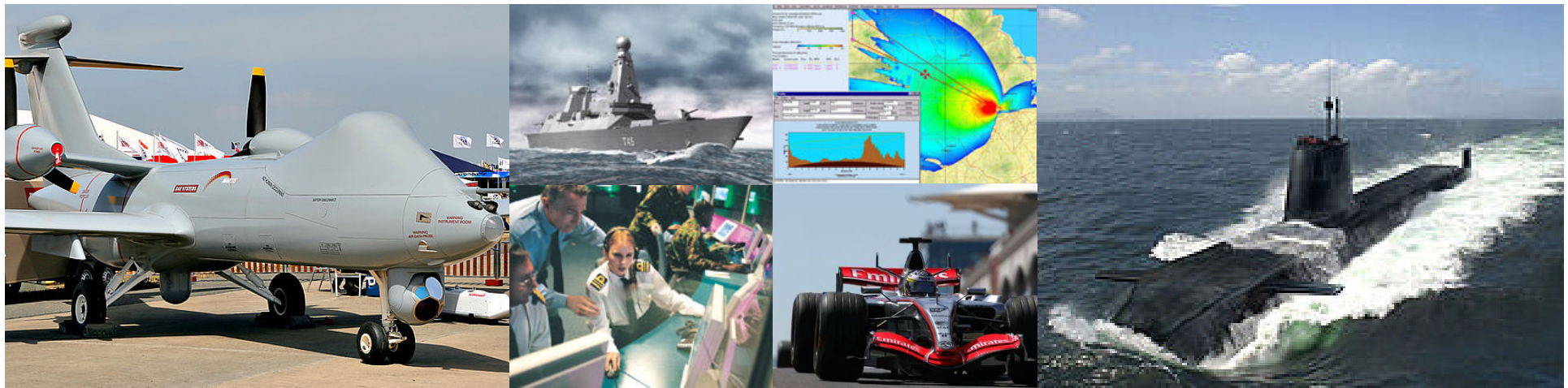


Navigation and Positioning in the 21st Century

Dr Ramsey Faragher, Principal Scientist
BAE Systems Advanced Technology Centre



Overview

- Why navigation is so important
- Why GPS changed the world
- Why GPS isn't enough
- Alternative methods of navigation
- Opportunistic positioning
- The Kalman Filter
- Indoor Positioning

- BAE Systems Advanced Technology Centre

Why is navigation so important?

- The ability to navigate drove animal evolution, by enabling us to
 - Hunt for food
 - Evade predators
 - Find mates
 - Migrate
- We still navigate today for exactly the same reasons!
- Most of our senses are used primarily for long and short range navigation (“sense and attack”, or “sense and avoid”)
 - Sight
 - Sound
 - Smell
 - Touch

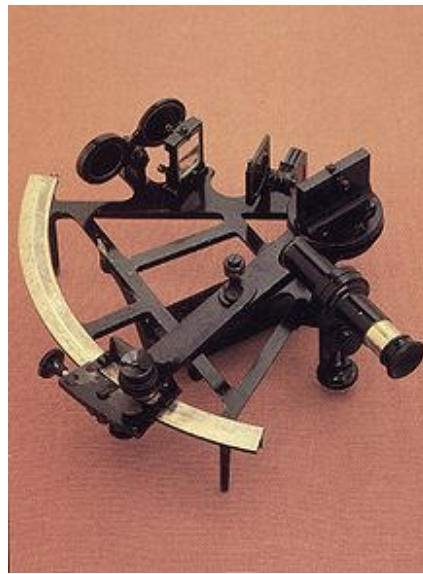
“Extra Sensory” Navigation Timeline

- 1st Century
 - Chinese discover that “loadstone” points North-South
- 8th Century
 - Chinese magnetise needles to fabricate portable compasses
- 11th Century
 - Viking “sunstones” were used to determine the direction of the sun even under cloudy conditions (exploits birefringence in calcite crystals)



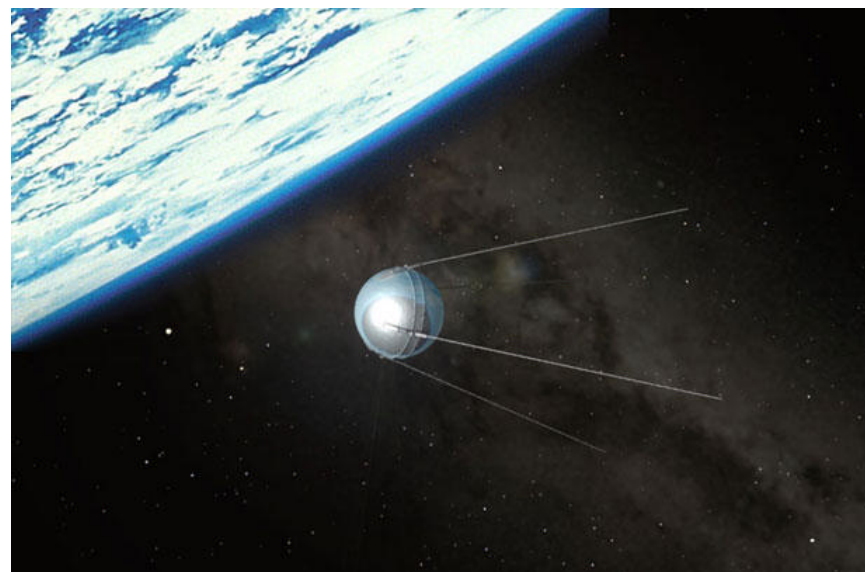
“Extra Sensory” Navigation Timeline

- 15th Century
 - Astrolabes and sextants provide latitude using the elevations of sun or stars
- 18th Century
 - John Harrison creates a chronometer (clock) stable enough to allow longitude to be accurately determined

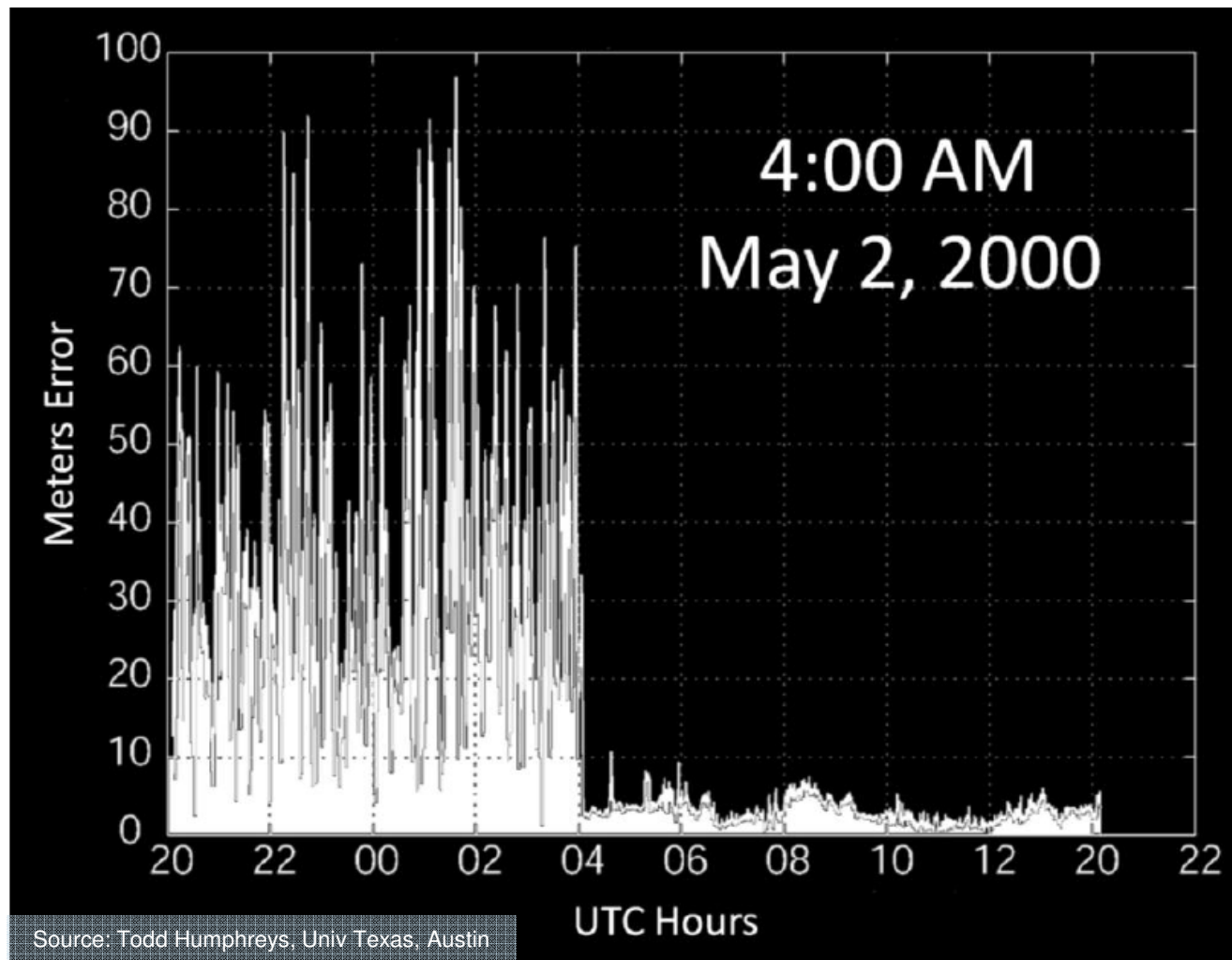


“Extra Sensory” Navigation Timeline

- 1930s
 - The beginnings of radio positioning, with huge advances during WWII
- 1957
 - Artificial satellites pave the way for satellite based, global positioning systems



