: the initialisation map INIT_ARM6 is applied twice on the left hand side and once on the right hand side. The results are equal because the three ISA components do not change during initialisation. The cycle one case requires the next state function to be applied between one to six times. This is because

IMM_ARM6_ONE						
$\vdash \forall a.$	<pre>IMM_ARM6 a 1 = DUR_ARM6</pre>	(INIT_ARM6 a)				

Therefore, the number of cases is primarily dictated by the definition of DUR_ARM6, and these cases are shown in Figure 8. The main branches correspond with the instruction classes and whether a branch (pc-write) occurs. The function NEXT_ARM6 is complex and naïve multi-cycle expansion of the time-consistency goal is impracticable. A number of steps are taken to structure the proof and limit the amount of rewriting, and these are discussed below. HOL is an interactive proof tool and the *goalstack* was used to manage the proof effort.

The overall structure of the (cycle one) proof is as follows:

1. The goal is re-arranged to be of the form:

 $\vdash \forall b. (STATE_ARM6 (DUR_ARM6 (INIT_ARM6 b)) b = a) \Rightarrow (INIT_ARM6 a = a)$

This prevents the state from being evaluated twice i.e. on both sides of the equality. Note that the theorem IMM_ARM6_ONE is also applied.

- 2. The main cases are introduced manually using the Cases_on tactic. Each case provides a context (for the evaluation) in the form of a list of assumptions.
- 3. The bulk of the evaluation is carried out using the *simplifier* tactic ASM_SIMP_TAC. The simplification set (*simpset*) used contains the conversion CBV_CONV, which is in turn given a computation set (*compset*) containing definitions from the specification and this then carries out call-by-value conversion. This provides fast, symbolic execution of the HOL specification.
- 4. The previous stage generates a set of *leaf* goals; these are re-arranged (to undo the first stage) and the initialisation function is applied. Thus, a set of goals of the form $t_1 = t_2$ are produced, where t_1 and t_2 are terms denoting state classes. Each state class is expressed in terms of primitive operations from the specification i.e. the 32-bit word and register/memory access operations. These remaining goals is discharged using the tactic RW_TAC, which is supplied with a set of lemmas. This tactic automatically carries out further case splitting as required.

When evaluating each case (Stage 3), a subset of the definitions from the specification are added to the *compset*. The definitions added are predominantly those listed in Table 12 because these control the flow of instructions through the pipeline. The conversion CBV_CONV is fairly crude as a rewriting engine—it is not really designed as a general purpose rewriting tool and is best suited to evaluating ground terms. Therefore, the execution is carried out in single cycle stages so as to periodically utilize the more general tactic ASM_SIMP_TAC, which will rewrite using the assumption list (context). Trade-offs arise in selecting the set of definitions to rewrite with—a certain amount of experimentation occurred at this point in the proof effort. The aim is to limit the size (and increase readability—for the interactive proof) of terms, and yet at the same time to avoid carrying out superfluous rewriting. Only certain parts of the state space are of real relevance when determining time-consistency. The components of most significance are the memory and the program counter because these determine the state of the pipeline during initialisation. The rewriting is, therefore, structured around evaluating these components.



Figure 8: Manual case splits for the data forwarding ARM6. Without data forwarding the str instruction class does not case split on the decchange; the two cycle case prevails.

In order to speed up the evaluation and increase readability, the tactic ABBREV_TAC is used: see [18]. This tactic replaces all instances of a sub-term in a goal with a variable and an assumption is added asserting the equality of this variable with the sub-term. For example, the program counter and instruction code are represented by the variables pc and i. This is achieved with

ABBREV_TAC 'pc = REG_READ6 reg usr 15'

and

For multi-cycle instruction classes, the sub-term representing the ALU output is abbreviated at the end of each cycle. This greatly reduces term sizes and increases evaluation times: the ALU sub-term is moderately large and occurs repeatedly because the ALU output propagates through the data path and control unit. The precise ALU output is of no significance with regards to time-consistency, and this means that the assumptions for these abbreviations can be discarded eventually.

The lemmas needed at Stage 4 only become apparent having completed Stage 3. It is at this point that large, unreadable terms can be a problem; for these sub-goals must be manually inspected and either: (i) a bug is spotted or (ii) a suitable lemma is constructed. The majority of lemmas that must be proved relate to the semantics of memory/register read and write operations. These operations are based on using the map substitution SUBST, which is defined by

```
\vdash_{def} SUBST m (a,w) b = (if a = b then w else m b)
```

- ∀m d a1 a2 b. ¬ALIGN_EQ a1 a2 ⇒ (MEMREAD (MEM_WRITE b m d a1) a2 = MEMREAD m a2)

This theorem states that if two 32-bit word addresses, a1 and a2, are not equal after word alignment (i.e. when ignoring the two least significant bits) then a write to address a1 may be ignored when reading from address a2. In principle this is a simple theorem to prove, however, a1 and a2 are 32-bit words and the memory is indexed by 30-bit words. Consequently, one must reason about the equality of bit sub-strings. Also, the memory write covers byte and word storage.

REG_WRITE_READ

There is a similar write-read theorem for registers:

```
\vdash ∀r m m2 p n n2.
n < 16 ∧ n2 < 16 ∧ ¬(n = n2) ⇒
(REG_READ6 (REG_WRITE r m n d) m2 n2 = REG_READ6 r m2 n2)
```

Differing numbers (less than sixteen) access different registers, but it is not the case that a mode and number pair uniquely identifies a register. This is because the same register can be accessed in different modes. For example, the program counter is mode invariant. This theorem cannot be generalised for all values of n and n2 because REG_READ6 and REG_WRITE have a peculiar semantics, which is based on the assumption that out-of-bounds indices do not occur. For example:

```
\vdash \forallr. REG_READ6 r usr 16 = REG_READ6 r fiq 8
```

Once n is greater than 31 the register accessed by REG_READ6 is effectively arbitrary. Indices are guaranteed to be in range by virtue of the fact that in use the index is either 14, 15 or a 4-bit field of the instruction code.

The theorems MEM_WRITE_READ and REG_WRITE_READ are used to establish that the pipeline state is consistent after re-initialisation. For example, if a branch or *pc*-write does not occur then ireg takes the value of pipeb as the pipeline shifts along a stage. Thus, ensuring that ireg is consistent involves proving that

⊢ MEMREAD m (REG_READ6 r usr 15 - 0x4) = MEMREAD m' (REG_READ6 r' usr 15 - 0x8)

where m' and r' are the states of the memory and register bank after instruction execution. The right-hand side represents the **ireg** state after re-initialisation and the left-hand side represents the old value of **pipeb** (the new **ireg** value). The terms are equivalent provided that reading the program counter from register bank r' gives an incremented program counter value (i.e. **REG_READ6** r usr 15 + 0x4) and the memory m' is not altered at this new pc location. This is where the two theorems above come into play. Note that it is again necessary to be able to reason about word addition and subtraction. Similar goals have to be verified for the cases in which branches occur.

