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Discuss the pros and cons of call-by-value and call-by-name semantics.

Consider the syntax of the following pure functional language

$$\begin{array}{ll} e & ::= & n \mid \mathbf{fn} \quad x{:}T \Rightarrow e \mid e \ e \mid x \mid \Omega \\ T & ::= & \operatorname{int} \mid T \rightarrow T \end{array}$$

[3]

where the static and dynamic semantics of Ω are given by rules

$$\begin{array}{ll} \text{(omega)} & \overline{\Gamma \vdash \Omega\text{:int}} & \text{(omega)} & \Omega \longrightarrow \Omega \end{array}$$

Give typing rules and CBN dynamic semantic rules for the other constructs. [6]

Give an expression that would behave differently in the CBV and CBN semantics, and give its final state in each (if any). [2]

For this language, the desired type preservation result would be of the form "If $\Gamma \vdash e:T$ and $e \longrightarrow e'$ then $\Gamma \vdash e':T$ ". In proving that, a substitution lemma would be required. Give a statement and proof of that substitution lemma. [9]