The day the world changed – 2nd May 2000



The impact of GPS on society

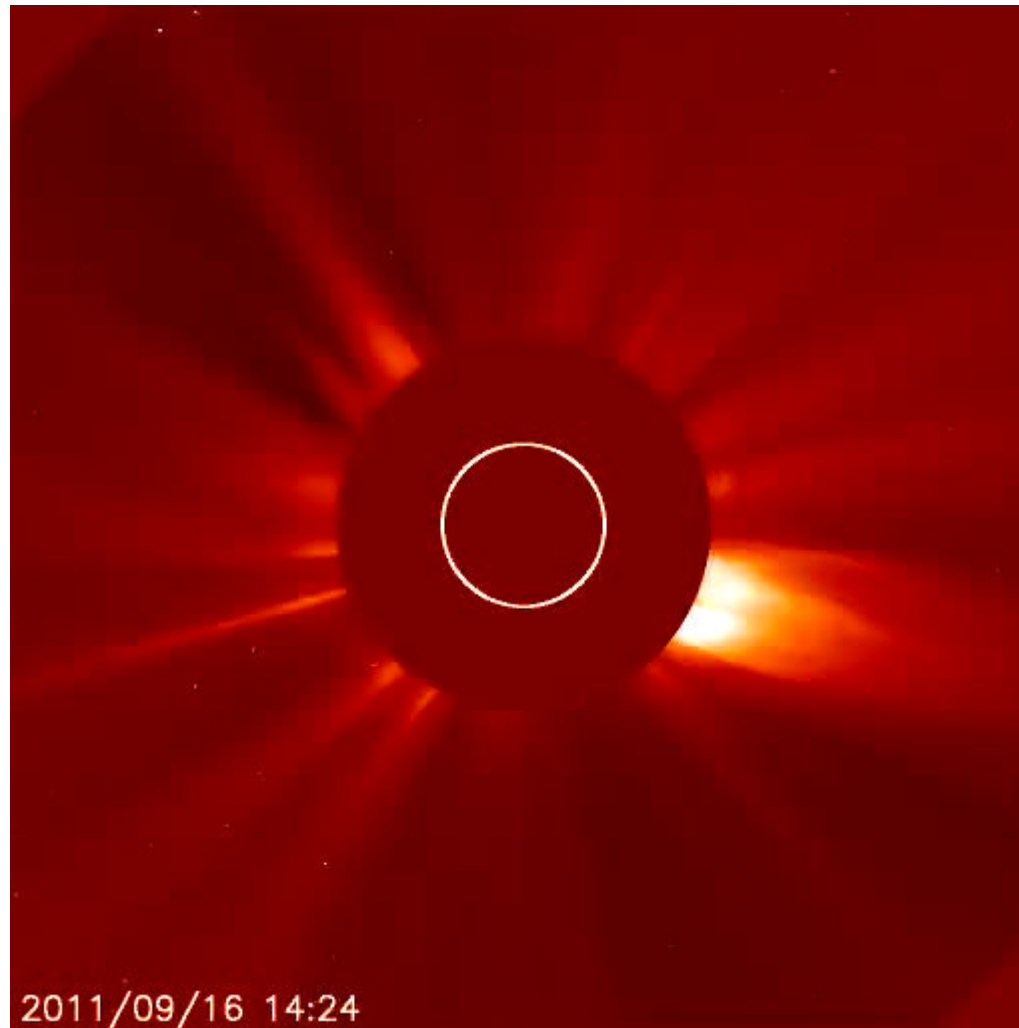
- European Commission estimates that 800 BILLION EURO of the European Economy depends on GPS
- We need it for our
 - Telecommunications and Data Transfer
 - Banking
 - Agriculture
 - Shipping and Air Traffic Control
 - Rail and Road Transport Sector
 - Emergency Services
- Today there are multiple Global Navigation Satellite Systems (GNSS)
 - GPS (USA), GLONASS (Russia), Beidou/Compass (China), Galileo (EU)

Why is GPS not enough?

- The very weak signals (a *quadrillionth* of a Watt at the Earth's surface) can be affected by:
 - Foliage, buildings, power lines, tunnels, etc
 - Electronic interference – malicious or otherwise
 - Space weather, especially during Solar maxima (e.g. 2013)



Coronal Mass Ejections 16/9/11 – 20/9/11



Aurora Australis



Alternative methods of navigation

- Stars and other celestial bodies
- Landmarks
- Magnetic field
- Gravitational field
- Scent
- Weather
- Dead reckoning and inertial navigation
- Sound
- Radio Navigation aids

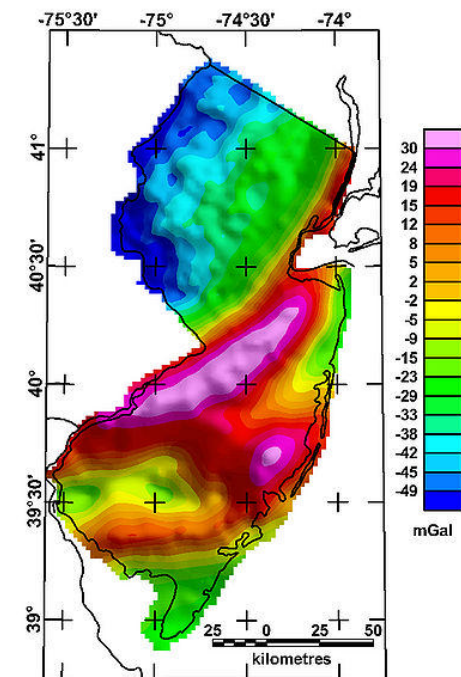
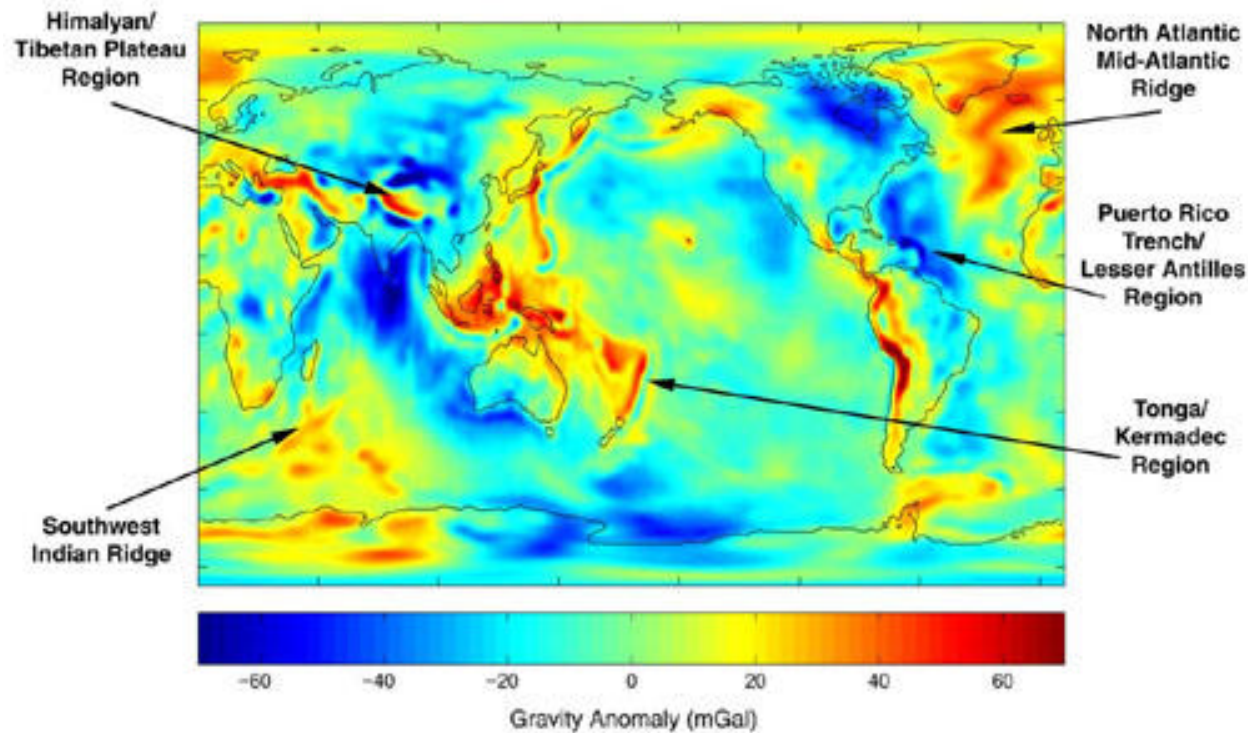
Alternative methods of navigation - Vision