In essence, time-consistency involves verifying that the initialisation function INIT_ARM6 acts as an invariant, and this entails reasoning about the control logic, in particular the pipeline control logic.

7.2.4 Correctness

The proof of correctness is very similar in structure to the proof of time-consistency. Correctness is reduced to the following goal using the one-step theorem:

 $\vdash (\forall a. STATE_ARM 0 (ABS_ARM6 a) = ABS_ARM6 (STATE_ARM6 (IMM_ARM6 a 0) a)) \land \\ \forall a. STATE_ARM 1 (ABS_ARM6 a) = ABS_ARM6 (STATE_ARM6 (IMM_ARM6 a 1) a)$

The cycle zero case is trivial to prove. The main cases for cycle one are those of Figure 8 but a few more cases are introduced at the leaves. Stage 1 of the time-consistency proof (re-arranging the goal) is not necessary because sub-terms are not repeated in the left and right hand sides of the correctness goal. The leaf goals are ISA state equivalences, with the primitive operations being word operations and read and write operations performed on the three state components: memory, registers and the program status registers. More definitions must be added to the evaluation *compset* because is now necessary to consider data aspects of the design i.e. the shifter and ALU units must be evaluated. Additional lemmas are needed to discharge the leaf goals. The state components are effectively reduced into a canonical form in order to establish their equivalence. For example, with registers the following two lemmas are used:

```
      REG_WRITE_WRITE and REG_WRITE_COMMUTES

      ⊢ ∀r m n d d2. REG_WRITE (REG_WRITE r m n d) m n d2 = REG_WRITE r m n d2

      ⊢ ∀r m1 m2 n n2 d d2.

      n < 16 ∧ n2 < 16 ∧ ¬(n = n2) ⇒</td>

      (REG_WRITE (REG_WRITE r m1 n2 d2) m2 n d = REG_WRITE (REG_WRITE r m2 n d) m1 n2 d2)
```

The second of these two lemmas in used with n2 specialised to fifteen; this enables multiple program counter updates to be reduced to a single write. A series of lemmas are needed to equate operations performed on the program counter. For example:

 \vdash \forall r m d. INC_PC (SUB8_PC (REG_WRITE r m 15 d)) = SUB8_PC (REG_WRITE r m 15 (d + 0x4))

Again, word arithmetic is needed in order to verify this theorem.

Various other lemmas were required to deal with some of the data manipulations performed by the ARM6. For example, the following lemma was needed to verify the load and swap instructions:

 $\vdash \forall$ hla. w32 (SLICEw hla) #>> l = w32 (BITSw hla)

This theorem is needed to reason about reading a byte from memory. In the ISA specification the required byte is simply selected using the BITSw function, whereas in the ARM6 the fieldextractor selects the required byte (keeping it in place) using SLICEw and this word is then rotated using the shifter. The operations BITSw, SLICEw and #>> (rotate right) are defined in terms of natural number division, mod, and addition. In practice, verifying results about these operation is often tedious to do in HOL. Having a well developed and extensive library of word theorems is clearly of great benefit here. Of course, there is always a temptation to cheat when such theorems are required. The ISA specification could have been modified (in a number of instances) to correspond with MA functionality. With the theorem above, logical shift right could have been used instead of rotate right: this would give the same result and be easier to verify in HOL. However, this path was resisted: the ISA remains abstract and the MA is true to the implementation. Verifying tricky word theorems is an important part of the formal verification. These proof obligations do not arise, as one might expect, through verifying the data aspects of the ISA (for example, when looking at the result of a data processing instruction) because here the operations performed are identical at both levels of abstraction. Instead, they are a consequence of relating the disparate ways in which the two level of abstraction (ISA and MA) make use of data operations in the course of instruction execution. At the ISA level succinctness and a clean presentation is important, whereas at the MA level physical organisation comes into play.

8 Summary and Future Work

The ARM6 micro-architecture has been modelled and formally verified in HOL. The processor's organisation is relatively simple, consisting of a three stage pipeline with multi-cycle execution. Nevertheless, formal verification is not trivial and subtle correctness issues must be considered. In particular, it remains to find the best methods to deal with (incorporate into the algebraic framework) implementation dependent behaviour i.e. the instruction flow (self-modifying code), exceptions and unpredictable instructions. It should not be necessary to modify the ISA specification or the MA implementation in a manner inconsistent with the spirit of the ARM references. Rather the correctness model should be adapted to reflect fully what is meant by correctness in the context of processor dependent behaviour. It has been demonstrated that the abstract definition of correctness presented in Section 3 is extensively suitable for ARM6 correctness. Furthermore, verification with the one-step theorems was shown to be a good approach: the initialisation function has a straightforward definition and it was not necessary to explicitly use an invariant.

It is clear that carrying out complete verifications of commercial micro-processors requires well developed tools and a good methodology. The HOL theorem prover enables one to:

- Formalise the abstract correctness model and one-step theorems.
- Model the ISA and MA in a concise manner.
- Carry out fast execution (for testing and verification) using CBV_CONV.
- Reason about word arithmetic and logic.
- Provide well structured proofs with the use of lemmas.

One of the disadvantages of using HOL is that the proof is not fully automated. Human interaction and expertise is required for the verification: one must manually direct the proof effort, spot bugs and supply necessary lemmas. However, it is worth noting that the structure of the main proofs are simple (case splitting, evaluation and application of lemmas) and the lemmas to be proved are not mathematically deep (equating memory substitutions). Therefore, for a given architecture, a library of theorems can be developed, which gives great potential for re-use and semi-automation. The structure of the proof varies little with similar designs. For example, the data forwarding version of the design was verified relatively quickly after completing the no-clobber version.

