

	<i>Introduction rules</i>	<i>Elimination rules</i>
\wedge	<p>...</p> <p><i>l.</i> P from ...</p> <p>...</p> <p><i>m.</i> Q from ...</p> <p>...</p> <p><i>n.</i> $P \wedge Q$ from <i>l</i> and <i>m</i> by \wedge-introduction (it doesn't matter in what order <i>l</i> and <i>m</i> are in)</p>	<p>...</p> <p><i>m.</i> $P \wedge Q$ from ...</p> <p>...</p> <p><i>n.</i> P from <i>m</i> by \wedge-elimination</p> <p>or</p> <p>...</p> <p><i>m.</i> $P \wedge Q$ from ...</p> <p>...</p> <p><i>n.</i> Q from <i>m</i> by \wedge-elimination</p>
\vee	<p>...</p> <p><i>m.</i> P from ...</p> <p>...</p> <p><i>n.</i> $P \vee Q$ from <i>m</i> by \vee-introduction</p> <p>or</p> <p>...</p> <p><i>m.</i> Q from ...</p> <p>...</p> <p><i>n.</i> $P \vee Q$ from <i>m</i> by \vee-introduction</p>	<p><i>l.</i> $P \vee Q$ from ... by ...</p> <div style="border: 1px solid black; padding: 5px; margin-bottom: 5px;"> <p>...</p> <p><i>m</i>₁. Assume P</p> <p>...</p> <p><i>m</i>₂. R</p> <p>...</p> </div> <div style="border: 1px solid black; padding: 5px; margin-bottom: 5px;"> <p>...</p> <p><i>n</i>₁. Assume Q</p> <p>...</p> <p><i>n</i>₂. R</p> <p>...</p> </div> <p><i>o.</i> R from <i>l</i>, <i>m</i>₁-<i>m</i>₂, <i>n</i>₁-<i>n</i>₂ by \vee-elimination (it doesn't matter what order <i>l</i>, <i>m</i>₁-<i>m</i>₂, and <i>n</i>₁-<i>n</i>₂ are in)</p>
\Rightarrow	<div style="border: 1px solid black; padding: 5px; margin-bottom: 5px;"> <p>...</p> <p><i>m.</i> Assume P</p> <p>...</p> <p><i>n.</i> Q from ... by ...</p> <p>...</p> </div> <p><i>n</i> + 1. $P \Rightarrow Q$ from <i>m</i>-<i>n</i>, by \Rightarrow-introduction</p>	<p>...</p> <p><i>l.</i> $P \Rightarrow Q$ by ...</p> <p>...</p> <p><i>m.</i> P by ...</p> <p>...</p> <p><i>n.</i> Q from <i>l</i> and <i>m</i> by \Rightarrow-elimination</p>
\neg	<div style="border: 1px solid black; padding: 5px; margin-bottom: 5px;"> <p>...</p> <p><i>m.</i> Assume P</p> <p>...</p> <p><i>n.</i> F from ... by ...</p> <p>...</p> </div> <p><i>n</i> + 1. $\neg P$ from <i>m</i>-<i>n</i>, by \neg-introduction</p>	<p>...</p> <p><i>l.</i> P by ...</p> <p>...</p> <p><i>m.</i> $\neg P$ by ...</p> <p>...</p> <p><i>n.</i> F from <i>l</i> and <i>m</i> by \neg-elimination</p>
T	<p>...</p> <p><i>n.</i> T</p>	No elimination rule for True.
F	No introduction rule for False.	<p>...</p> <p><i>m.</i> F from ... by ...</p> <p>...</p> <p><i>n.</i> P from <i>m</i>, by F-elimination</p>
\forall	<div style="border: 1px solid black; padding: 5px; margin-bottom: 5px;"> <p>...</p> <p><i>m.</i> Consider an arbitrary x (from domain ...)</p> <p>...</p> <p><i>n.</i> $P(x)$ by ...</p> <p>...</p> </div> <p><i>n</i> + 1. $\forall x.P(x)$ from <i>m</i>-<i>n</i> by \forall-introduction</p>	<p>...</p> <p><i>m.</i> $\forall x.P(x)$ from ...</p> <p>...</p> <p><i>n.</i> $P(v)$ from <i>m</i> by \forall-elimination</p>
\exists	<p>...</p> <p><i>m.</i> $P(v)$</p> <p>...</p> <p><i>n.</i> $\exists x.P(x)$ from <i>m</i> by \exists-introduction with witness $x = v$</p>	<p><i>l.</i> $\exists x.P(x)$</p> <p>...</p> <div style="border: 1px solid black; padding: 5px; margin-bottom: 5px;"> <p><i>m.</i> For some actual x_1, $P(x_1)$</p> <p>...</p> <p><i>n.</i> Q (where x_1 not free in Q)</p> <p>...</p> </div> <p><i>o.</i> Q from <i>l</i>, <i>m</i>-<i>n</i>, by \exists-elimination</p>
	<div style="border: 1px solid black; padding: 5px; margin-bottom: 5px;"> <p>...</p> <p><i>m.</i> Assume $\neg P$</p> <p>...</p> <p><i>n.</i> F from ... by ...</p> <p>...</p> </div> <p><i>n</i> + 1. P from <i>m</i>-<i>n</i>, by contradiction</p> <p style="text-align: right;"><i>(Proof by contradiction)</i></p>	