- Stellar cameras
 - Positioning accurate to ~100 metres, precise orientation measurement
 - Requires a stable platform, visibility
- Recognise landmarks and determine relative position
 - Requires databases, significant processing, visibility, etc.
- Visual Odometry
 - Use cameras to infer motion (determine velocity and changes in heading)



Alternative methods of navigation

- Map matching
 - Gravitational/magnetic/photographic/radar/sonar/radio
 - Requires stable maps (slow temporal changes), databases, etc

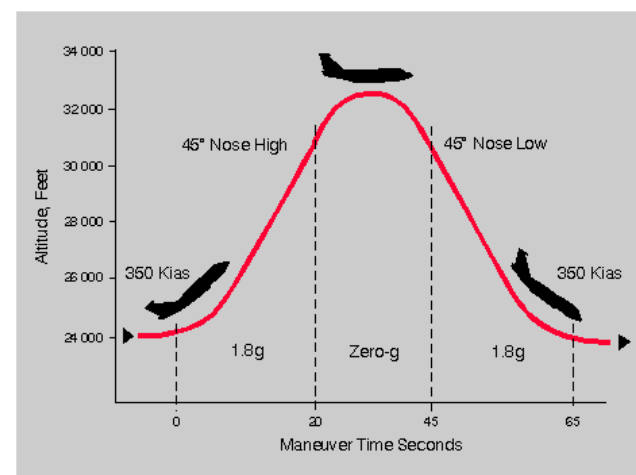


Gravitational Aiding of an Inertial Navigation System

- What is an Inertial Navigation System?
 - Integrate the outputs from accelerometers and gyroscopes over time to determine changes in orientation, velocity, and position
 - Accuracy degrades exponentially with time (integration of errors)
- Gyroscopes
 - Determine orientation changes
- Accelerometers
 - Determine forces acting on the system
 - Integrate acceleration to determine velocity, integrate velocity to determine position
 - Must account for the effect of gravity

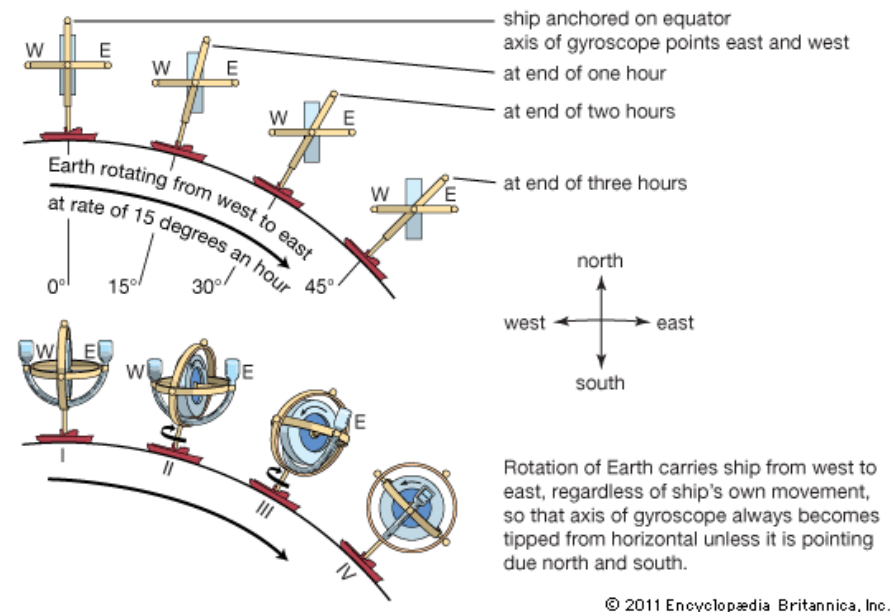
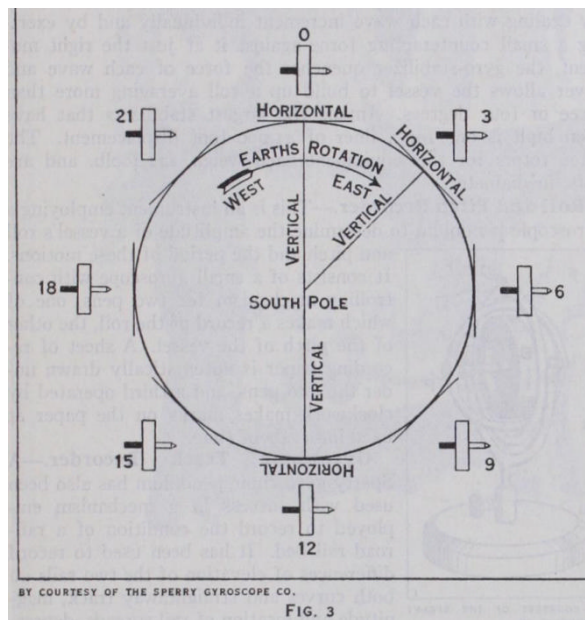
Gravitational Aiding of an Inertial Navigation System

- Effect of gravity on an Inertial Navigation System
 - A free-falling accelerometer measures no force (gravity is accelerating all components downwards equally, so no relative measurement between test mass and sensor frame can be made)
 - *An accelerometer is a device that senses deviation from free fall*
 - A dropped INS cannot record it's motion towards the centre of the Earth unless you add in the force of gravity before integrating



Gravitational Aiding of an Inertial Navigation System

- To add in gravity correctly we need to know which direction is “down”
- Gyroscopes provide orientation relative to the horizon
- However, the rotation of the Earth, and motion over the curved Earth must also be accounted for



The Navigation Equation

Gyro-compensated Accelerometer measurements

System acceleration

$$\mathbf{a}_e^n = \mathbf{b}^n - (2\boldsymbol{\omega}_{ie}^n + \boldsymbol{\omega}_{en}^n) \times \mathbf{v}_e^n + \mathbf{g}_l^n$$

System velocity

Gravity

Effect of rotating Earth

$$\boldsymbol{\omega}_{ie}^n = [\Omega \cos L \quad 0 \quad -\Omega \sin L]^T$$

$$\boldsymbol{\omega}_{en}^n = \begin{bmatrix} \dot{\lambda} \cos L & -\dot{L} & -\dot{\lambda} \sin L \end{bmatrix}^T$$

Longitude

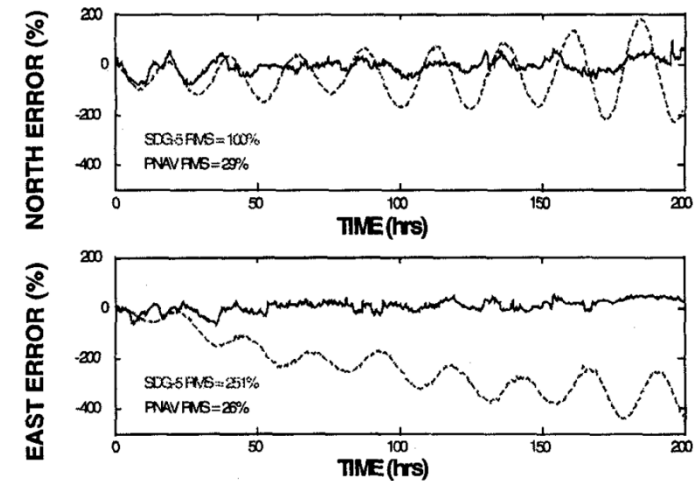
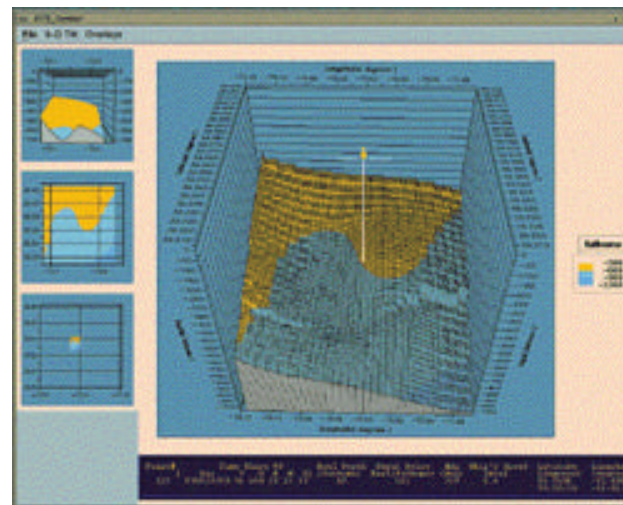
Earth rotation rate