It is also of great advantage to be able to formalise and reason about correctness in an abstract setting. In this way, different implementations can be related by virtue of conforming with the same correctness condition. There is, therefore, no ambiguity as to precisely what is meant by correctness from one verification to the next. One correctness condition is not sufficient for all circumstances (for example, variants arise when one considers input, output, superscalar designs, error states and non-determinism), but it is clearly advantageous to develop a small family of correctness statements designed for microprocessor verification. It could be argued that the modifications made to the ARM6 implementations (the no-clobber and data forwarding versions) are an artifact of an over prescriptive correctness definition. Equally, one could also take the line that ARM should have taken a more purist and formal line with the ARM architecture i.e. stipulate that the program counter should always correspond with the address (in memory) of the instruction to be executed (and this relationship should be maintained throughout the course of instruction execution). The actual ARM6 violates this condition in two ways: (i) the instruction being executed is from the address pc-0x8; and (ii) it can execute an instruction that has been over-written in memory. In other words, ideally the ISA should be wholly implementation (pipeline) independent and each processor should be designed accordingly. However, it should be possible to modify our definition of correctness to more closely correspond with ARM's approach.

The formal verification brought about proof obligations in which the semantics of word operations was of importance. In particular, it was necessary to reason about 32-bit addition, subtraction and bit rotation, as well as bit field manipulations (extraction and concatenation). A HOL theory of bits and words was developed during the course of the verification and this theory should facilitate further specification and verification work (even outside the domain of processor verification). The word theory was developed with the ARM in mind, and so there is scope for extending the library with additional theorems and operations.

The verification was carried out on a modest desktop PC (800MHz) and processing power was not found to be a *major* problem. During testing the ISA could be executed at a rate of one or two instructions per second, and the MA took up to ten seconds per instruction. This

is adequate for small scale testing and evaluation. The computation time for the verification is dominated by the time-consistency and correctness proofs; these involved approximately two and three million primitive HOL inferences respectively. The total CPU time for these two proofs was approximately fourteen minutes. However, using CBV_CONV in a proof is not as straightforward as it might be and a bespoke tactic for fast contextual evaluation would be beneficial. Were further instruction classes to be included (for example, the multiple data transfers) then the existing proof of correctness (for the instructions covered in this report) would be slowed due to the overhead of executing a more complex specification. The new instruction class would also have to be verified. The overall proof complexity is proportional to the number of instruction classes (because this primarily determines the number of cases) and so pipelined processor verifications of this nature appear to be quite tractable. The proof script was split into two main files: about 800 lines of lemmas and a thousand lines for the time-consistency and correctness proofs. It is important to find ways to ensure that the proof scripts are fairly small, presentable and hence manageable, otherwise it is all too easy to 'get lost' in the proof.

The ARM6 specification and verification took about six months (one person), with the time being split almost equally between specification and verification. The work on the theory of words represents almost half of the effort. The correctness problems with self-modifying code was identified prior to carrying out the verification. Two bugs were spotted in the course of the verification, but by happenstance they combined in a way that made the design correct—they simply represented an unrealistic implementation and this was rectified.

Future work will focus on the following:

- Changing the definition of correctness to encompass self-modifying code and more advanced memory models.
- Looking ways to deal with unpredictable instructions.
- Incorporating external interrupts.
- Verification of the multiple data transfer instruction class.

Each of these will build upon the existing verification work. In the long term more advanced micro-architectures may be studied and there is potential to look at broader systems level correctness concerns, for example: bus protocols and multi-processor systems.

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A The Data Path Specification

A.1 The Memory Interface

```
\vdash_{def} AREG ic is ireg aregn inc reg15 aluout =
           if (is = t4) \land (ic = reg_shift) then
               if
                 (¬BITw 24 ireg ∨ BITw 23 ireg) ∧ (BITSw 15 12 ireg = 15)
               then
                 aluout
               else
                 reg15
           else
               if (is = t4) \land ((ic = ldr) \lor (ic = str)) then
                   if
                     (¬BITw 24 ireg \lor BITw 21 ireg) \land (BITSw 19 16 ireg = 15)
                  then
                     aluout
                  else
                     reg15
               else
                  if (is = t5) \land (ic = ldr) \lor (is = t6) \land (ic = swp) then
                     (if BITSw 15 12 ireg = 15 then aluout else reg15)
                  else
                      if
                         (is = t3) \wedge
                         ((ic = data_proc) \wedge (¬BITw 24 ireg \vee BITw 23 ireg) \wedge
                          (BITSw 15 12 ireg = 15) V
                          (ic = mrs_msr) \land \negBITw 21 ireg \land
                          (BITSw 15 12 ireg = 15) \lor (ic = ldr) \lor (ic = str) \lor
                          (ic = br)) \lor (ic = swp)
                      then
                         aluout
                      else
                          if (is = t3) \land (ic = swi_ex) then
                            w32 (aregn * 4)
                          else
                            inc
\vdash_{\mathit{def}} \texttt{AREGN1} \texttt{ intstart} = \texttt{if intstart then 1 else 2}
\vdash_{def} DIN ic is ireg data =
          if ((ic = ldr) \lor (ic = swp)) \land (is = t4) then data else ireg
\vdash_{def} DINWRITE ic is = \neg((ic = swp) \land (is = t5))
\vdash_{def} NBW ic is ireg =
          \neg(BITw 2^{-2} ireg \land
             ((is = t3) \land ((ic = ldr) \lor (ic = str) \lor (ic = swp)) \lor
             (is = t4) \land (ic = swp)))
\vdash_{\mathit{def}} NRW ic is = (is = t3) \land (ic = str) \lor (is = t4) \land (ic = swp)
```

- See Section 6.1.2, page 17. These functions are listed in Table 3.
- AREGN1 only has two cases: software interrupt or undefined instruction.
- NBW evaluates true for word access and false for byte access.
- NRW evaluates true for memory write and false for memory read.

A.2 The Field Extractor/Extender

```
\vdash_{\mathit{def}} FIELD ic is ireg oareg din =
         if is = t3 then
           if ic = br then
              SIGN_EX_OFFSET (BITSw 23 0 din)
           else
              if (ic = ldr) \lor (ic = str) then
                w32 (BITSw 11 0 din)
              else
                if (ic = mrs_msr) \lor (ic = data_proc) then
                  w32 (BITSw 7 0 din)
                else
                  ARB
         else
           if (is = t5) \wedge (ic = ldr) \vee (is = t6) \wedge (ic = swp) then
              if \neg BITw 22 ireg then
                din
              else
                w32 (SLICEw (8 * oareg + 7) (8 * oareg) din)
            else
              ARB
```

- See Section 6.1.3, page 17.
- The function SIGN_EX_OFFSET is defined in [13].
- oareg is required to be ≤ 3 , and hence the application of slice selects a byte. This can implemented quite simply, without the need for the addition or multiplication.

A.3 The General Purpose Registers

```
\vdash_{def} PCWA ic is ireg =
          (is = t3) \wedge
          (\neg(ic = data_proc) \lor (BITSw 24 23 ireg = 2) \lor
           \neg\,(\texttt{BITSw}\ 15\ 12\ \texttt{ireg} = 15)) \wedge
          (¬(ic = mrs_msr) \lor BITw 21 ireg \lor ¬(BITSw 15 12 ireg = 15)) \land
          \neg(ic = undef) \lor (ic = br) \lor (ic = swi_ex)
\vdash_{def} RAA ic is ireg =
           if is = t3 then
              if (ic = data_proc) \lor (ic = ldr) \lor (ic = str) then
                 BITSw 19 16 ireg
               else
                  if ic = reg_shift then
                    BITSw 11 8 ireg
                  else
                      if (ic = br) \lor (ic = swi_ex) then 15 else ARB
           else
              if (is = t4) \wedge (ic = reg_shift) then
                 BITSw 19 16 ireg
               else
                 ARB
\vdash_{def} RBA ic is ireg =
          if
             (is = t3) ∧
             ((ic = data_proc) \lor (ic = mrs_msr) \lor (ic = ldr) \lor
              (ic = str)) \vee (is = t4) \wedge (ic = reg_shift) \vee
             (is = t5) \land (ic = swp)
           then
             BITSw 3 0 ireg
           else
              if (is = t3) \land (ic = swp) then
                 BITSw 19 16 ireg
               else
                  if (is = t4) \land (ic = str) then
                    BITSw 15 12 ireg
                  else
                      if (is = t5) \land ((ic = br) \lor (ic = swi_ex)) then
                        14
                      else
                        ARB
\vdash_{def} RWA ic is ireg =
           if
             ((is = t3) \land (ic = data_proc) \lor
              (is = t4) \land (ic = reg_shift)) \land
             (¬BITw 24 ireg ∨ BITw 23 ireg) ∨
             (is = t3) \wedge (ic = mrs_msr) \wedge \neg \texttt{BITw} 21 ireg \lor
             (is = t5) \land (ic = ldr) \lor (is = t6) \land (ic = swp)
           then
             (T,BITSw 15 12 ireg)
           else
              if
                 (is = t4) \land ((ic = ldr) \lor (ic = str)) \land
                 (¬BITw 24 ireg \lor BITw 21 ireg)
               then
                 (T,BITSw 19 16 ireg)
               else
                  if
                    ((is = t4) \lor (is = t5)) \land
                     ((ic = br) \land BITw 24 ireg \lor (ic = swi_ex))
                  then
                    (T.14)
                  else
                    (F,ARB)
```

Notes:

• See Section 6.1.4, page 18. These functions are listed in Table 4.

- **PCWA** evaluates true when the program counter takes the value of the incremented address register.
- RAA and RBA give values in the range 0–15, or the value is unspecified (ARB).
- RWA gives a pair: the fist component is true when a register is to take the value of the ALU output; the second component is the index of the destination register, which is a number in the range 0–15.

A.4 The Program Status Registers

 $\vdash_{def} PSRA$ ic is ireg =

```
(is = t3) ∧
          ((ic = swi_ex) \lor
           \negBITw 22 ireg \land
           ((ic = mrs_msr) \lor (ic = data_proc) \land \negBITw 20 ireg)) \lor
          (is = t4) \land \negBITw 22 ireg \land (ic = reg_shift) \land \negBITw 20 ireg
\vdash_{def} PSRDAT ic is ireg nbs aregn cpsrl psrfb alu sctlc =
         if
            BITw 20 ireg \wedge
            ((is = t3) \land (ic = data_proc) \lor (is = t4) \land (ic = reg_shift))
          then
            if BITSw 15 12 ireg = 15 then
              if USER nbs then cpsrl else psrfb
            else
              (let (n,z,c,v) = NZCV alu in
                  if
                    \negBITw 23 ireg \land \negBITw 22 ireg \lor
                    BITw 24 ireg \land BITw 23 ireg
                  then
                   SET_NZC n z sctlc cpsrl
                  else
                    SET_NZCV n z c v cpsrl)
         else
            if (is = t3) \wedge (ic = mrs_msr) then
              if USER nbs then
                if \neg\texttt{BITw}\ 22 ireg \wedge\ \texttt{BITw}\ 19 ireg then
                   w32 (SLICEw 31 28 (ALUOUT alu) + BITSw 27 0 psrfb)
                else
                   ARB
              else
                if BITw 19 ireg then
                   if BITw 16 ireg then
                     w32
                       (SLICEw 31 28 (ALUOUT alu) + SLICEw 27 8 psrfb +
                        BITSw 7 0 (ALUOUT alu))
                   else
                     w32 (SLICEw 31 28 (ALUOUT alu) + BITSw 27 0 psrfb)
                else
                   if BITw 16 ireg then
                     w32 (SLICEw 31 8 psrfb + BITSw 7 0 (ALUOUT alu))
                   else
                     ARB
            else
              if (is = t3) \wedge (ic = swi_ex) then
                SET_IFMODE T ((aregn = 0) \lor (aregn = 7) \lor BITw 6 cpsrl)
                   (exception2mode (num2exception aregn)) cpsrl
              else
                if (is = t4) \wedge (ic = swi_ex) then psrfb else ARB
\vdash_{def} PSRFBWRITE ic is = \neg((is = t4) \land (ic = swi_ex))
\vdash_{def} PSRWA ic is ireg nbs =
         if
            BITw 20 ireg \wedge
            ((is = t3) \wedge (ic = data_proc) \vee
             (is = t4) \land (ic = reg_shift)) \lor (is = t3) \land (ic = swi_ex)
         then
            (T,T)
         else
            if (is = t3) \land (ic = mrs_msr) then
              if
                ¬BITw 21 ireg \vee ¬BITw 19 ireg \wedge ¬BITw 16 ireg \vee
                USER nbs \wedge (BITw 22 ireg \vee \neg \text{BITw} 19 ireg \wedge BITw 16 ireg)
              then
                (F,ARB)
              else
                (T,¬BITw 22 ireg)
            else
              if (is = t4) \wedge (ic = swi_ex) then (T,F) else (F,ARB)
```

```
Hef exception2mode e =
    case e of
    reset → svc
    undefined → und
    software → svc
    address → svc
    pabort → abt
    dabort → abt
    interrupt → irq
    fast → fiq
```

- See Section 6.1.5, page 18. These functions are listed in Table 5.
- The functions exception2mode and num2exception are from the modified ISA specification: see Section 5.
- PSRA evaluates true if the CPSR is to be read and false if an SPSR is to be read.
- **nbs** is the current operating mode.
- The functions SET_NZC, SET_NZCV and SET_IFMODE are defined in [13].
- alu is a 5-tuple, and the functions NZCV and ALUOUT are used to extract the status flags and output word respectively.
- PSRWA gives a pair: the first component is true when a PSR is to be updated; the second component is true for CPSR update and false for SPSR update.