Latitude

Effect of moving over a curved surface

Gravitational Aiding of an Inertial Navigation System

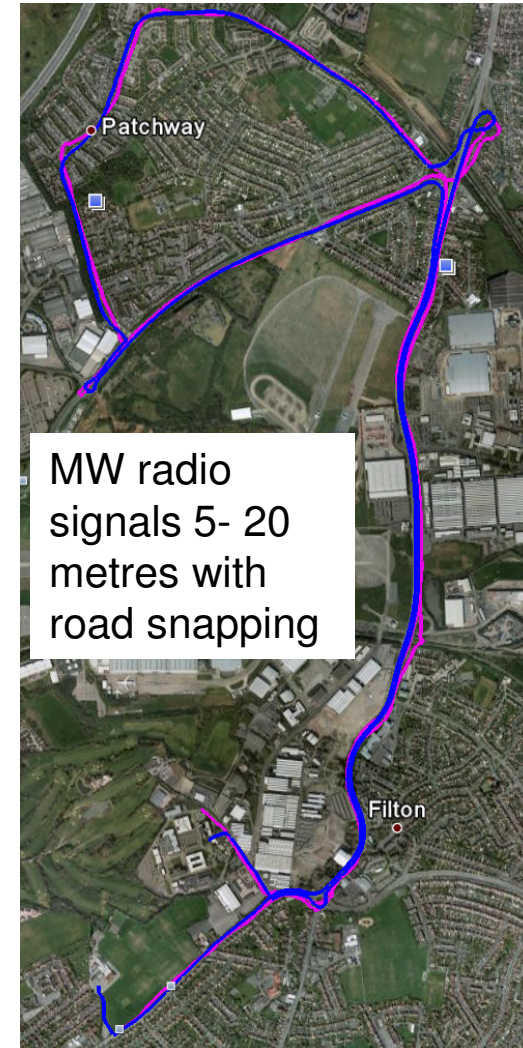
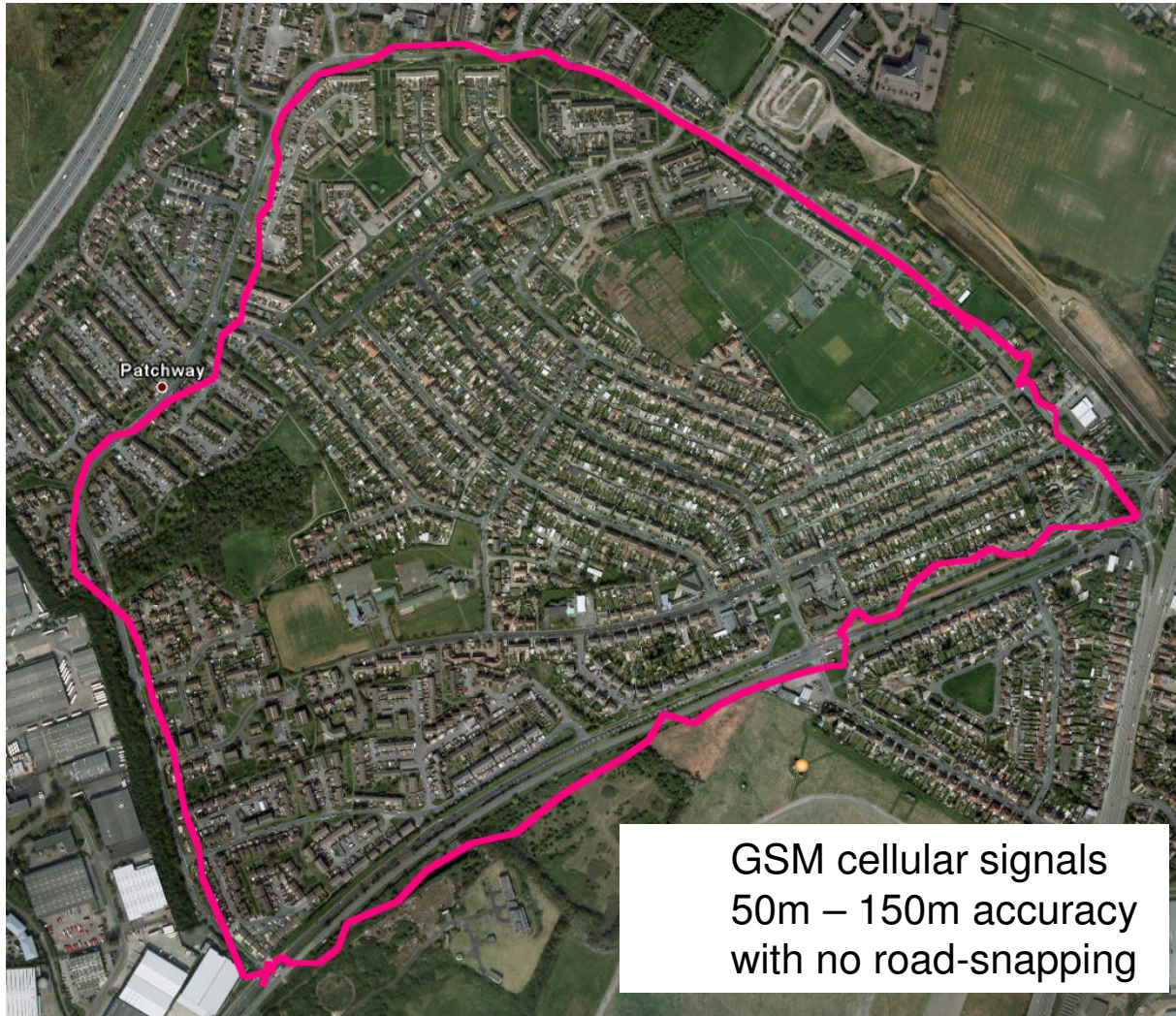
- Gravitational gradiometers and gravimeters :
 - Measurements of gravitational strength and gradient
 - Measurements of vertical Coriolis acceleration
 - Measurements of vertical deflection
 - Provision of passive terrain estimation



Navigation using Opportunistic Radio Signals

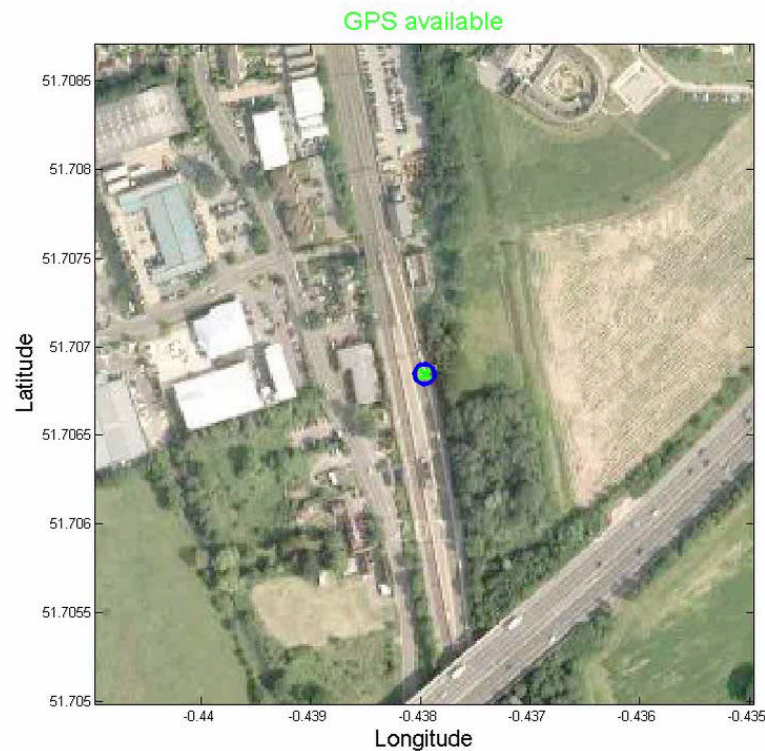
- Advantages
 - High signal availability in populated inland areas
 - 2G cellular, 3G cellular, TV, VHF radio, MW radio, DAB radio, WiFi...
 - Much higher transmission powers than GPS provides better signal penetration
 - GPS = 50W @ 20,200km; Droitwich MW transmitter = 50,000W @ 1-1000km
 - Great range in frequencies (1MHz to 3GHz)
 - Protection against interference
 - Independent propagation characteristics
 - Fusion of multiple signals of different provides integrity monitoring
- Disadvantages
 - The signals are typically not designed for radio positioning
 - Some need a calibration step, and smart navigation filters are required
 - The database of source locations may be unknown
 - Simultaneous Localisation and Mapping allows navigation without prior knowledge of source locations