A.5 The Data Buses and Shifter

```
\vdash_{def} BUSA ic is psrrd ra =
         if is = t3 then
            if ic = mrs_msr then
              psrrd
            else
              if
                (ic = data_proc) \lor (ic = ldr) \lor (ic = str) \lor (ic = br) \lor
                (ic = swi_ex)
              then
                ra
              else
                ARB
         else
            if (is = t4) \land (ic = reg_shift) then
              ra
            else
              if (is = t5) \land ((ic = br) \lor (ic = swi_ex)) then
                0x3
              else
                ARB
\vdash_{def} BUSB ic is ireg din' rb =
         if
            (is = t3) ∧
            ((ic = br) \lor
             BITw 25 ireg \land ((ic = data_proc) \lor (ic = mrs_msr)) \lor
             \negBITw 25 ireg \land ((ic = ldr) \lor (ic = str))) \lor
            (is = t5) \land (ic = ldr) \lor (is = t6) \land (ic = swp)
         then
            din'
         else
           rb
\vdash_{def} SCTRLREGWRITE ic is = (is = t3) \land (ic = reg_shift)
\vdash_{def} SHIFTER ic is ireg oareg sctrlreg busb c =
         if is = t3 then
            if BITw 25 ireg \wedge ((ic = data_proc) \vee (ic = mrs_msr)) then
              ROR busb (2 * BITSw 11 8 ireg) c
            else
              if
                (ic = swp) \lor
                \negBITw 25 ireg \land ((ic = ldr) \lor (ic = str) \lor (ic = mrs_msr))
              then
                LSL busb 0 c
              else
                if
                   \negBITw 25 ireg \land (ic = data_proc) \lor
                  BITw 25 ireg \land ((ic = ldr) \lor (ic = str))
                then
                  SHIFT_IMMEDIATE2 (BITSw 11 7 ireg) (BITSw 6 5 ireg) busb c
                else
                  if ic = br then LSL busb 2 c else ARB
         else
            if (is = t4) \wedge (ic = reg_shift) then
              SHIFT_REGISTER2 (BITSw 7 0 sctrlreg) (BITSw 6 5 ireg) busb c
            else
              if (is = t5) \wedge (ic = ldr) \vee (is = t6) \wedge (ic = swp) then
                ROR busb (8 * oareg) c
              else
                if (is = t5) \land ((ic = br) \lor (ic = swi_ex)) then
                  LSL busb 0 c
                else
                  ARB
```

- See Section 6.1.6, page 18. These functions are listed in Table 6.
- BUSA gives value 0x3 for branches and exceptions, and this is used to compute the link register value (which is NOT 0x3 + pc).

- SHIFTER gives a pair: the first component is the carry out; the second component is the output word.
- The functions LSL, ROR, SHIFT_IMMEDIATE2 and SHIFT_REGISTER2 are taken from the modified ISA specification.
- LSL busb 0 c = (c,busb).

A.6 The ALU

```
\vdash_{def} ALU6 ic is ireg alua alub c =
         if
            (ic = data_proc) \land (is = t3) \lor (ic = reg_shift) \land (is = t4)
         then
            ALU (BITSw 24 21 ireg) alua alub c
         else
            if (ic = mrs_msr) \wedge (is = t3) then
              ALU_logic (if BITw 21 ireg then alub else alua)
            else
              if (ic = ldr) \lor (ic = str) then
                if (is = t3) \wedge \neg BITw 24 ireg then
                  ALU_logic alua
                else
                  if (is = t3) \vee (is = t4) then
                     if BITw 23 ireg then ADD alua alub F else SUB alua alub T
                  else
                    if (is = t5) \land (ic = ldr) then ALU_logic alub else ARB
              else
                if (is = t3) \land (ic = br) then
                  ADD alua alub F
                else
                  if (ic = br) \lor (ic = swi_ex) then
                     if is = t4 then
                      ALU_logic alua
                     else
                      if is = t5 then ADD (NOT alua) alub F else ARB
                  else
                     if ic = swp then ALU_logic alub else ARB
\vdash_{def} ALUAWRITE ic is =
          \neg((is = t4) \land
            ((ic = ldr) \lor (ic = str) \lor (ic = br) \lor (ic = swi_ex)))
\vdash_{def} \texttt{ALUBWRITE} ic is =
         \neg((is = t4) \land ((ic = ldr) \lor (ic = str) \lor (ic = swp)))
```

- See Section 6.1.7, page 19. These functions are listed in Table 7.
- ALU6 gives a 5-tuple (n,z,c,v,aluout).
- The functions ALU, ALU_logic and ADD are defined in [13].

B Pipeline Control Specification

```
\vdash_{def} ABORTINST iregval onewinst ointstart ireg n z c v =
           ¬iregval ∨
           onewinst \wedge \neg\texttt{ointstart} \wedge
            ¬CONDITION_PASSED n z c v (BITSw 31 28 ireg)
\vdash_{def} ALIGN_EQ a b = (WORD_ALIGN a = WORD_ALIGN b)
\vdash_{def} IC abortinst nxtic = (if abortinst then unexec else nxtic)
\vdash_{def} INTSEQ ic is = (ic = undef) \land (is = t3)
\vdash_{def} IREGVAL pipecval pcchange = pipecval \land \neg pcchange
\vdash_{def} IS abortinst nxtis = (if abortinst then ARB else nxtis)
\vdash_{def} \text{NEWINST} ic is intstart =
           intstart \lor (ic = data_proc) \lor (ic = mrs_msr) \lor (ic = unexec) \lor
           ((ic = str) \lor (ic = reg_shift)) \land (is = t4) \lor
           ((ic = ldr) \lor (ic = br) \lor (ic = swi_ex)) \land (is = t5) \lor
           (ic = swp) \land (is = t6)
\vdash_{def} NXTIC intstart newinst ic ireg =
           if intstart then
             swi_ex
           else
             if ¬newinst then ic else DECODE_INST (w2n ireg)
\vdash_{def} NXTIS ic is newinst =
           if newinst then
             t3
           else
             if
                (is = t3) \land
                ((ic = reg_shift) \lor (ic = ldr) \lor (ic = str) \lor (ic = br) \lor
                 (ic = swi_ex) \lor (ic = swp))
              then
                t4
              else
                if
                   (is = t4) ∧
                   ((ic = ldr) \lor (ic = br) \lor (ic = swi_ex) \lor (ic = swp))
                then
                  t.5
                else
                  if (is = t5) \land (ic = swp) then t6 else ARB
\vdash_{def} PCCHANGE rwa = (let (w,a) = rwa in w \land (a = 15))
\vdash_{def} \texttt{PIPEALL} opipebll = opipebll
\vdash_{def} PIPEAVAL pcchange = \negpcchange
\vdash_{def} PIPEAWRITE pipeall = pipeall
\vdash_{def} PIPEBLL newinst ic = newinst \lor (ic = br) \lor (ic = swi_ex)
\vdash_{def} PIPEBWRITE pipebll = pipebll
\vdash_{def} PIPECHANGE areg apipea apipeb =
          ALIGN_EQ areg apipea \lor ALIGN_EQ areg apipeb
\vdash_{def} \texttt{PIPECWRITE} \text{ newinst} = \texttt{newinst}
\vdash_{def} \texttt{PIPESTATAWRITE pipeall pcchange = pipeall \lor pcchange} \vdash_{def} \texttt{PIPESTATBWRITE pipebll pcchange = pipebll \lor pcchange}
\vdash_{def} PIPESTATIREGWRITE newinst pcchange = newinst \lor pcchange
```