Navigation using Opportunistic Radio Signals

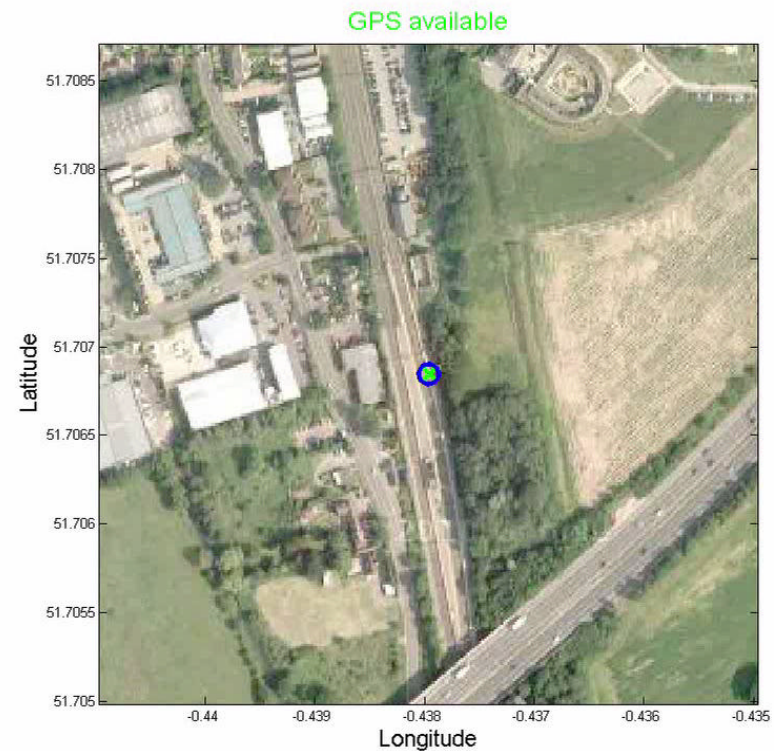


Supporting rail positioning requirements

Tracking using GSM-R with rail snapping



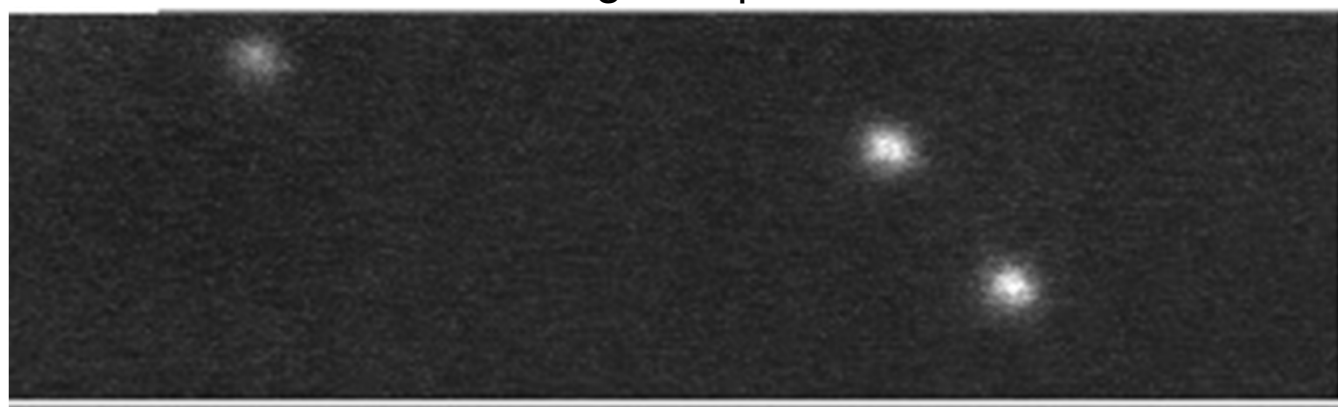
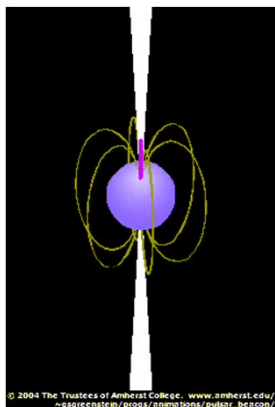
For comparison: Tracking using GSM-R **without** rail snapping



Provides 6m accuracy @ 66% confidence,
12m accuracy @ 95% confidence

Astronomical opportunistic radio positioning

- Utilizing the predictability and stability of Pulsars to navigate in deep space
- A Pulsar is a rotating Neutron Star emitting pulses of EM radiation
 - Matter falling onto the Neutron Star is accelerated through curved paths by the star's powerful magnetic field
 - EM radiation is “beamed” out from the magnetic poles of the stars



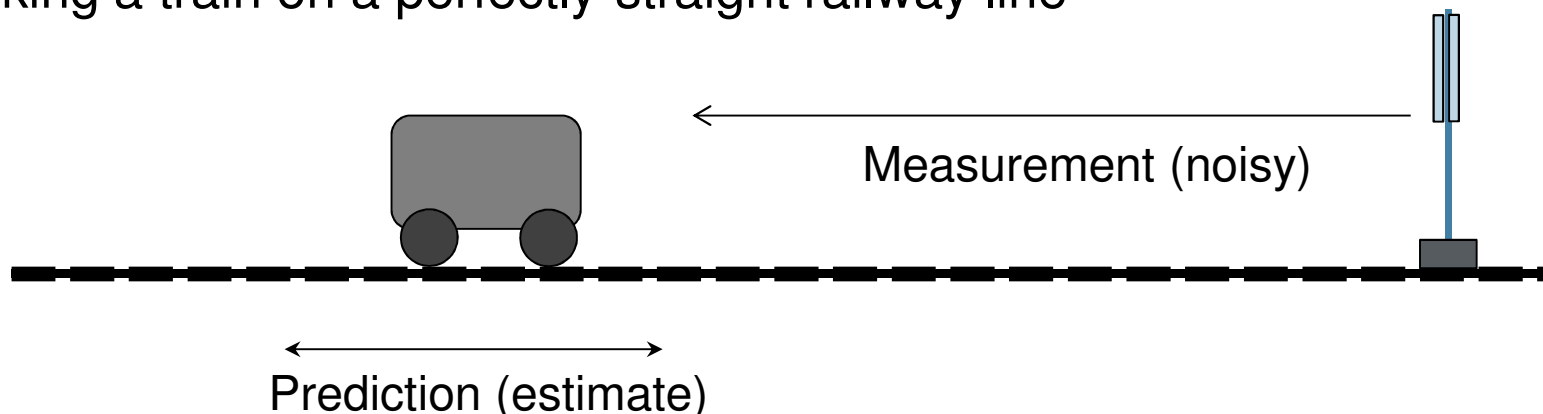
- NASA and ESA are both investigating the use of pulsar navigation to support deep space missions

Fusing data – the Kalman Filter

- The most famous navigation filter – (Rudolph Kalman, 1960)
 - A navigation filter fuses *predictions* based on models or estimates of allowed user movement and *measurements* from available sensors
 - The Kalman filter took Armstrong to the moon – and prevented him from smashing into it!
 - You own at least one Kalman Filter yourself, probably many more.
 - GPS receivers, phase-locked loops in electronic devices, computer games (software and hardware)...