Definitions for the data forwarding implementation:

```
\begin{array}{l} \vdash_{def} \texttt{IREGVAL pipecval pcchange decchange =} \\ & \texttt{pipecval} \land \neg(\texttt{pcchange} \lor \texttt{decchange}) \\ \vdash_{def} \texttt{PIPEBWRITE pipebll pipebchange = pipebll } \land \neg\texttt{pipebchange} \\ \vdash_{def} \texttt{PIPECHANGE nrw pcchange areg pipe =} \\ & \texttt{nrw} \land \neg\texttt{pcchange} \land \texttt{ALIGN\_EQ} \texttt{areg pipe} \end{array}
```

- See Section 6.2.3, page 28. These functions are listed in Table 12.
- The functions CONDITION_PASSED, DECODE_INST, WORD_ALIGN and SET_BYTE are taken from the modified ISA specification.

C The Initialisation and Next State Functions

 $\vdash_{def} \text{REG}_{READ6}$ reg mode n = if n = 15 then FETCH_PC reg else REG_READ reg mode n

```
Hedef INIT_ARM6
(ARM6 mem (DP reg psr areg din alua alub)
    (CTRL pipea pipeaval pipeb pipebval ireg iregval apipea apipeb
        ointstart onewinst opipebll nxtic nxtis aregn nbw nrw
        sctrlreg psrfb oareg)) =
    (let pc = REG_READ6 reg usr 15 in
        ARM6 mem (DP reg psr pc (MEMREAD mem (pc - 0x8)) alua alub)
        (CTRL (MEMREAD mem (pc - 0x4)) T (MEMREAD mem (pc - 0x4)) T
        (MEMREAD mem (pc - 0x8)) T (pc - 0x4) (pc - 0x4) F T T
        (DECODE_INST (w2n (MEMREAD mem (pc - 0x8)))) t3 2 nbw F
        sctrlreg psrfb oareg))
```

 \vdash_{def} NEXT_ARM6 = PHASE2 o PHASE1

- See Section 6.3, page 28.
- The function REG_READ6 is used to access registers. This is essentially the same as the ISA function REG_READ but it differs when reading the program counter. The ISA version adds eight to the program counter (to compensate for the pipeline), whereas at the MA level the program counter is naturally running ahead.
- The initialisation function INIT_ARM6 preserves the ISA state components mem, reg and psr.
- The address register **areg** holds the **pc** value (this is the address of the next instruction to be fetched).
- Both the instruction register **ireg** and data-in register **din** holds the current instruction code (from address pc-0x8). This ensures that the field extractor/extender processes the instruction code.
- The pipeline contains the instructions from addresses pc-0x8 and pc-0x4 and these values are flagged as being valid.
- The next instruction sequence is t3 and the next instruction class is the decoding of the instruction register.
- The nrw bit is clear because a memory read (instruction fetch) is going to occur. The nbw bit can have any value because it does not affect memory reads.
- The phase functions are defined in the following sections.

C.1 Version 1 (No-Clobber)

```
\vdash_{def} PHASE1 (ARM6 mem (DP reg psr areg din alua alub)
         (CTRL pipea pipeaval pipeb pipebval ireg iregval apipea apipeb
               ointstart onewinst opipebll nxtic nxtis aregn nbw nrw sctrlreg psrfb oareg)) =
    let cpsr = CPSR_READ psr
    in
    let (n,z,c,v,nbs) = DECODE_PSR cpsr
    in
    let abortinst = ABORTINST iregval onewinst ointstart ireg n z c v
    in
    let ic = IC abortinst nxtic
    and is = IS abortinst nxtis
    in
    let pcwa = PCWA ic is ireg
    and rwa = RWA ic is ireg
    in
    let intseq = INTSEQ ic is
    and pcchange = PCCHANGE rwa
    in
    let newinst = NEWINST ic is intseq
    in
    let pipeall = PIPEALL opipebll
    and pipebll = PIPEBLL newinst ic
    and pipec = if PIPECWRITE newinst then pipeb else ireg
    and pipecval = pipebval
    in
    let psrrd = if PSRA ic is ireg then cpsr else SPSR_READ psr nbs
    in
    let psrfb' = if PSRFBWRITE ic is then psrrd else psrfb
    in
    let raa = RAA ic is ireg
    and rba = RBA ic is ireg
    in
    let ra = REG_READ6 reg nbs raa
    and rb = REG_READ6 reg nbs rba
    and din' = FIELD ic is ireg oareg din
    in
    let busa = BUSA ic is psrrd ra
    and busb = BUSB ic is ireg din' rb
    and sctrlreg' = if SCTRLREGWRITE ic is then ra else sctrlreg
    in
    let shifter = SHIFTER ic is ireg oareg sctrlreg busb c
    in
    let shcout = FST shifter
    and shout = SND shifter
    in
    let alua' = if ALUAWRITE ic is then busa else alua
    and alub' = if ALUBWRITE ic is then shout else alub
    in
  (busb,c,shcout,rwa,cpsr,nbs,ic,is,pcwa,pcchange,pipeall,pipec,pipecval,
  ARM6 mem (DP reg psr areg din alua' alub')
    (CTRL pipea pipeaval pipeb pipebval ireg iregval apipea apipeb
       intseq newinst pipebll nxtic nxtis aregn nbw nrw sctrlreg'
       psrfb' oareg))
```