Simple 1-Dimensional navigation problem

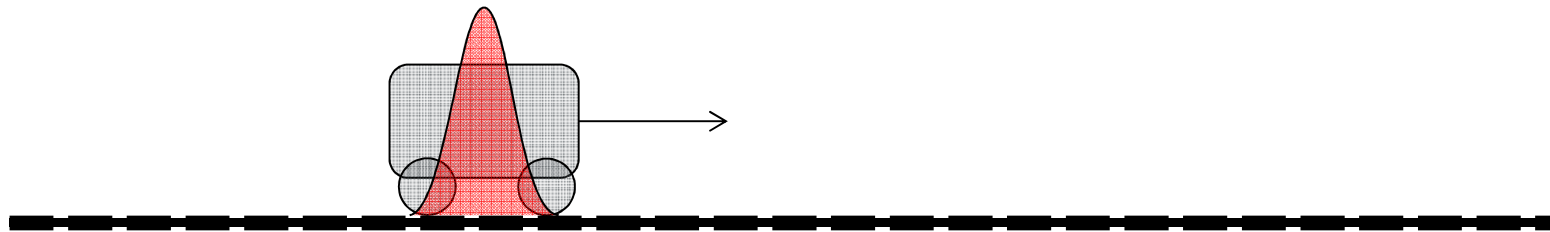
- Tracking a train on a perfectly-straight railway line



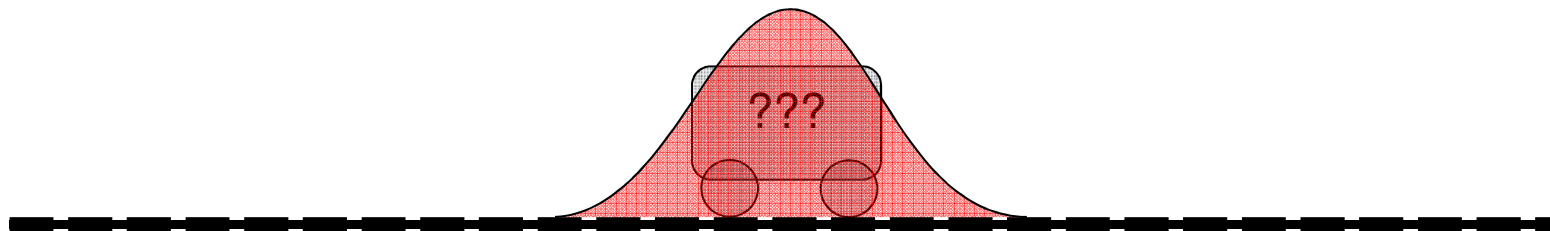
- Estimate change in position of train using control inputs (if available) or simple knowledge (maximum acceleration and deceleration possible, etc)
- Fuse this estimate with the available sensor measurements (in this case a radio ranging measurement) and determine optimum estimate given all available information

Probability framework

- Take last known state of train (position, velocity, braking force, etc)



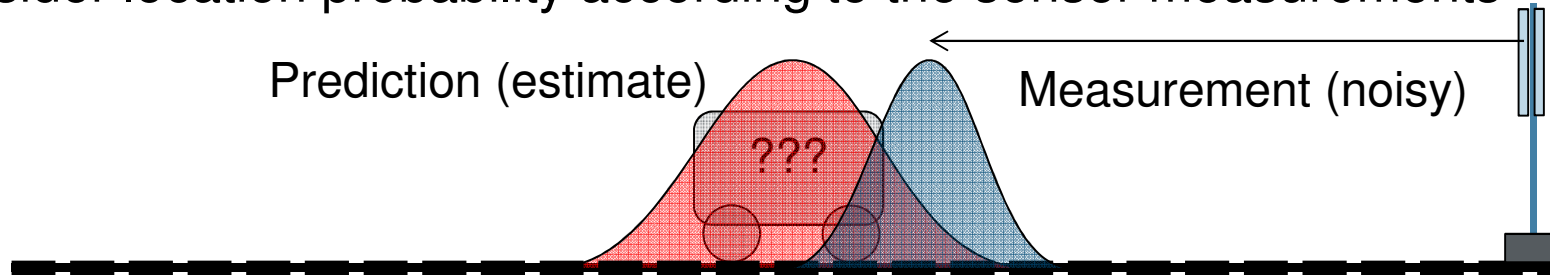
- Make a prediction of where the train is now, accounting that it may have braked or accelerated in the intervening period



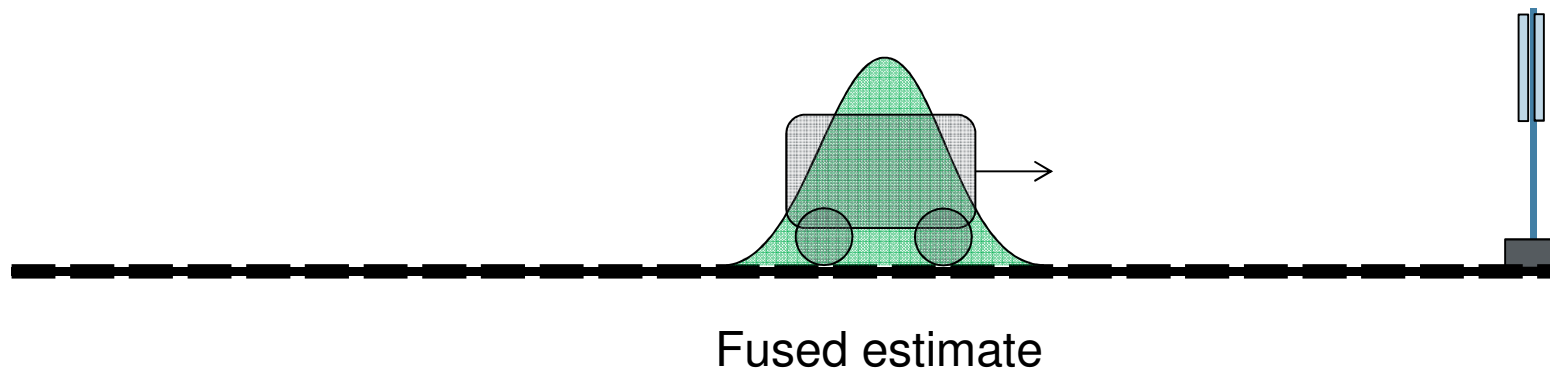
Prediction (estimate)

Probability framework

- Consider location probability according to the sensor measurements



- Combine probability density functions to provide optimal estimate



Deriving Kalman's Filter as the product of two Gaussians

$$x_1(r) \triangleq \frac{1}{\sqrt{2\pi\sigma_1^2}} e^{-\frac{(r-\mu_1)^2}{2\sigma_1^2}}$$

$$x_2(r) \triangleq \frac{1}{\sqrt{2\pi\sigma_2^2}} e^{-\frac{(r-\mu_2)^2}{2\sigma_2^2}}$$

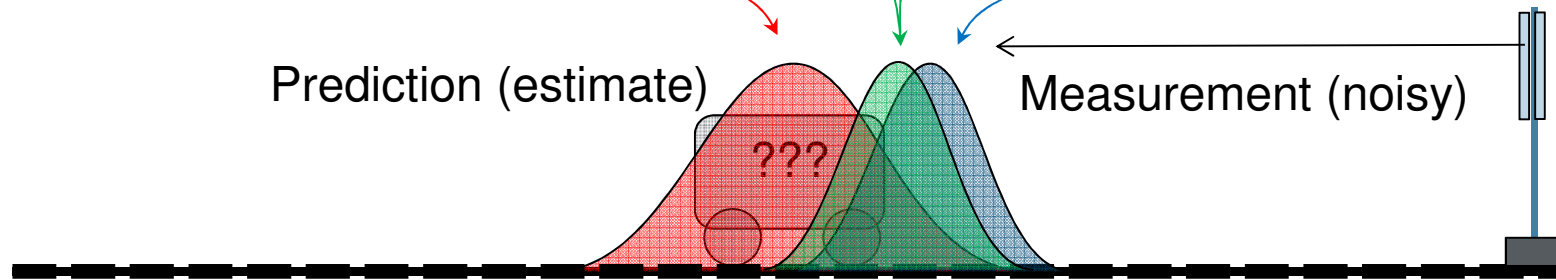
Mean and variance of the new Gaussian given by the product of x_1 and x_2

$$\mu = \frac{\mu_1\sigma_2^2 + \mu_2\sigma_1^2}{\sigma_1^2 + \sigma_2^2}$$

$$\sigma^2 = \frac{\sigma_1^2\sigma_2^2}{\sigma_1^2 + \sigma_2^2}$$

Prediction (estimate)

Measurement (noisy)



Deriving Kalman's Filter as the product of two Gaussians

$$x_1(r) \triangleq \frac{1}{\sqrt{2\pi\sigma_1^2}} e^{-\frac{(r-\mu_1)^2}{2\sigma_1^2}} \quad x_2(r) \triangleq \frac{1}{\sqrt{2\pi\sigma_2^2}} e^{-\frac{(r-\mu_2)^2}{2\sigma_2^2}}$$

Mean and variance of the new Gaussian given by the product of x_1 and x_2

$$\mu = \frac{\mu_1\sigma_2^2 + \mu_2\sigma_1^2}{\sigma_1^2 + \sigma_2^2} \quad \sigma^2 = \frac{\sigma_1^2\sigma_2^2}{\sigma_1^2 + \sigma_2^2}$$

$$\mu = \mu_1 + \frac{\sigma_1^2(\mu_2 - \mu_1)}{\sigma_1^2 + \sigma_2^2} \quad \sigma^2 = \sigma_1^2 - \frac{\sigma_1^2\sigma_1^2}{\sigma_1^2 + \sigma_2^2}$$

$$\hat{\mathbf{y}}_{k|k} = \hat{\mathbf{y}}_{k|k-1} + \mathbf{K}_k \mathbf{j}_k$$

$$\mathbf{P}_{k|k} = \mathbf{P}_{k|k-1} - \mathbf{K}_k \mathbf{H}_k \mathbf{P}_{k|k-1}$$

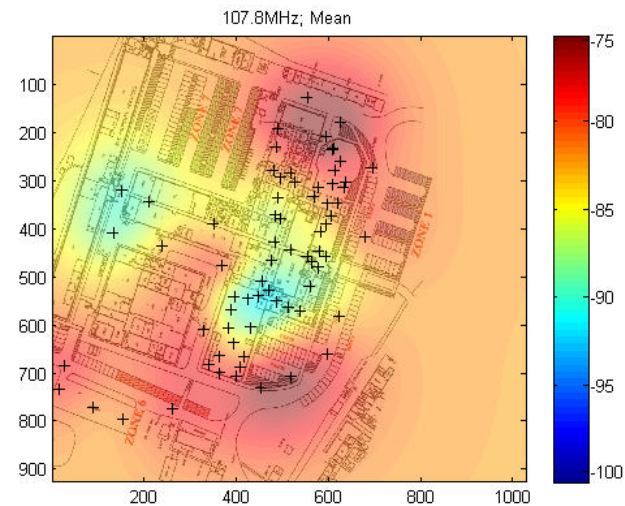
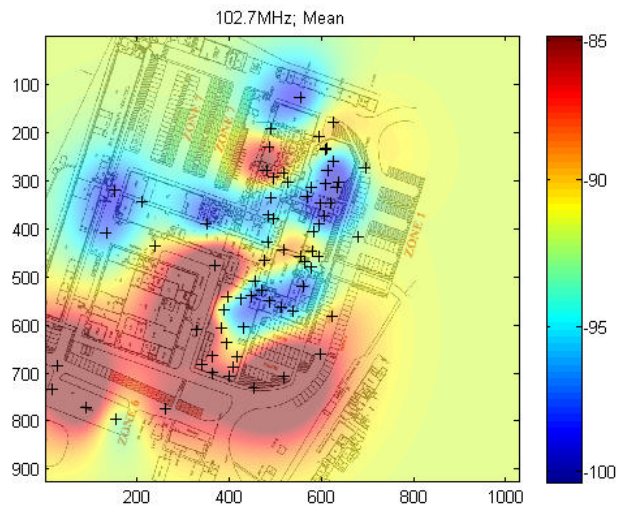
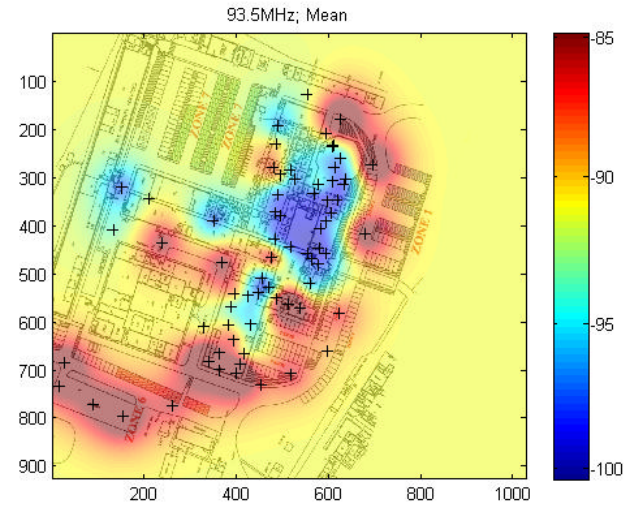
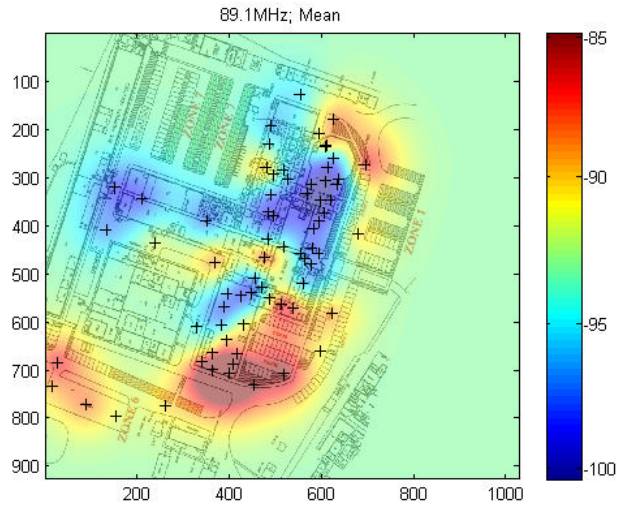
$$\mathbf{K}_k = \mathbf{P}_{k|k-1} \mathbf{H}_k^T (\mathbf{H}_k \mathbf{P}_{k|k-1} \mathbf{H}_k^T + \mathbf{R}_k)^{-1}$$

$$\mathbf{j}_k = \mathbf{z}_k - \mathbf{H}_k \hat{\mathbf{y}}_{k|k-1}$$

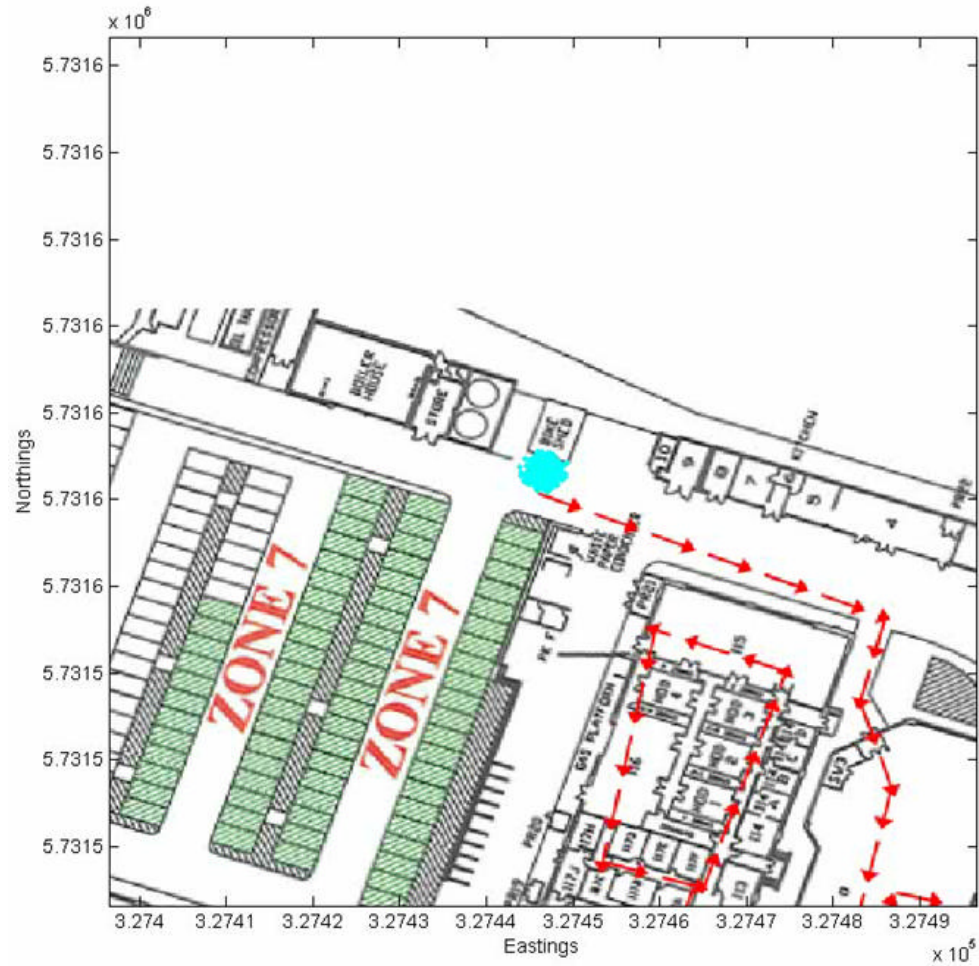
A new take on radio positioning

- Traditionally radio positioning has been “propagation based” – a critical assumption involves associating signal flight times to distances from transmitters
 - In complex signal environments (e.g. indoors) multipath interference corrupts timing measurements and dramatically reduces positioning accuracy
 - There is a great desire for GPS-like positioning indoors (emergency services, lone workers, security, smartphone apps, soldier tracking, etc)
 - The development of a new opportunistic radio positioning system than becomes *more accurate* in a *more complex* signal environment was required
 - Ideally the *complete absence* of a given signal should also provide useful positioning information – impossible for a timing-based system