Notes:

• The functions CPSR_READ, SPSR_READ and DECODE_PSR are taken from the ISA specification.

```
\vdash_{def} PHASE2 (busb,c,shcout,rwa,cpsr,nbs,ic,is,pcwa,pcchange,pipeall,pipec,pipecval,
           ARM6 mem (DP reg psr areg din alua alub)
            (CTRL pipea pipeaval pipeb pipebval ireg iregval apipea
               apipeb intseq newinst pipebll nxtic nxtis aregn nbw nrw
               sctrlreg psrfb oareg)) =
    let alu = ALU6 ic is ireg alua alub c
    in
    let aluout = ALUOUT alu
    and inc = areg + 0x4
    and pcbus = REG_READ6 reg usr 15
    and psrwa = PSRWA ic is ireg nbs
    in
    let psrdat = PSRDAT ic is ireg nbs aregn cpsr psrfb alu shcout
    and data = if nrw then ARB else MEMREAD mem areg
    in
    let mem' = if nrw \land (pcchange \lor \neg PIPECHANGE areg apipea apipeb)
                  then MEMWRITE mem busb areg nbw else mem
    and reg' = if pcwa then REG_WRITE reg nbs 15 inc else reg
    and psr' = if FST psrwa then
                  if SND psrwa then CPSR_WRITE psr psrdat else SPSR_WRITE psr nbs psrdat
               else psr
    in
    let reg'' = if FST rwa then REG_WRITE reg' nbs (SND rwa) aluout else reg'
    in
    let oareg' = BITSw 1 0 areg
    and areg' = AREG ic is ireg aregn inc pcbus aluout
    and pipea' = if PIPEAWRITE pipeall then data else pipea
    and apipea' = if PIPEAWRITE pipeall then areg else apipea
    in
    let pipeb' = if PIPEBWRITE pipebll then pipea' else pipeb
    and apipeb' = if PIPEBWRITE pipebll then apipea' else apipeb
    and pipeaval' = if PIPESTATAWRITE pipeall pcchange then PIPEAVAL pcchange else pipeaval
    in
    let pipebval' = if PIPESTATBWRITE pipebll pcchange then pipeaval' else pipebval
    and iregval' = if PIPESTATIREGWRITE newinst pcchange then IREGVAL pipecval pcchange
                                                          else iregval
    in
    let nxtic' = NXTIC intseq newinst ic pipec
    and nxtis' = NXTIS ic is newinst
    and din' = if DINWRITE ic is then DIN ic is pipec data else din
    and aregn' = AREGN1 intseq
    and nbw' = NBW ic is ireg
    and nrw' = NRW ic is
    in
   ARM6 mem' (DP reg'' psr' areg' din' alua alub)
     (CTRL pipea' pipeaval' pipeb' pipebval' pipec iregval' apipea'
        apipeb' intseq newinst pipebll nxtic' nxtis' aregn' nbw' nrw'
        sctrlreg psrfb oareg')
```

- The functions CPSR_WRITE, SPSR_WRITE and REG_WRITE are taken from the ISA specification.
- In order to avoid writing over the pipeline, an extra condition is added to the memory write condition i.e. pcchange $\lor \neg$ PIPECHANGE areg apipea apipeb. Removing this condition would make the specification more faithful to the actual ARM6 behaviour.

C.2 Version 2 (Data Forwarding)

```
\vdash_{def} PHASE1 (ARM6 mem (DP reg psr areg din alua alub)
         (CTRL pipea pipeaval pipeb pipebval ireg iregval apipea apipeb
               ointstart onewinst opipebll nxtic nxtis aregn nbw nrw sctrlreg psrfb oareg)) =
    let cpsr = CPSR_READ psr
    in
    let (n,z,c,v,nbs) = DECODE_PSR cpsr
    in
    let abortinst = ABORTINST iregval onewinst ointstart ireg n z c v
    in
    let ic = IC abortinst nxtic
    and is = IS abortinst nxtis
    in
    let pcwa = PCWA ic is ireg
    and rwa = RWA ic is ireg
    in
    let intseq = INTSEQ ic is
    and pcchange = PCCHANGE rwa
    in
    let pipeachange = PIPECHANGE nrw pcchange areg apipea
    and pipebchange = PIPECHANGE nrw pcchange areg apipeb
    and newinst = NEWINST ic is intseq
    in
    let pipecwrite = PIPECWRITE newinst
    in
    let pipeall = PIPEALL opipebll
    and pipebll = PIPEBLL newinst ic
    and pipec = if pipecwrite then pipeb else ireg
    and pipecval = pipebval
    and decchange = pipecwrite \land pipebchange
    in
    let psrrd = if PSRA ic is ireg then cpsr else SPSR_READ psr nbs
    in
    let psrfb' = if PSRFBWRITE ic is then psrrd else psrfb
    in
    let raa = RAA ic is ireg
    and rba = RBA ic is ireg
    in
    let ra = REG_READ6 reg nbs raa
    and rb = REG_READ6 reg nbs rba
    and din' = FIELD ic is ireg oareg din
    in
    let busa = BUSA ic is psrrd ra
    and busb = BUSB ic is ireg din' rb
    and sctrlreg' = if SCTRLREGWRITE ic is then ra else sctrlreg
    in
    let shifter = SHIFTER ic is ireg oareg sctrlreg busb c
    in
    let shcout = FST shifter
    and shout = SND shifter
    in
    let alua' = if ALUAWRITE ic is then busa else alua
    and alub' = if ALUBWRITE ic is then shout else alub
    in
 (busb,c,shcout,rwa,cpsr,nbs,ic,is,pcwa,pcchange,
  pipeachange,pipebchange,decchange,pipeall,pipec,pipecval,
  ARM6 mem (DP reg psr areg din alua' alub')
    (CTRL pipea pipeaval pipeb pipebval ireg iregval apipea apipeb
       intseq newinst pipebll nxtic nxtis aregn nbw nrw sctrlreg' psrfb' oareg))
```

Notes:

• This definition is similar to that of version 1. In order to implement the data forwarding, three additional values are computed: pipeachange, pipebchange and decchange. The first two are determined by comparing apipea and apipeb with areg (the address of the memory write). The value decchange indicates whether or not pipeb is going to be overwritten in parallel with a decode of the old pipeb.

```
\vdash_{\textit{def}} \texttt{PHASE2} \ (\texttt{busb,c,shcout,rwa,cpsr,nbs,ic,is,pcwa,pcchange,pipeachange,pipebchange,decchange,}
           pipeall, pipec, pipecval, ARM6 mem (DP reg psr areg din alua alub)
              (CTRL pipea pipeaval pipeb pipebval ireg iregval apipea apipeb
                intseq newinst pipebll nxtic nxtis aregn nbw nrw sctrlreg psrfb oareg)) =
    let alu = ALU6 ic is ireg alua alub c
    in
    let aluout = ALUOUT alu
    and inc = areg + 0x4
    and pcbus = \overrightarrow{REG}_READ6 reg usr 15
    and psrwa = PSRWA ic is ireg nbs
    in
    let psrdat = PSRDAT ic is ireg nbs aregn cpsr psrfb alu shcout
    and data = if nrw then ARB else MEMREAD mem areg
    and oareg' = BITSw 1 0 areg
    in
    let areg' = if decchange then apipea else AREG ic is ireg aregn inc pcbus aluout
    and nxtic' = NXTIC intseq newinst ic pipec
    and nxtis' = NXTIS ic is newinst
    and din' = if DINWRITE ic is then DIN ic is pipec data else din
    and aregn' = AREGN1 intseq
    and nbw' = NBW ic is ireg
    and nrw' = NRW ic is
    in
    let mem' = if nrw then MEMWRITE mem busb areg nbw else mem
    and reg' = if decchange then REG_WRITE reg nbs 15 apipea
                else
                  if pcwa then REG_WRITE reg nbs 15 inc else reg
    and psr' = if FST psrwa then
                   if SND psrwa then CPSR_WRITE psr psrdat else SPSR_WRITE psr nbs psrdat
                else psr
    in
    let reg'' = if FST rwa then REG_WRITE reg' nbs (SND rwa) aluout else reg'
    in
    let pipea' = if PIPEAWRITE pipeall then data else
                    if pipeachange then
                      if nbw then busb else SET_BYTE oareg' busb pipea
                    else pipea
    and apipea' = if PIPEAWRITE pipeall then areg else apipea
    in
    let pipeb' = if PIPEBWRITE pipebll decchange then pipea' else
                    if pipebchange then
                      if nbw then busb else SET_BYTE oareg' busb pipeb
                    else pipeb
    and apipeb' = if PIPEBWRITE pipebll decchange then apipea' else apipeb
    and pipeaval' = if PIPESTATAWRITE pipeall pcchange then PIPEAVAL pcchange else pipeaval
    in
    let pipebval' = if PIPESTATBWRITE pipebll pcchange then pipeaval' else pipebval
    and iregval' = if PIPESTATIREGWRITE newinst pcchange then IREGVAL pipecval pcchange decchange
                                                           else iregval
    in
  ARM6 mem' (DP reg'' psr' areg' din' alua alub)
    (CTRL pipea' pipeaval' pipeb' pipebval' pipec iregval' apipea'
       apipeb' intseq newinst pipebll nxtic' nxtis' aregn' nbw' nrw'
       sctrlreg psrfb oareg')
```

- The memory write is restored in accordance with the actual ARM6 behaviour i.e. the pipe change condition is dropped.
- The pipeline behaviour is now more complicated: the **busb** value (to be stored in memory) is conditionally forwarded to **pipea** or **pipeb**. The function **SET_BYTE** (from the ISA specification) is needed to cope with a byte store i.e. the least significant byte of **busb** overwrites a single byte in **pipea** or **pipeb**.
- If decchange is set then the ireg register is flagged as being invalid because pipeb needs to be decoded.

D The Data and Temporal Abstractions

```
\vdash_{def} SUB8_PC reg = SUBST reg (r15, reg r15 - 0x8)
\vdash_{def} ABS\_ARM6 (ARM6 mem (DP reg psr areg din alua alub) ctrl) =
       ARM mem (SUB8_PC reg) psr
\vdash_{def} \texttt{DUR}\_\texttt{ARM6} (ARM6 mem (DP reg psr areg din alua alub)
             (CTRL pipea pipeaval pipeb pipebval ireg iregval apipea apipeb
               ointstart onewinst opipebll nxtic nxtis aregn nbw nrw sctrlreg psrfb oareg)) =
    let (n,z,c,v,nbs) = DECODE_PSR (CPSR_READ psr) in
    let abortinst = ABORTINST iregval onewinst ointstart ireg n z c v in
    let ic = IC abortinst nxtic in
    let pcchange = PCCHANGE (RWA ic t3 ireg)
    in
    if ic = undef then
      Δ
     else
      if (ic = mrs_msr) \lor (ic = data_proc) then
        if pcchange then 3 else 1
       else
         if ic = reg_shift then
            if (BITSw 15 12 ireg = 15) \wedge (¬BITw 24 ireg \vee BITw 23 ireg) then 4 else 2
         else
            if ic = 1dr then
               if (BITSw 15 12 ireg = 15) \lor
                   (BITSw 19 16 ireg = 15) \wedge (¬BITw 24 ireg \vee BITw 21 ireg) then 5 else 3
            else
               if ic = str then
                   if (BITSw 19 16 ireg = 15) \wedge (¬BITw 24 ireg \vee BITw 21 ireg) then 4 else 2
               else
                   if (ic = br) \lor (ic = swi_ex) then
                      3
                    else
                       if ic = swp then
                         if BITSw 15 12 ireg = 15 then 6 else 4
                       else
                         1
\vdash_{def} IMM_ARM6 a O = O \land
    IMM_ARM6 a (SUC t) = DUR_ARM6 (STATE_ARM6 (IMM_ARM6 a t) a) + IMM_ARM6 a t
```

With the data forwarding implementation, the function DUR_ARM6 is refined for the case of store instructions:

```
if ic = str then
    if (BITSw 19 16 ireg = 15) ∧ (¬BITw 24 ireg ∨ BITw 21 ireg) then 4 else
    if (let (Im,P,U,B,W,L,Rn,Rd,offset) = DECODE_LDR_STR (w2n ireg) in
        ALIGN_EQ (FST (ADDR_MODE2 (SUB8_PC reg) nbs c Im P U Rn offset)) apipeb) then 3 else 2
else ...
```

- See Section 7.1, page 31.
- The function SUB8_PC subtracts eight from the program counter and is used in the definition of ABS_ARM6.
- The duration map DUR_ARM6 gives a value based on the instruction class (ic) and whether or not the program counter is a destination register.
- The map DUR_ARM6 is only ever applied to initial cycles i.e. for states part way through the execution of an instruction, it does not determine how many cycles remain.
- The immersion IMM_ARM6 is constructed so as to be uniform with respect to DUR_ARM6 and STATE_ARM6.