Radio wallpaper (VHF FM 88 MHz – 108 MHz)



Simultaneous Localisation And Mapping



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**GRADUATE CAREERS IN
SCIENCE, ENGINEERING,
BUSINESS AND FINANCE,**



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WHO ARE WE?

- Europe's largest defence, security and aerospace company
- Global capability
- Customers in over 100 countries
- 100,000 highly skilled people
- Annual sales exceed £22.4 billion
- More than 100 new inventions each year



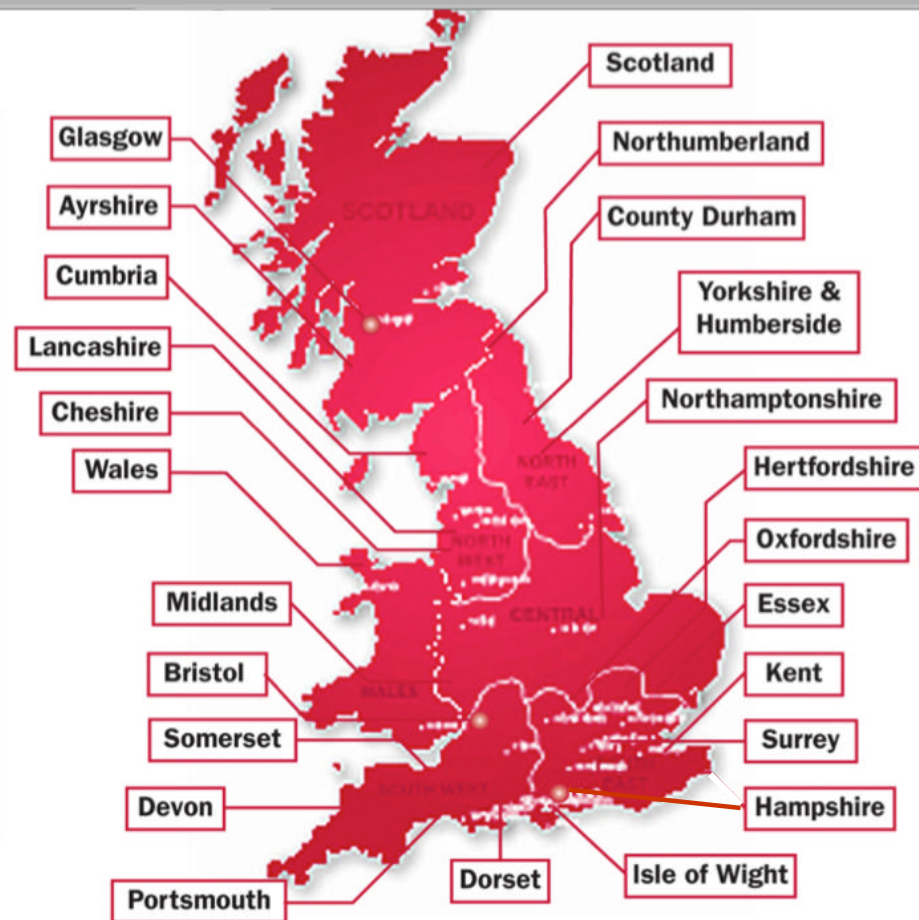
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WHERE ARE WE?

Main Business Units

- Platform Solutions
- Global Combat Systems
- Detica
- Maritime
- Military Air and Information



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WHAT DO WE DO?

Technology & Innovation

3D Ice Prediction tool - ICECREMO2

Advanced Materials & Processes

Advanced Welding Processes

Airborne Communications for UAVs

Antenna Systems

Bird Strike

Cleanroom Fabrication and Assembly

Communications Technology

Crash Analysis

Degaussing

Direct Write

Electronics and Packaging

Engineering Methods for Aerodynamic Characteristic Prediction

Flight-Qualified Embedded Electronics and Software

Greenlawn Communications Antenna Systems Laboratory (CASL)

Hydrodynamic Ram

Information Display and Visualisation

Infrared (IR) / Thermal Imaging as a Diagnostic Tool

Intelligence Solutions

Laser Engineering - 2 micron High Power Laser

Lightning, Electromagnetic Pulse (EMP) and Electrostatic Discharge (ESD)

Manufacturing Processes

MESAF

Military Imaging Applications

N'Connex Mission Capability Suite

Non-Destructive Test & Evaluation

Optical Sampling Techniques

Ad Hoc Networks

Advanced Propellant Guns

Aerodynamics

Airspeed Measurement System using a Laser

Antenna Test Chamber

Ceramic Composite Armor

Cognitive Radio

Computational Fluid Dynamics (CFD)

Data Diode

Design and Simulation of Fibre Optic Networks

Electromagnetics (EM)

Email Transfer Application

Experimental Impact Testing

Fibre Optic Sensors

Flite3D CFD code for Unstructured Euler Fluid Dynamics

High Availability Library (HAL)

Human Performance Modelling

Hyperspectral Imaging

Information Processing & Management

Infrared Signature Modelling and Measurement

Joint Expeditionary Forensic Facilities (JEFF)

Laser Surface Treatment of Materials

Long Range Hyperspectral Imaging System (LORHIS)

MAGNUM 4Mb Radiation-Hardened SRAM

Manufacturing Simulation

Micro Electromechanical Systems (MEMS)

Modelling of Composite Damage

Network Communications and Security

Optical Asse

Optical Sign

Advanced Armor Solutions

Advanced Waveforms

AGILE2

AN/VRC-99x Tactical Communications System

Beryllium mirrors

CirCube™

Communications

Control & Stabilisation

Data Forwarding Application

Design, Process & Product Optimisation

Electronic Press Kits (EPKs)

EMMA

Fibre Optic and Free-space Optical Communications

File Transfer Application

Gigabit Data Diode

Gimbal systems

Human Factors Integration

Human Sciences

Information Assurance

Information, Networked & Autonomous Systems

Installed Antenna Modelling

Joint Tactical Radio System (JTRS)

Lethality and Vulnerability Modelling

Low Frequency Modelling

Manufacturing

MEMS Services

Microwave Component Repair

Modelling of Resin Transfer Moulding

Network Enabled Capability (NEC)

Optical Sampling Techniques

Optical Sign

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Advanced Technology Centre (ATC)

- 400 world-leading scientists, mathematicians and engineers
- Research, development, consultancy, specialist manufacturing and technology brokering services.
- Defence, aerospace, security, space sector and commercial markets



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ATC Customers and Collaborators

- BAE Systems Business Units
- Ministry of Defence
- US Department of Defense
- European Space Agency
- UK Sport
- UK Emergency Services
- UK Transport Sector
- UK Security sector
- Dozens of Universities
- And many others.....

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Some of the ATC topics of interest

- ↘ Abnormal behaviour detection & video analytics
- ↘ Bio-inspired technologies
- ↘ Body-worn electronics
- ↘ Computational engineering & fluid dynamics
- ↘ Counter IED, detection & neutralisation
- ↘ Cyber Security
- ↘ Human Sciences
- ↘ Impact dynamics modelling and testing
- ↘ Less than lethal deterrents
- ↘ Micro & nanotechnology and smart materials
- ↘ Photonics and laser technologies
- ↘ Remote Sensing, radar & antenna development
- ↘ Reducing the burden on the dismounted soldier
- ↘ Stealth technology and materials
- ↘ Technologies for covert & secure operations
- ↘ Unmanned and autonomous systems

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Congratulations, you've reached your destination.....

